Whatever can go wrong
will go wrong.

attributed to Edward A. Murphy

Murphy was an optimist.

authors of lock-free programs

3. LOCK FREE KERNEL

Literature

Maurice Herlihy and Nir Shavit. *The Art of Multiprocessor Programming*. Morgan Kaufmann Publishers Inc., San Francisco, CA, USA, 2008.

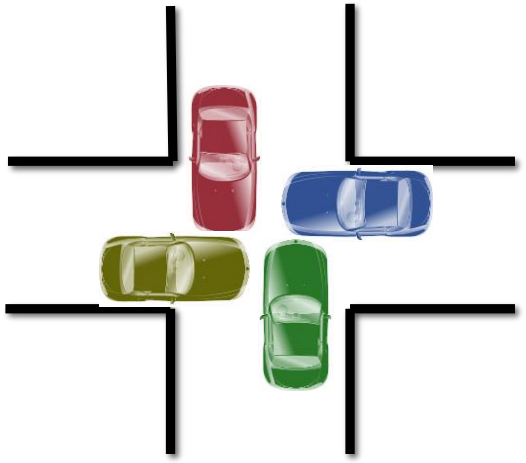
Florian Negele. *Combining Lock-Free Programming with Cooperative Multitasking for a Portable Multiprocessor Runtime System.* ETH-Zürich, 2014. http://dx.doi.org/10.3929/ethz-a-010335528

A substantial part of the following material is based on Florian Negele's Thesis.

Florian Negele, Felix Friedrich, Suwon Oh and Bernhard Egger, *On the Design and Implementation of an Efficient Lock-Free Scheduler,* 19th Workshop on Job Scheduling Strategies for Parallel Processing (JSSPP) 2015.

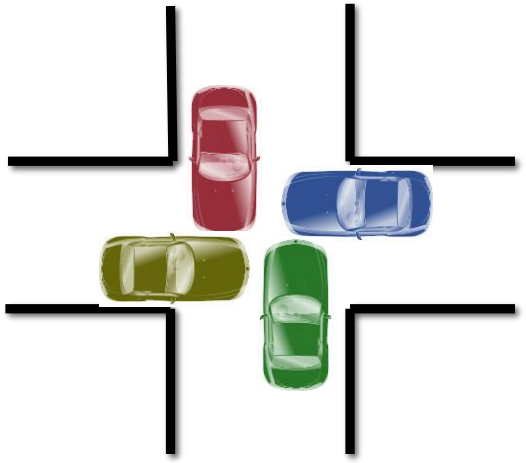
Problems with Locks

Problems with Locks

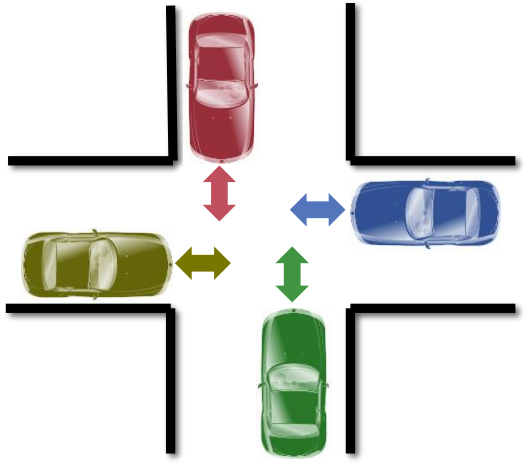


Deadlock

Problems with Locks

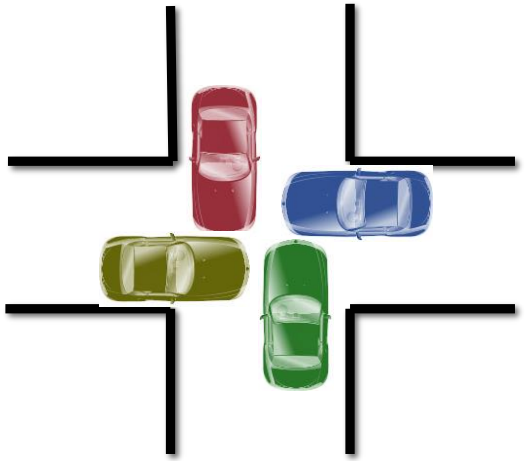


Deadlock

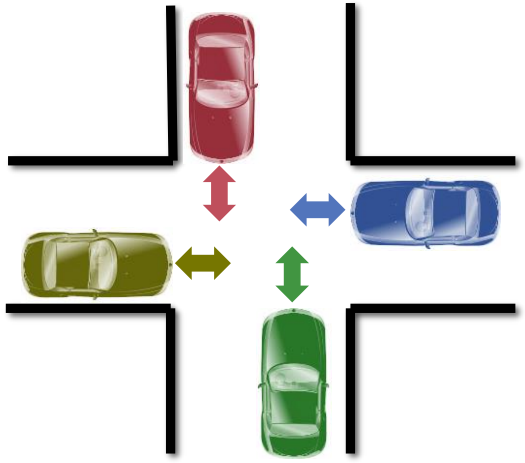


Livelock

Problems with Locks



Deadlock



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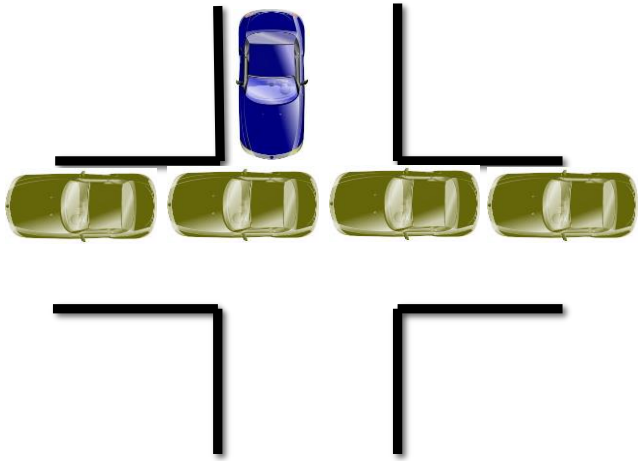
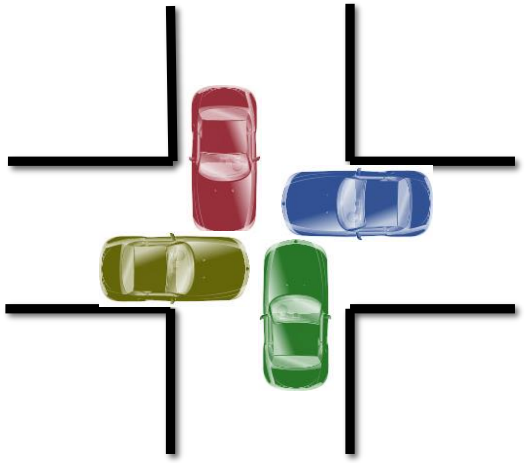
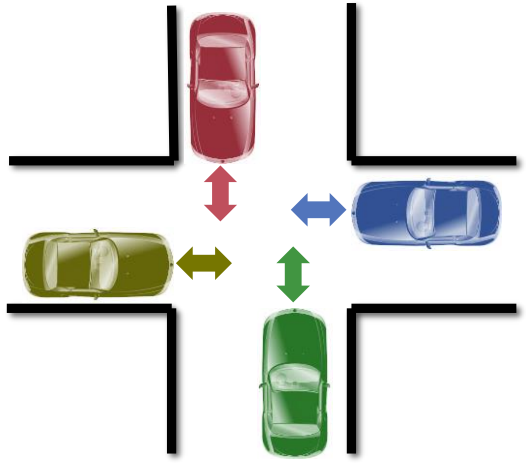


Starvation

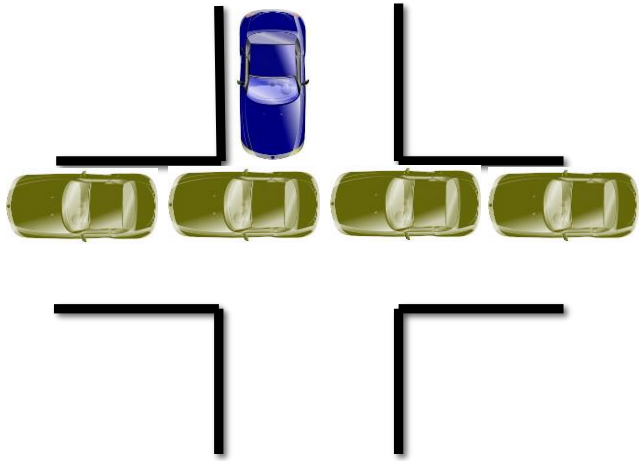
Problems with Locks



Deadlock



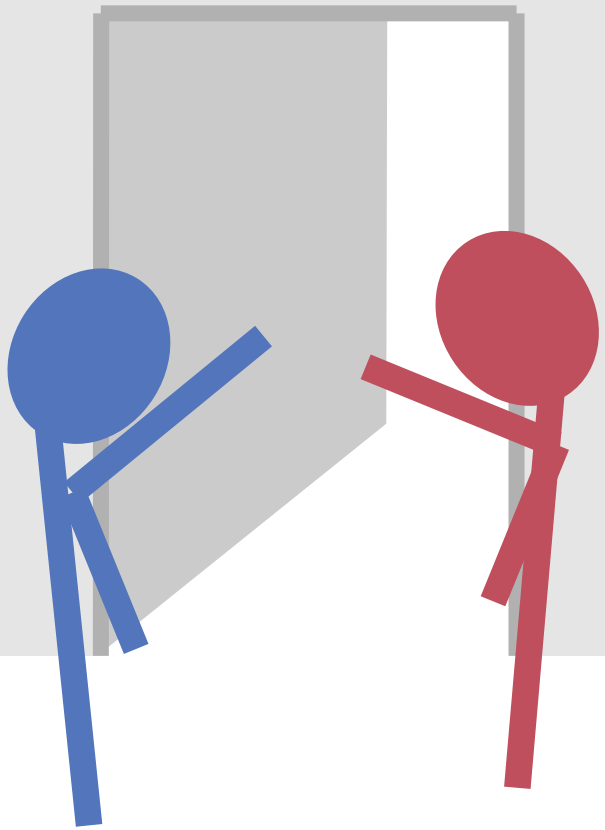
Livelock



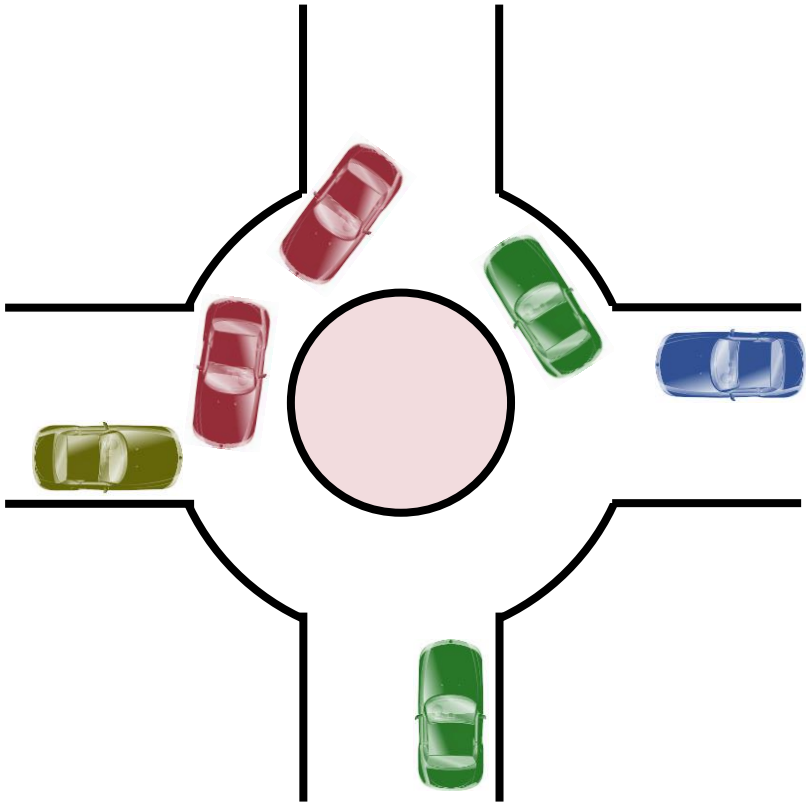
Starvation

Parallelism? Progress Guarantees? Reentrancy? Granularity? Fault Tolerance?

Politelock



Lock-Free



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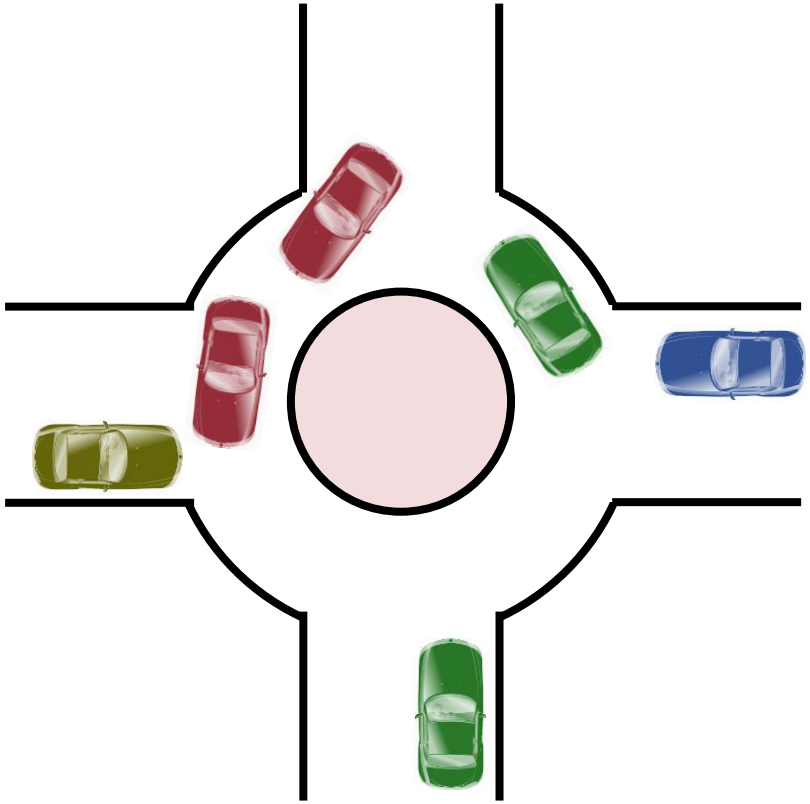

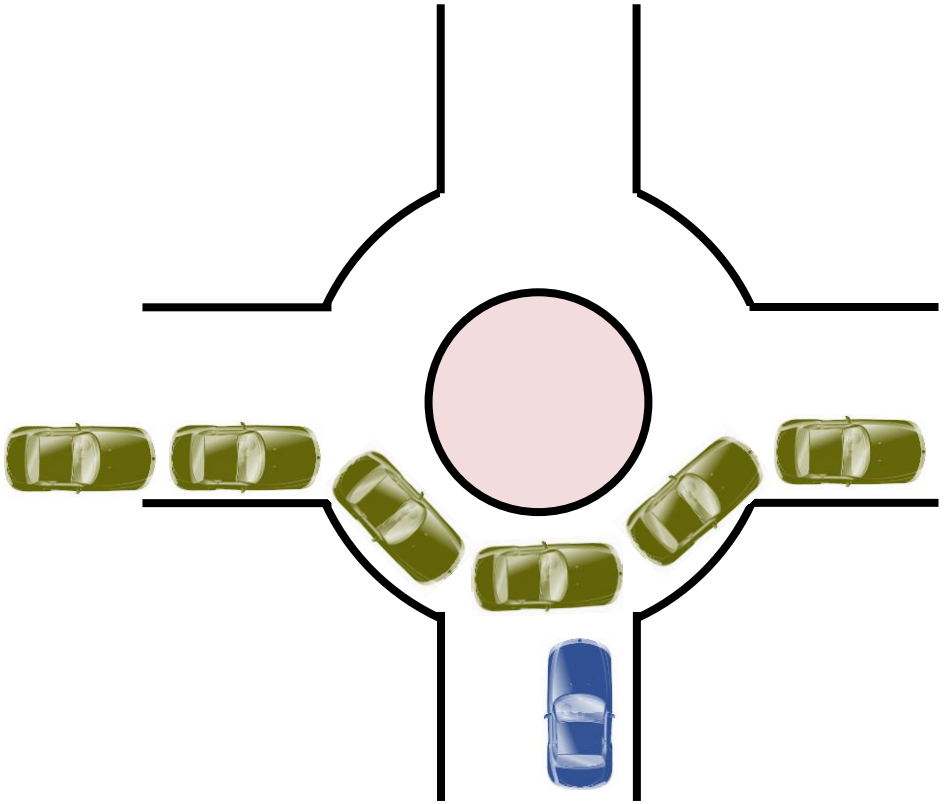

Definitions

Lock-freedom: at least one algorithm makes progress even if other algorithms run concurrently, fail or get suspended.
Implies system-wide progress but not freedom from starvation.

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Implies freedom from starvation.

Progress Conditions

	Blocking	Non-Blocking
Someone make progress	Deadlock-free	**Lock-free**
Everyone makes progress	Starvation-free	Wait-free

Goals

Goals

Lock Freedom

- Progress Guarantees
- Reentrant Algorithms

Goals

Portability

- Hardware Independence
- Simplicity, Maintenance

Guiding principles

1. Keep things **simple**
2. Exclusively employ **non-blocking** algorithms in the system

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1. Keep things **simple**
2. Exclusively employ **non-blocking** algorithms in the system

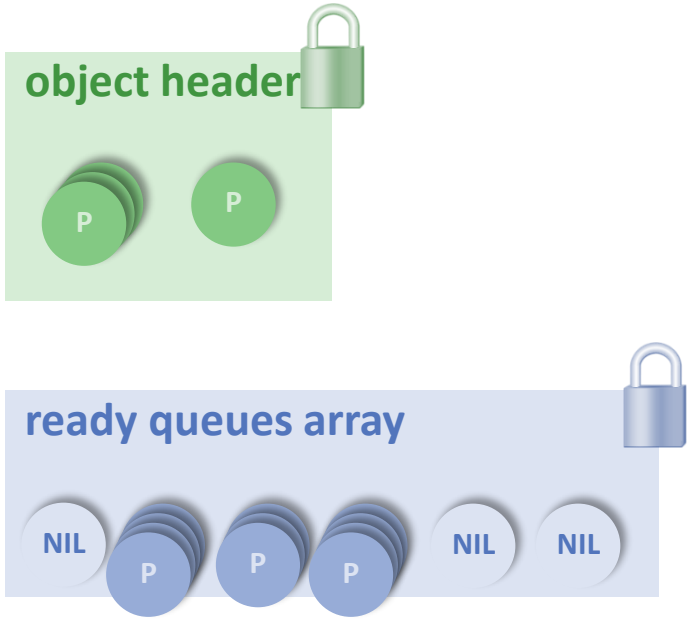
→ Use **implicit cooperative multitasking**

→ no virtual memory

→ limits in optimization

Where are the Locks in the Kernel?

Scheduling Queues / Heaps



Memory Management

CAS (again)

int CAS (memref a, int old, int new)

atomic

CAS (again)

- Compare **old** with data at memory location

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previous = mem[a];

CAS (again)

- Compare **old** with data at memory location

- If and only if data at memory equals **old** overwrite data with **new**

int CAS (memref a, int old, int new)

atomic

```
previous = mem[a];
if (old == previous)
    Mem[a] = new;
```

CAS (again)

- Compare **old** with data at memory location
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- Return previous memory value

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CAS (again)

- Compare **old** with data at memory location
- If and only if data at memory equals **old** overwrite data with **new**
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```
int CAS (memref a, int old, int new)
atomic {
    previous = mem[a];
    if (old == previous)
        Mem[a] = new;
    return previous;
}
```

CAS is implemented wait-free(!) by hardware.

Memory Model for Lockfree Active Oberon

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Only **two rules**

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1. **Data shared** between two or more activities at the same time has to be **protected using exclusive blocks** unless the data is read or modified using the compare-and-swap operation

Memory Model for Lockfree Active Oberon

Only **two rules**

1. **Data shared** between two or more activities at the same time has to be **protected using exclusive blocks** unless the data is read or modified using the compare-and-swap operation
2. Changes to shared data **visible to other activities after leaving an exclusive block or executing a compare-and-swap** operation.

   Implementations are free to reorder all other memory accesses as long as their effect equals a sequential execution within a single activity.

Inbuilt CAS

- CAS instruction as statement of the language

```
PROCEDURE CAS(VAR variable, old, new: BaseType): BaseType
```

  - Operation executed atomically, result visible instantaneously to other processes
  - CAS(variable, x, x) constitutes an atomic read

Inbuilt CAS

- CAS instruction as statement of the language

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```

  - Operation executed atomically, result visible instantaneously to other processes
  - CAS(variable, x, x) constitutes an atomic read
- Compiler required to implement CAS as a synchronisation barrier
  - Portability, even for non-blocking algorithms
  - Consistent view on shared data, even for systems that represent words using bytes

Simple Example: Non-blocking counter

```
PROCEDURE Increment(VAR counter: LONGINT): LONGINT;
VAR previous, value: LONGINT;
BEGIN
   REPEAT
      previous := CAS(counter,0,0);
      value := CAS(counter, previous, previous + 1);
   UNTIL value = previous;
   return previous;
END Increment;
```

Lock-Free Programming

Lock-Free Programming

Performance of CAS

- on the H/W level, CAS triggers a memory barrier
- performance suffers with increasing number of contenders to the same variable

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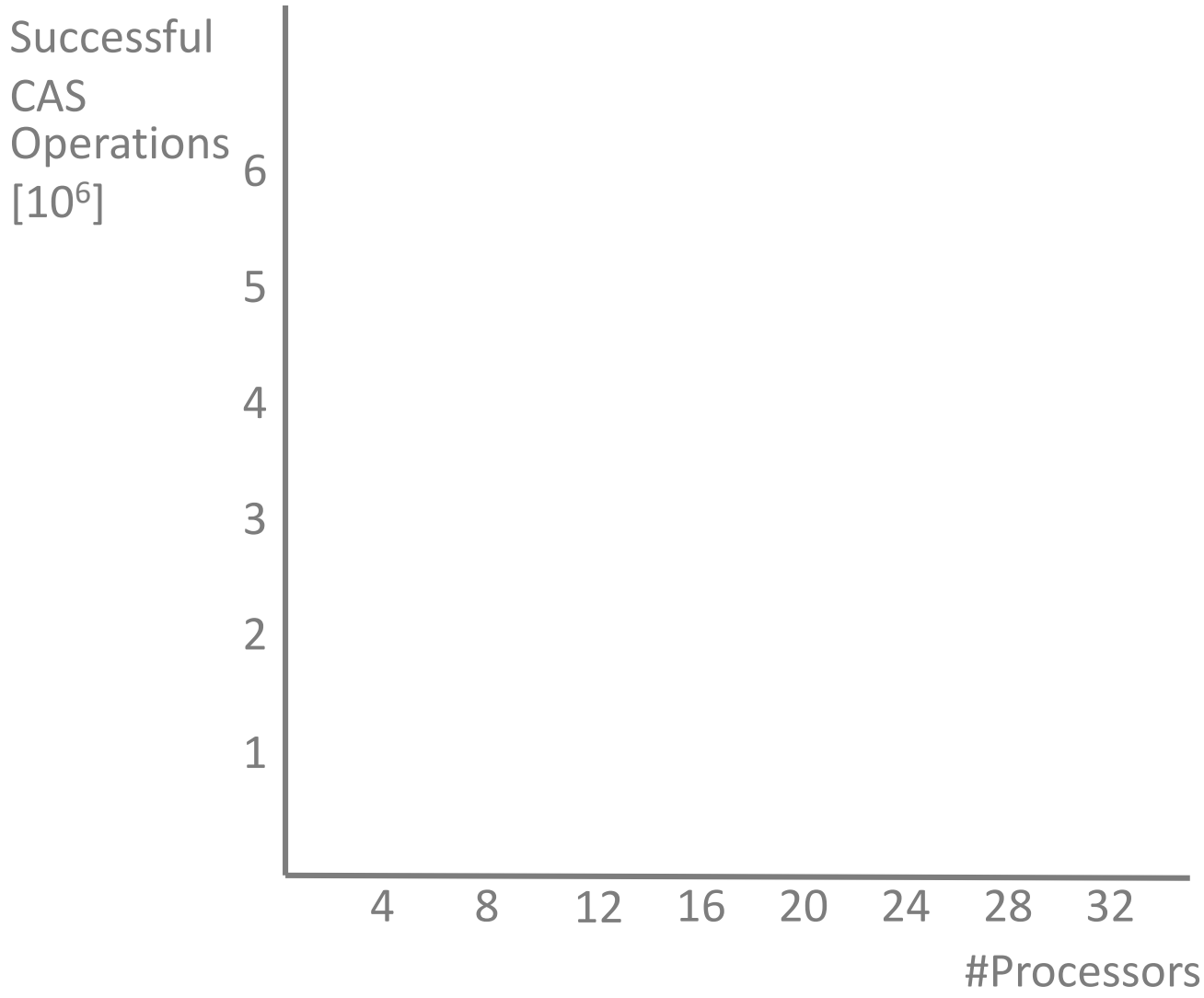

Lock-Free Programming

Performance of CAS

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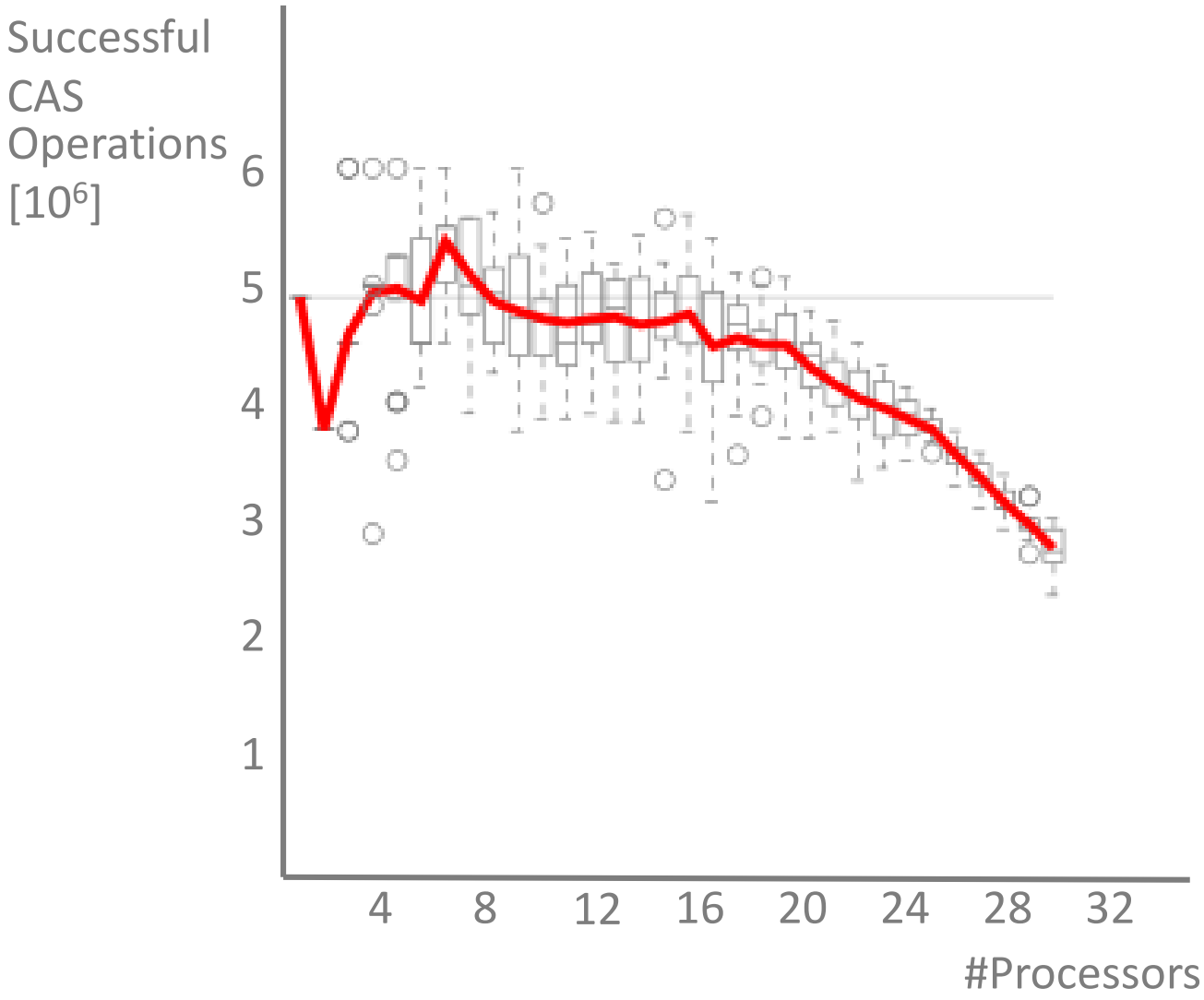
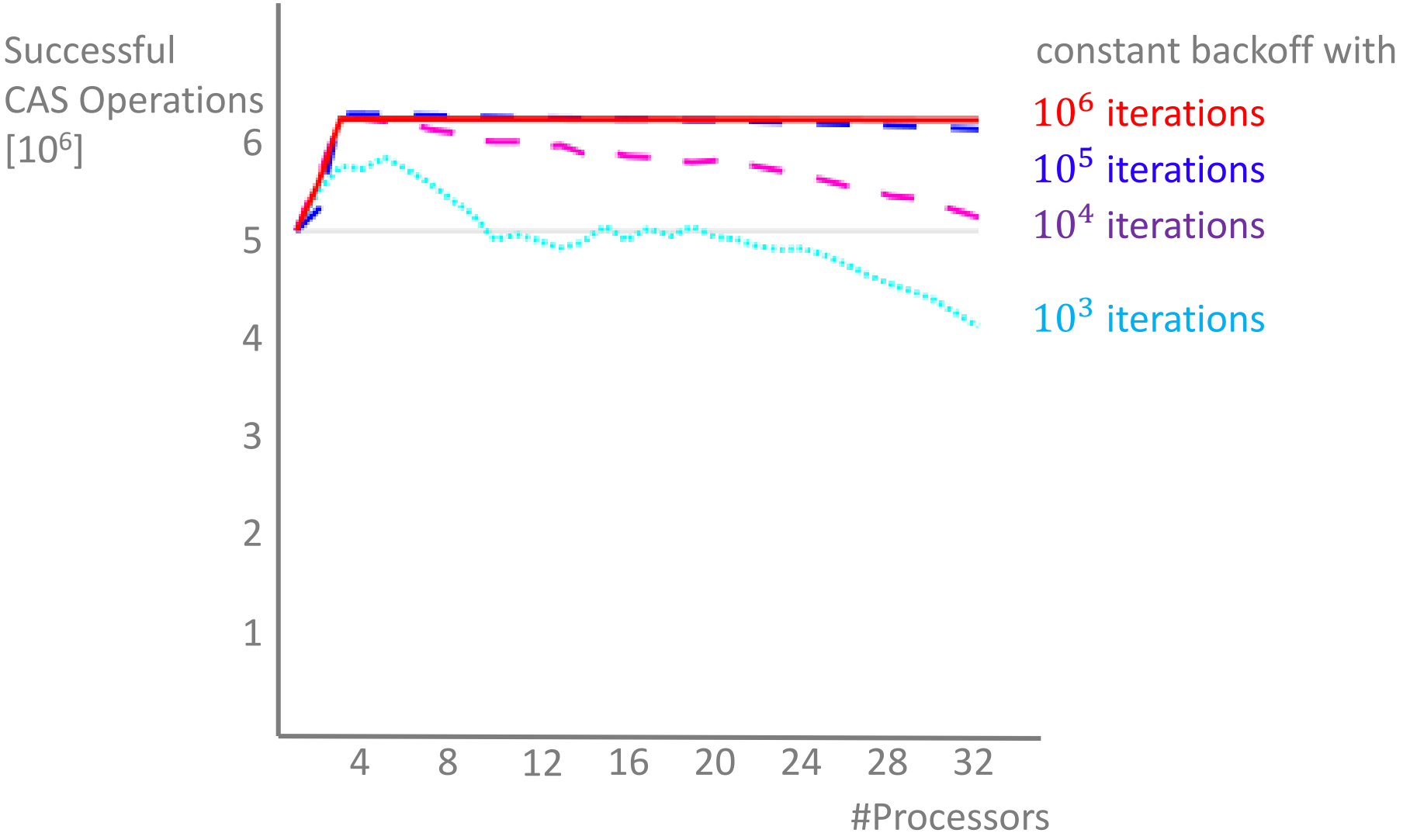
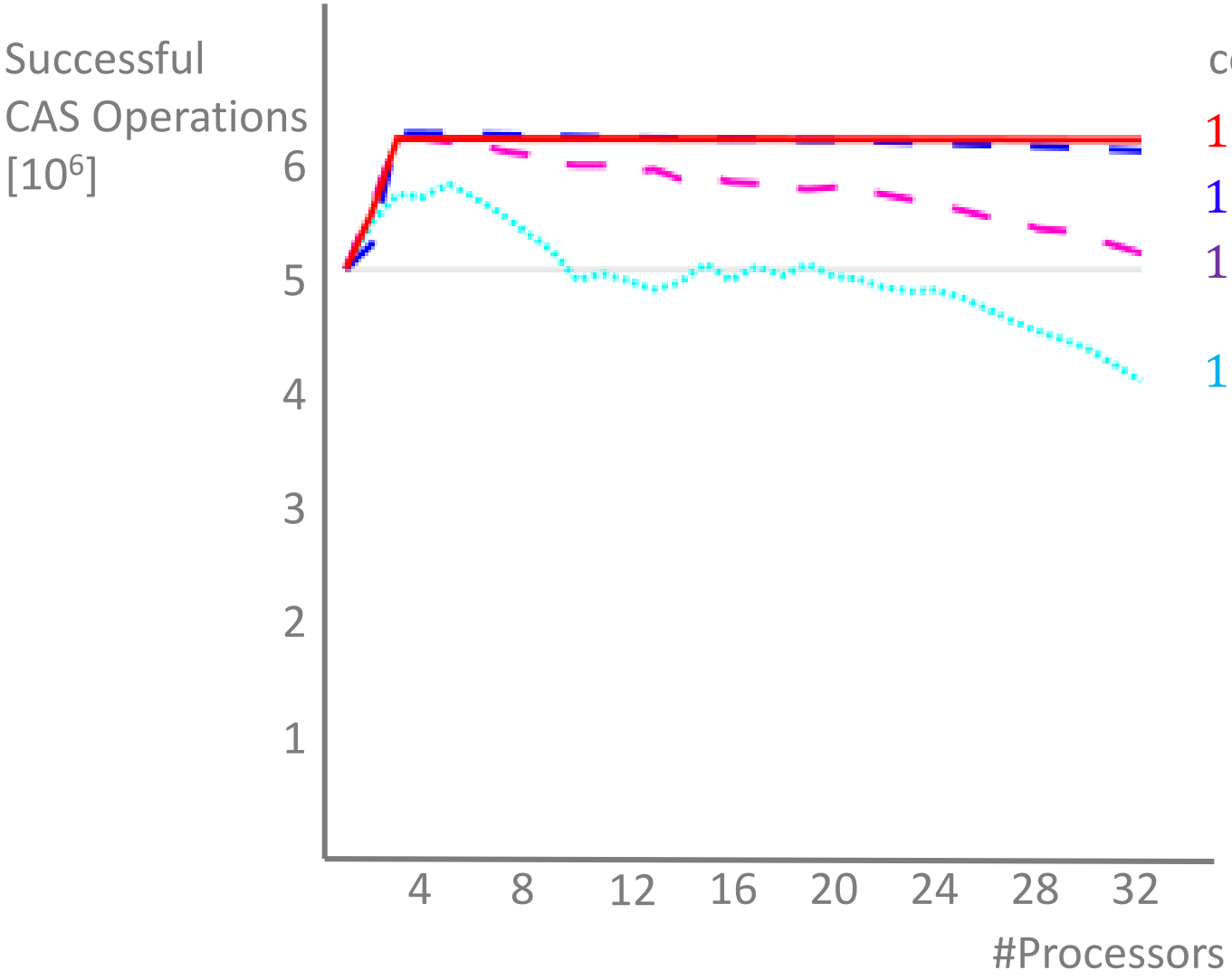


CAS with backoff



CAS with backoff



constant backoff with

10^6 iterations

10^5 iterations

10^4 iterations

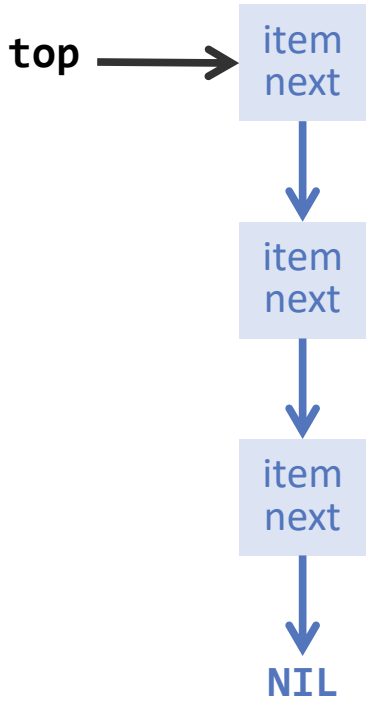
10^3 iterations

```
LOOP
    value := CAS (counter, 0, 0);
    IF CAS (counter, v, v+1) = v THEN
        EXIT
    END;
    CPU.Backoff;
END;
```

Stack

```
Node = POINTER TO RECORD
  item: Object;
  next: Node;
END;

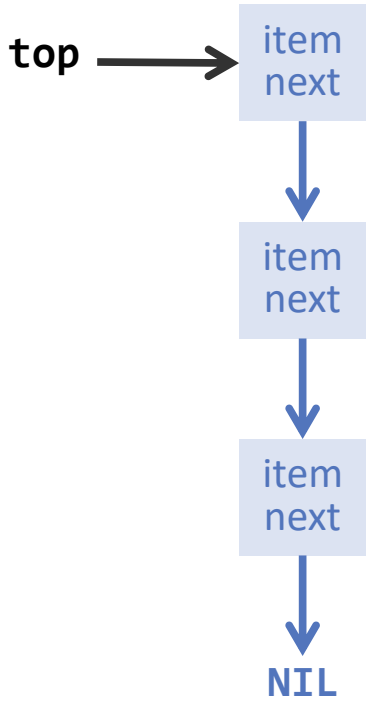
Stack = OBJECT
VAR top: Node;
  PROCEDURE Pop(VAR head: Node): BOOLEAN;
  PROCEDURE Push(head: Node);
END;
```



Stack -- Blocking

```
PROCEDURE Push(node: Node): BOOLEAN;
BEGIN{EXCLUSIVE}
   node.next := top;
   top := node;
END Push;

PROCEDURE Pop(VAR head: Node): BOOLEAN;
VAR next: Node;
BEGIN{EXCLUSIVE}
   head := top;
   IF head = NIL THEN
      RETURN FALSE
   ELSE
      top := head.next;
      RETURN TRUE;
   END;
END Pop;
```

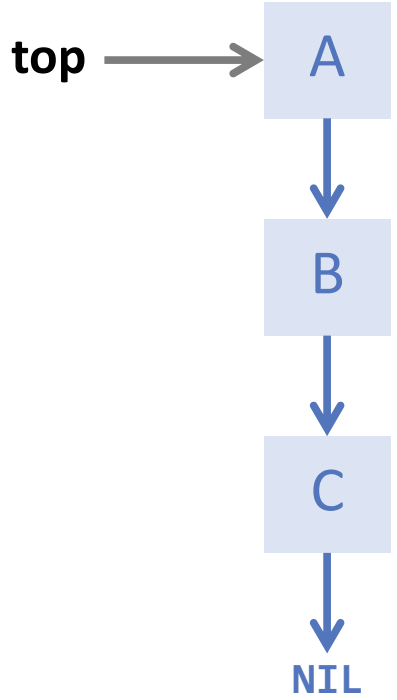


Stack -- Lockfree

```
PROCEDURE Pop(VAR head: Node): BOOLEAN;
VAR next: Node;
BEGIN




END Pop;
```



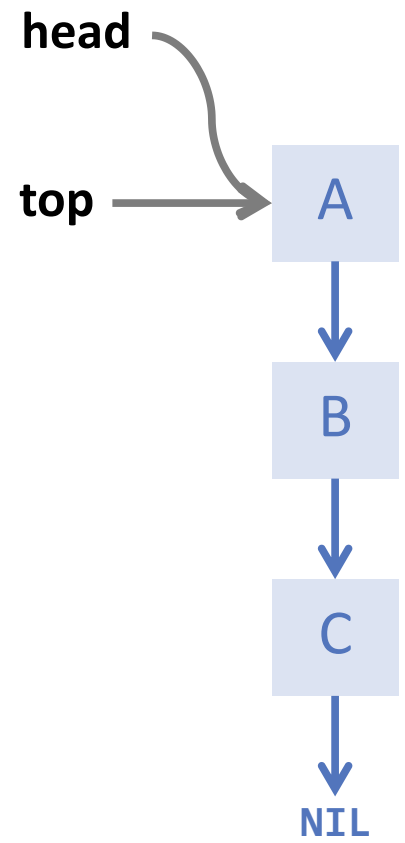
Stack -- Lockfree

```
PROCEDURE Pop(VAR head: Node): BOOLEAN;
VAR next: Node;
BEGIN

     head := CAS(top, NIL, NIL);
     IF head = NIL THEN
        RETURN FALSE
     END;
     next := head.next;




END Pop;
```



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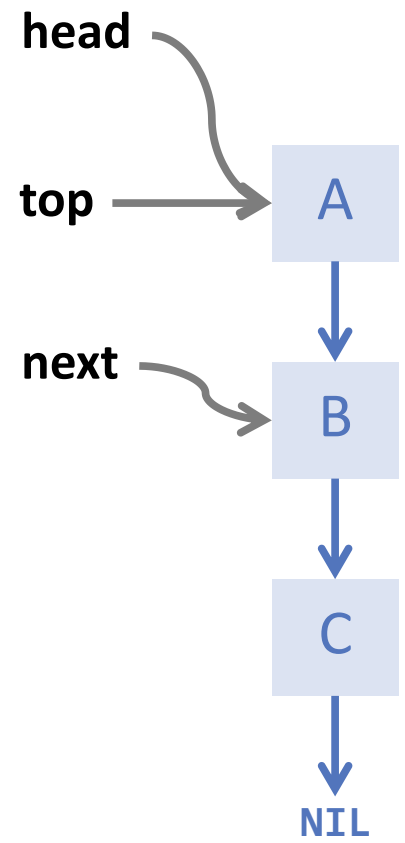

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      IF CAS(top, head, next) = head THEN
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      END;


END Pop;
```
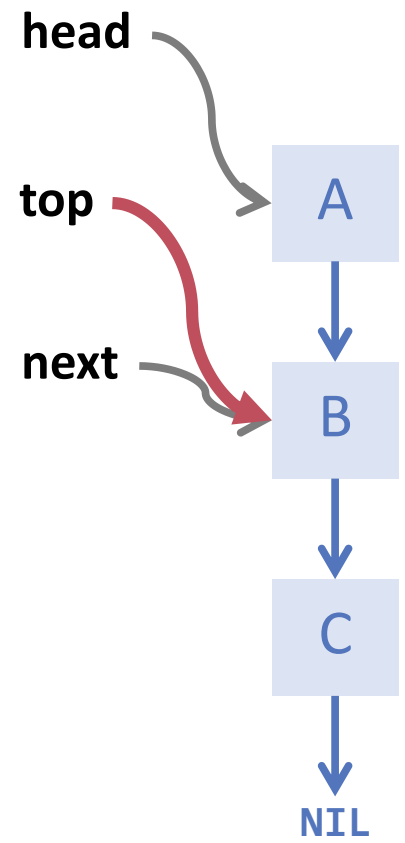
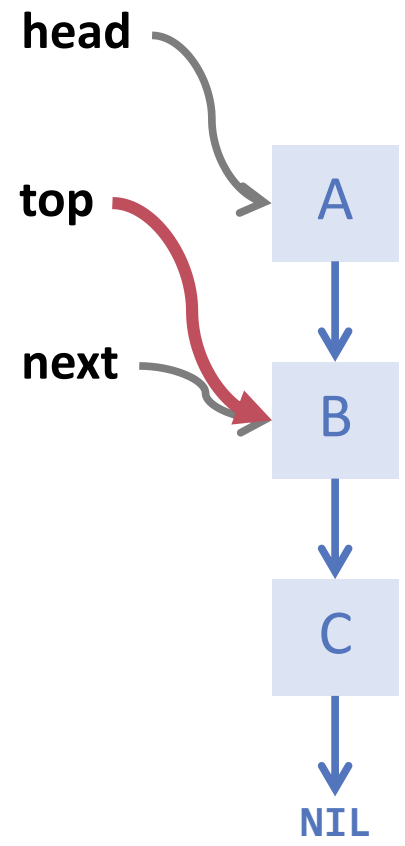



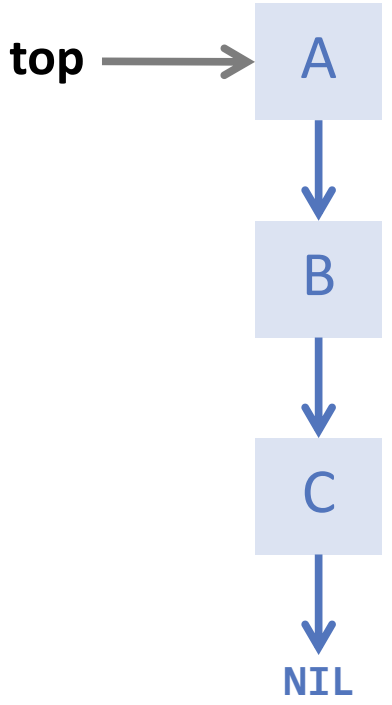
Stack -- Lockfree

```
PROCEDURE Pop(VAR head: Node): BOOLEAN;
VAR next: Node;
BEGIN
   LOOP
      head := CAS(top, NIL, NIL);
      IF head = NIL THEN
         RETURN FALSE
      END;
      next := head.next;
      IF CAS(top, head, next) = head THEN
         RETURN TRUE
      END;
      CPU.Backoff
   END;
END Pop;
```



Stack -- Lockfree

```
PROCEDURE Push(new: Node);
BEGIN




END Push;
```



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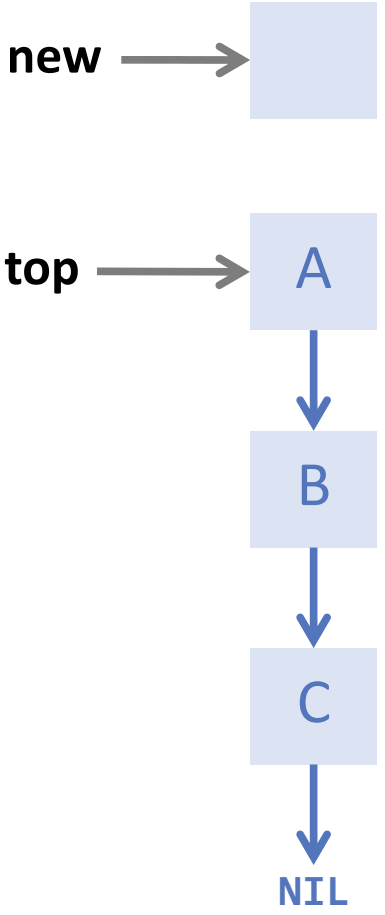

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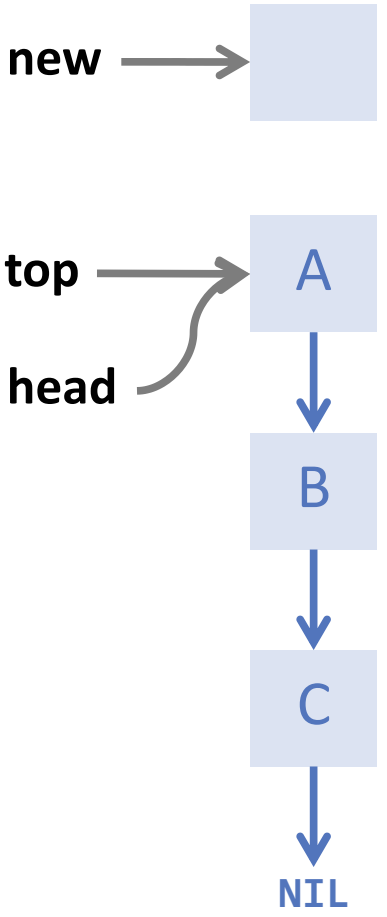
BEGIN

      head := CAS(top, NIL, NIL);
      new.next := head;




END Push;
```



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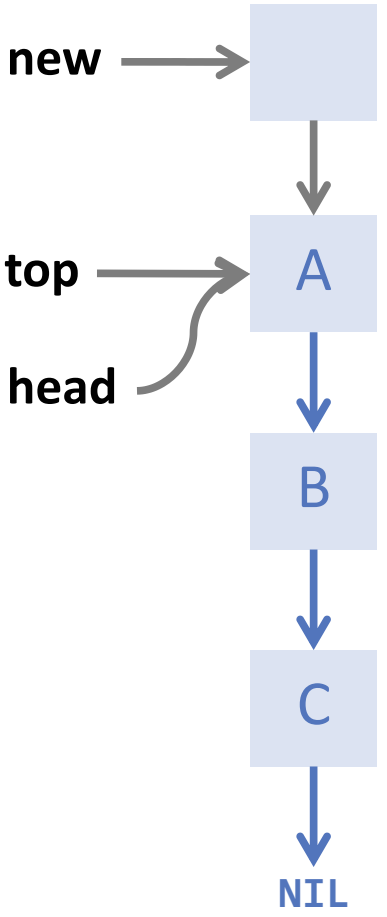
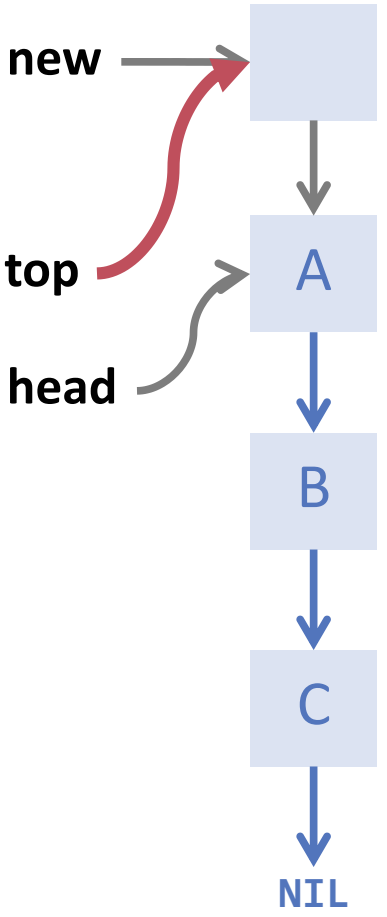


Stack -- Lockfree

```
PROCEDURE Push(new: Node);
BEGIN

      head := CAS(top, NIL, NIL);
      new.next := head;
      IF CAS(top, head, new) = head THEN
         EXIT
      END;


END Push;
```



Stack -- Lockfree

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      IF CAS(top, head, new) = head THEN
         EXIT
      END;
      CPU.Backoff;
   END;
END Push;
```
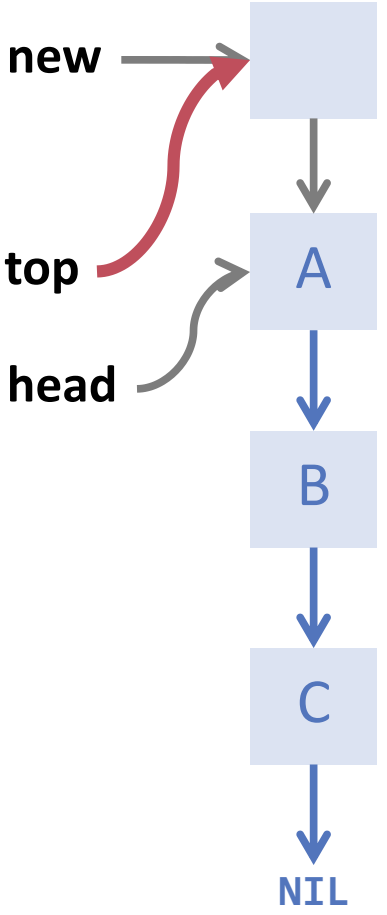



Node Reuse

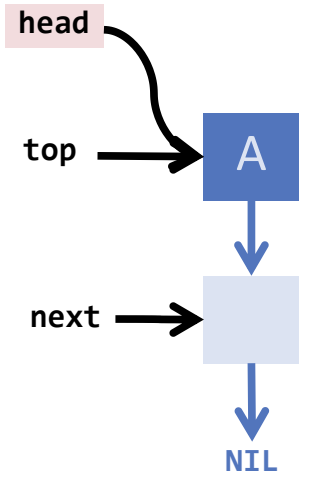
Assume we do not want to allocate a new node for each Push and maintain a Node-pool instead. Does this work?

NO ! WHY NOT?

ABA Problem

ABA Problem

Thread X
in the middle
of pop: after read
but before CAS



ABA Problem

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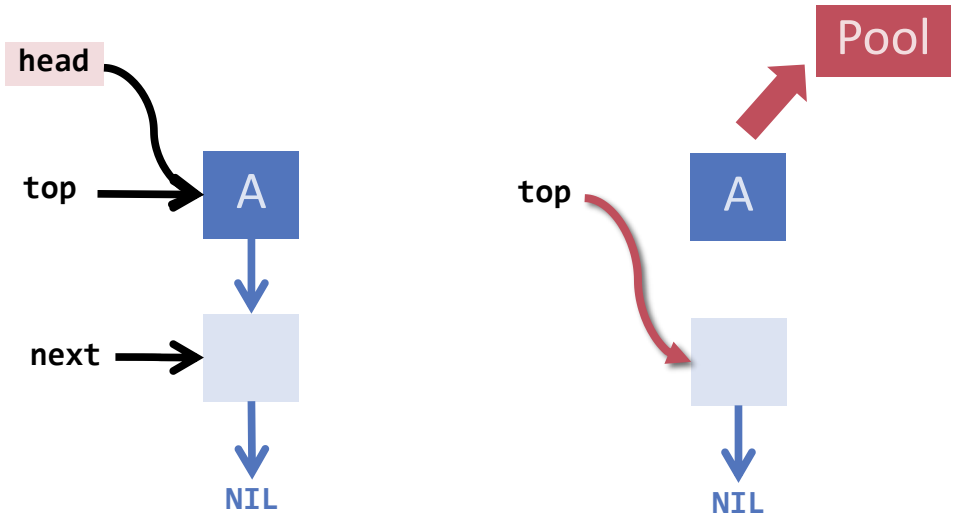
pops A



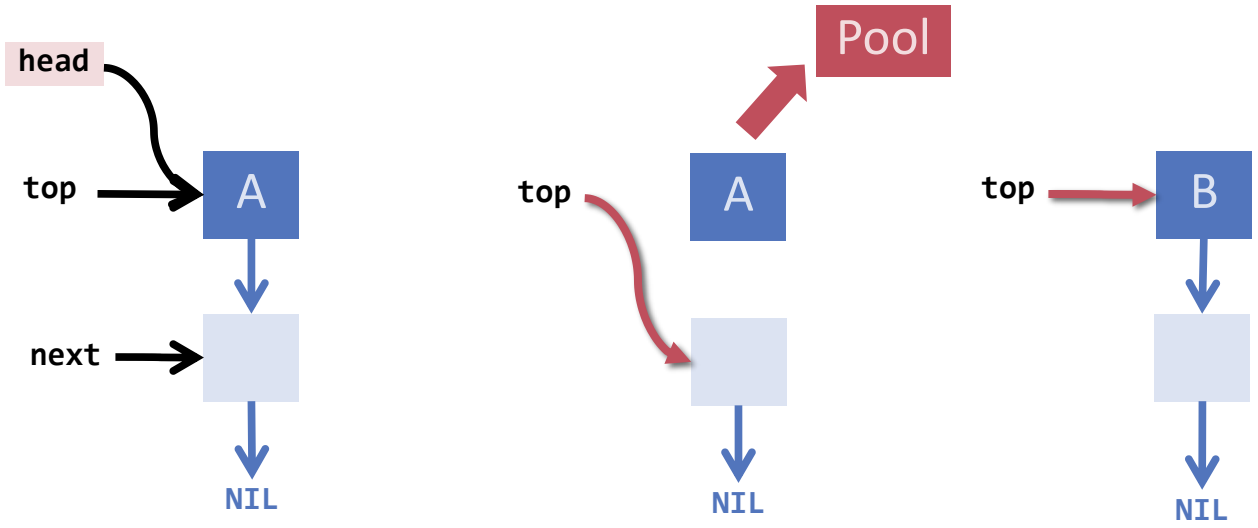
time

ABA Problem

Thread X
in the middle
of pop: after read
but before CAS

Thread Y
pops A

Thread Z
pushes B



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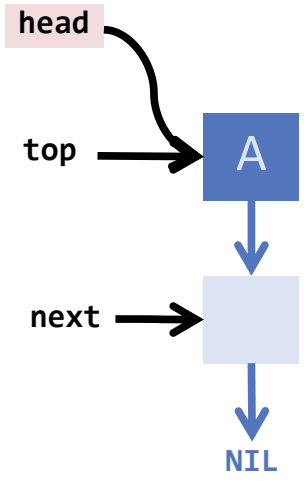

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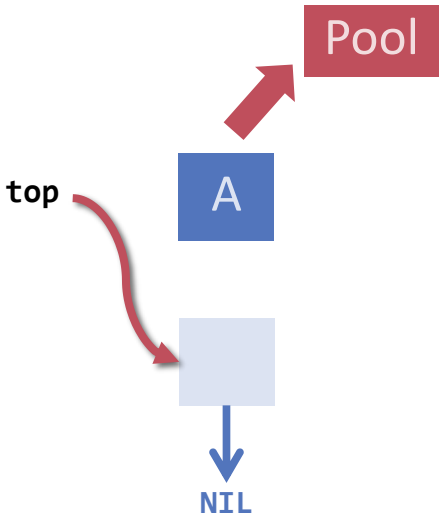
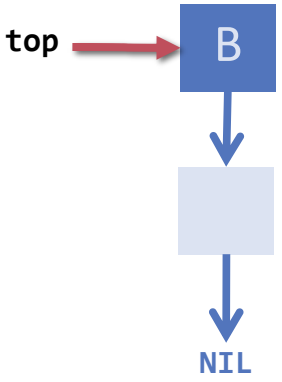
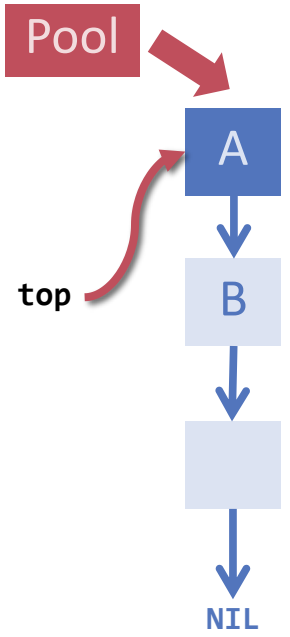
pops A



Thread Z
pushes B



Thread Z'
pushes A



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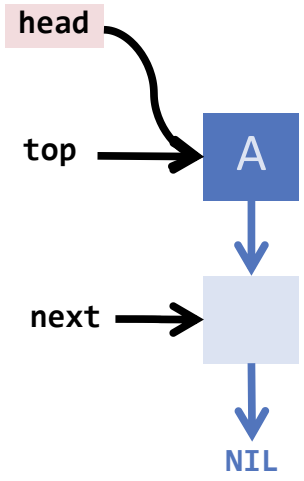

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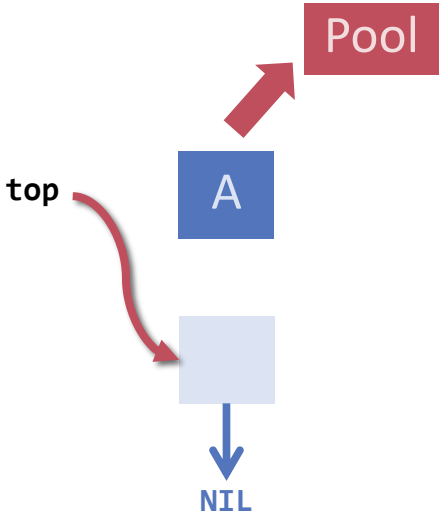
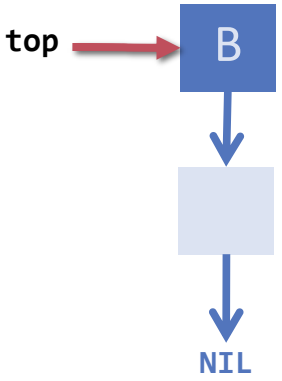


Thread Z
pushes B



Thread Z'
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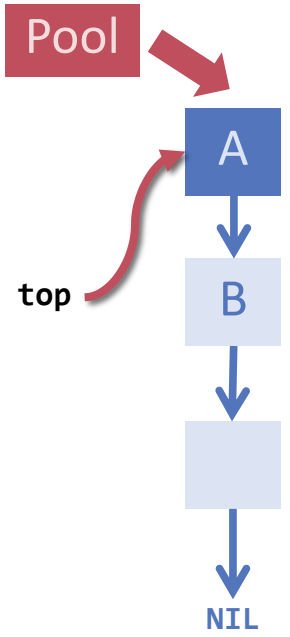
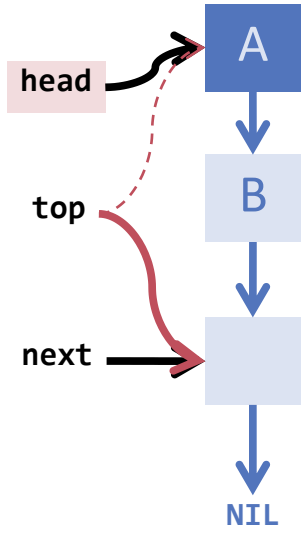


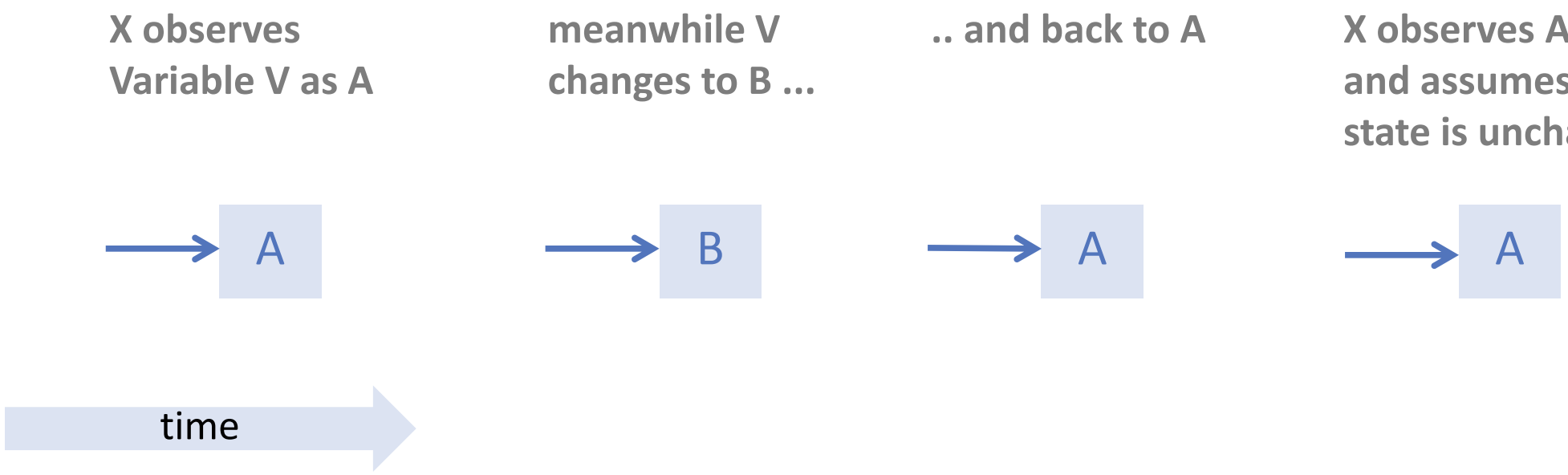
Thread X
completes pop



time

The **ABA**-Problem

"The ABA problem ... occurs when one activity fails to recognise that a single memory location was modified temporarily by another activity and therefore erroneously assumes that the overal state has not been changed."



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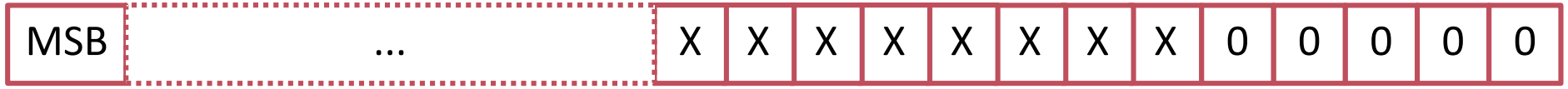

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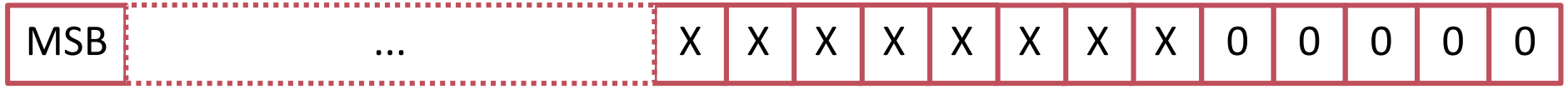

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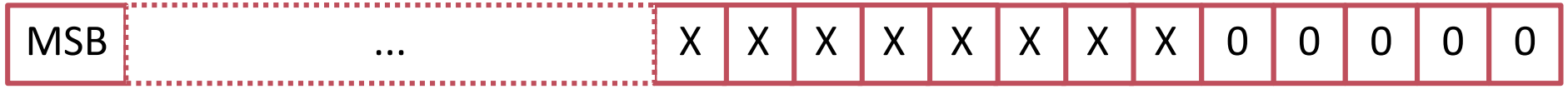

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This makes the ABA problem very much less probable because now 32 versions of each pointer exist.

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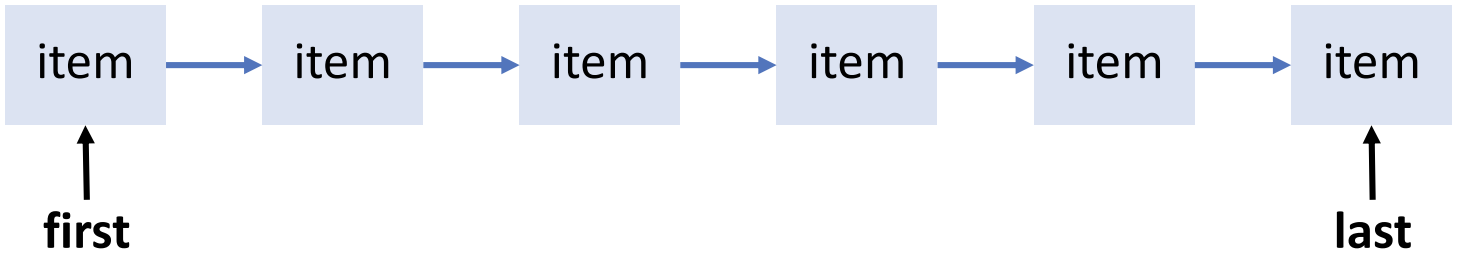
- Before a process Y tries to reuse P, it checks all entries of the hazard array

Unbounded Queue (FIFO)



Enqueue

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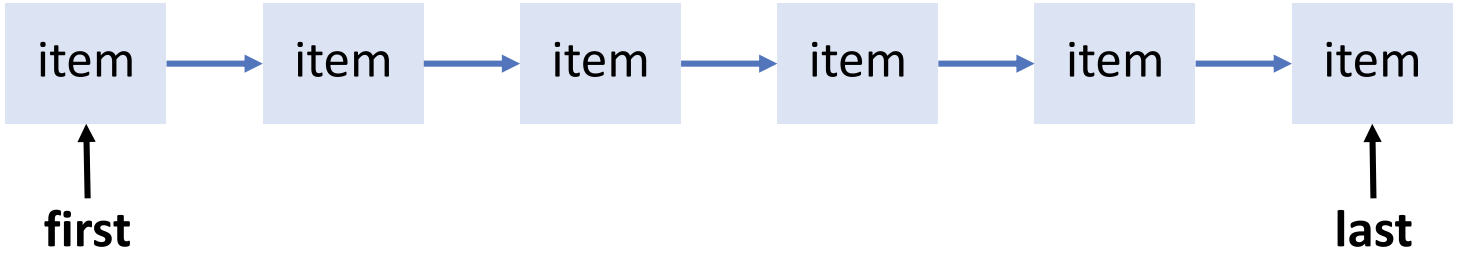

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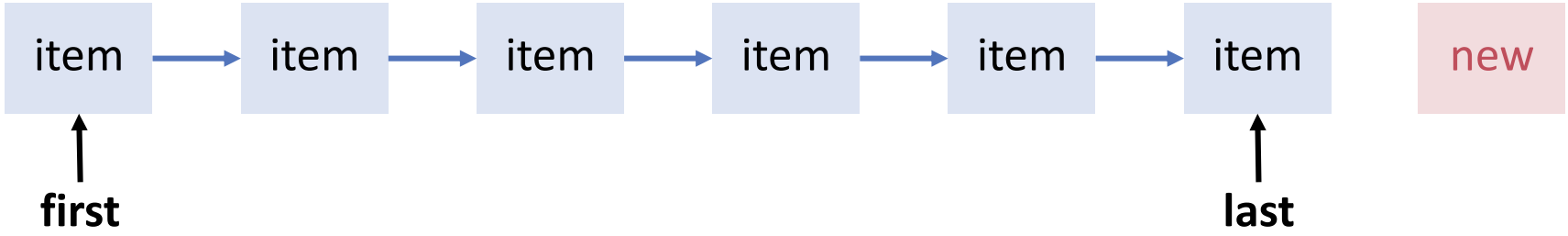

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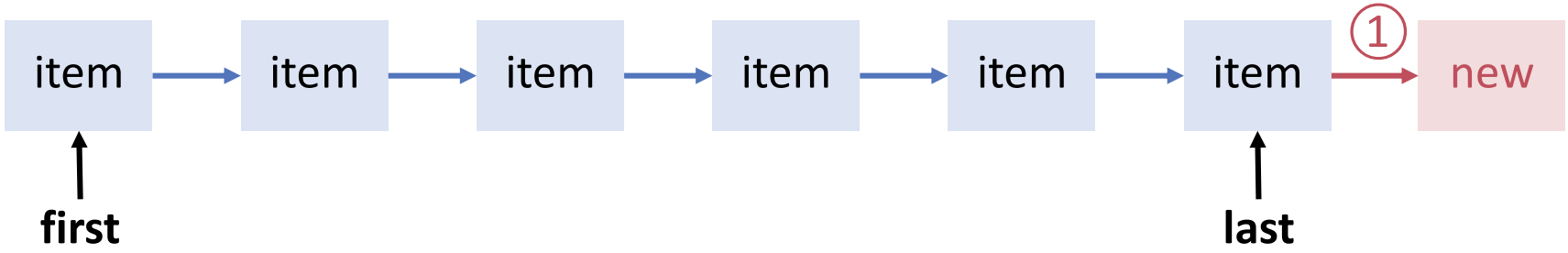

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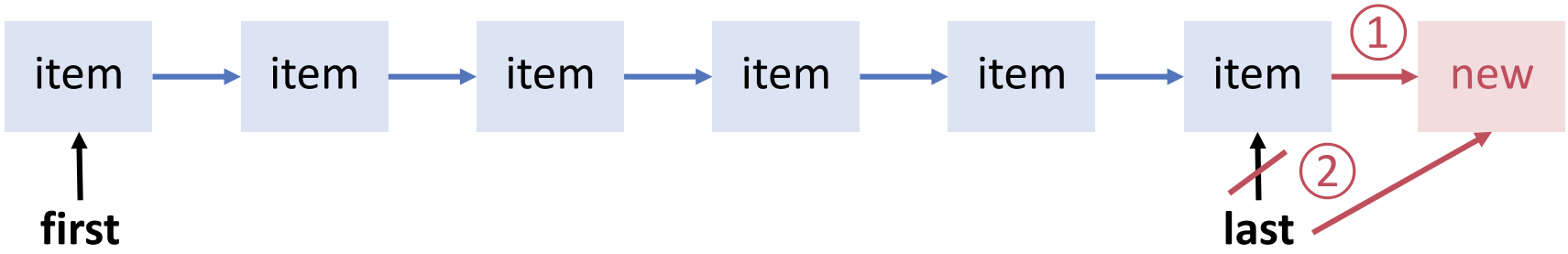

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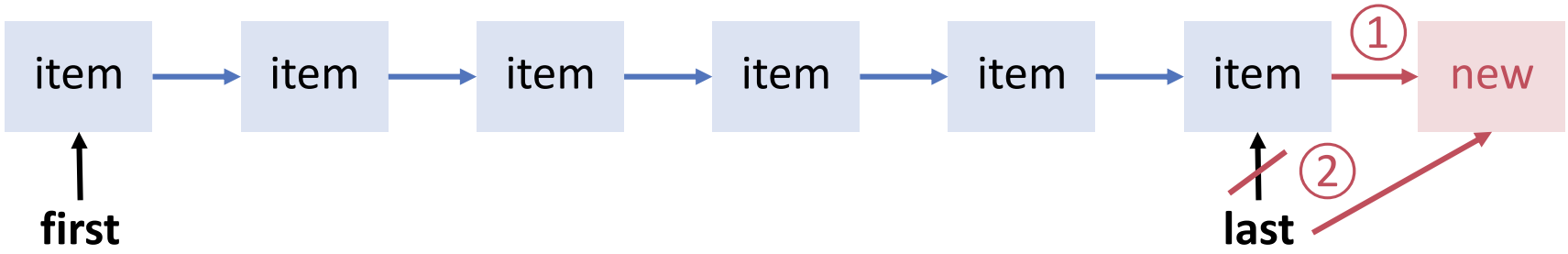

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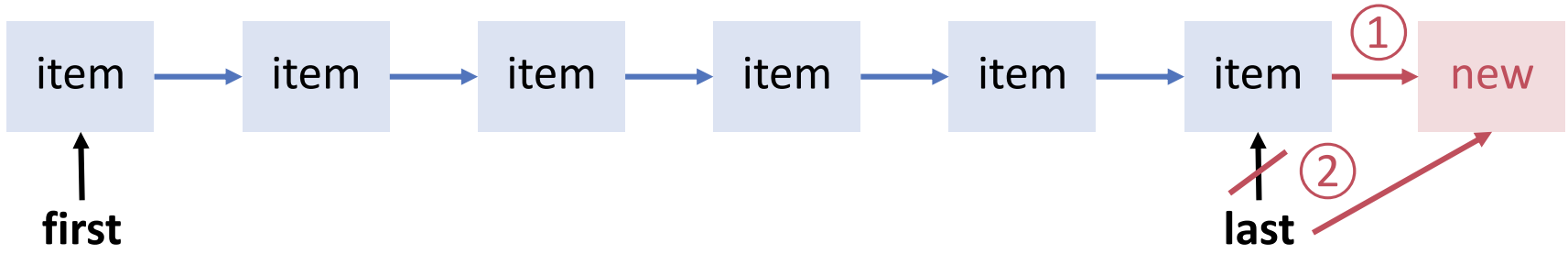

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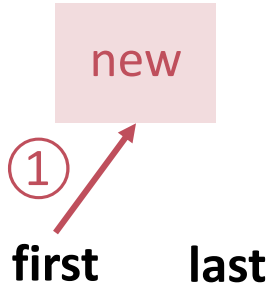

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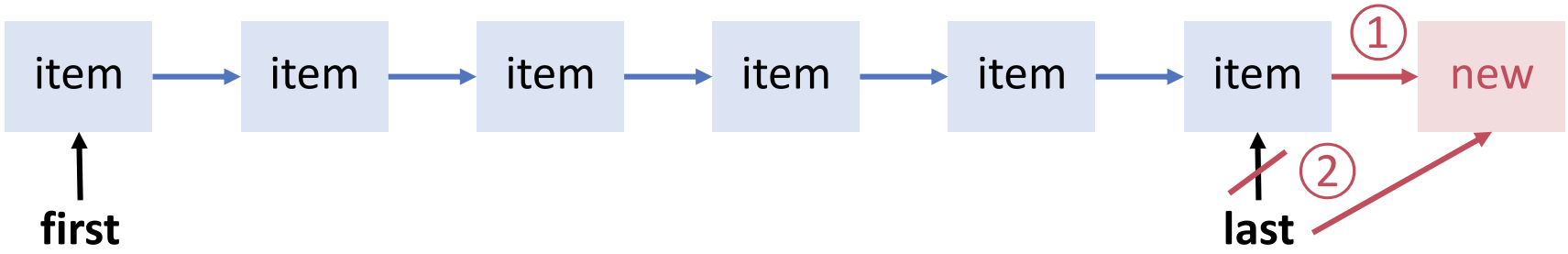

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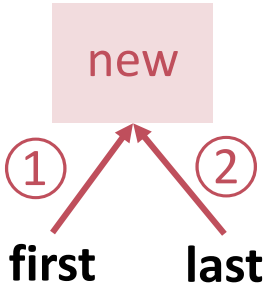

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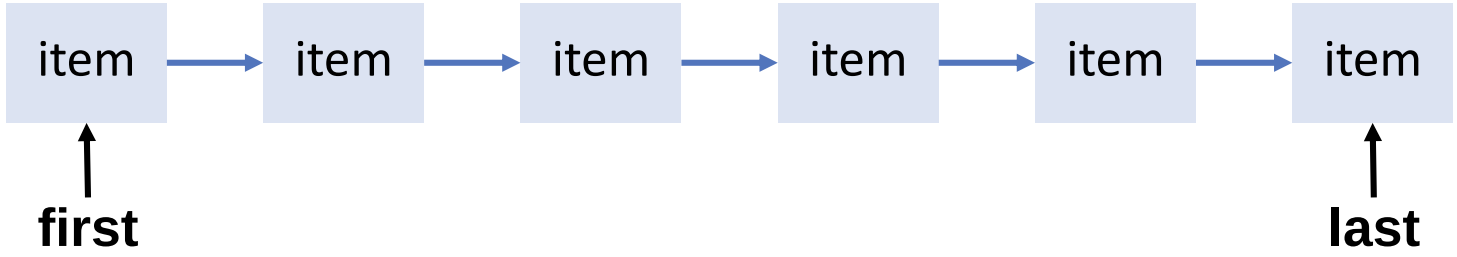

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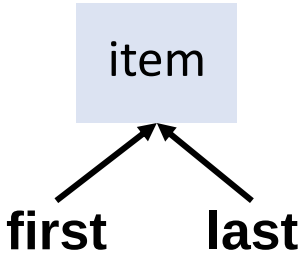

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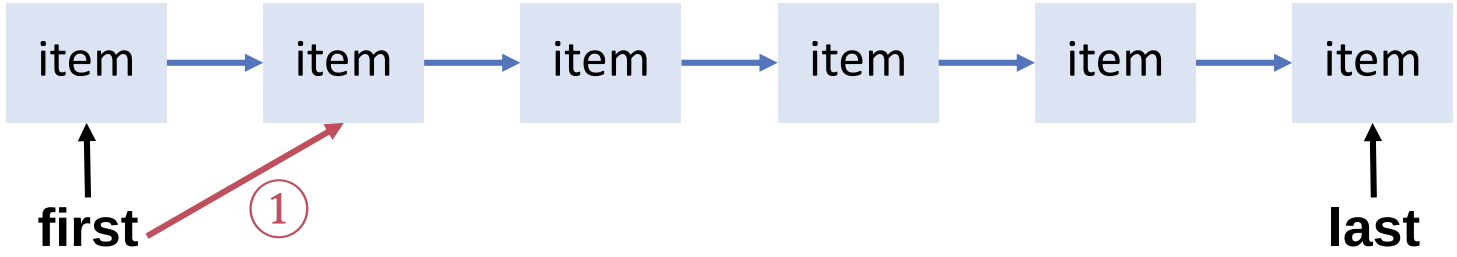

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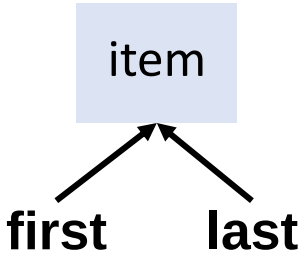

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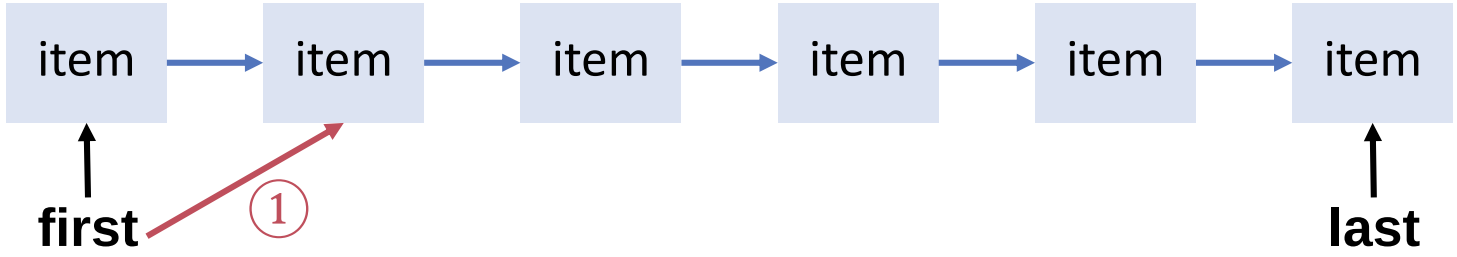

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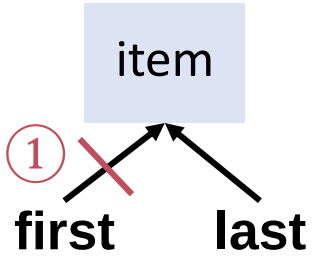

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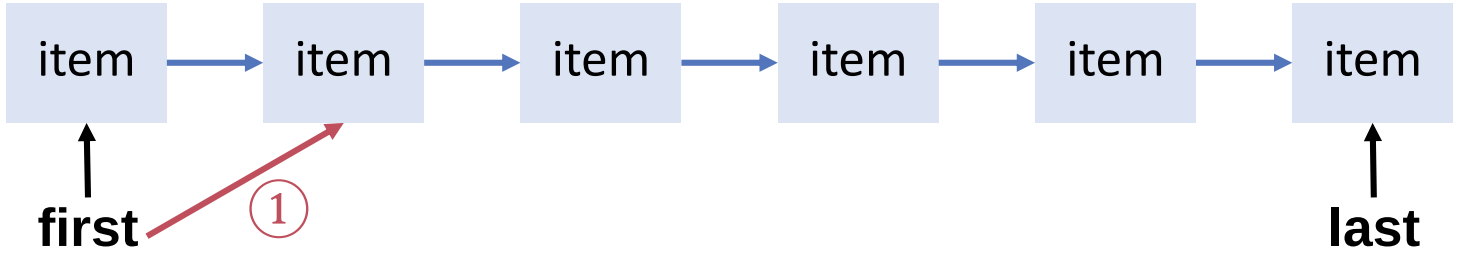

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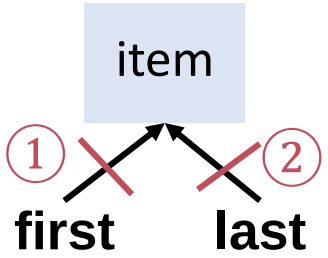

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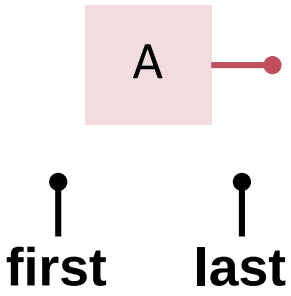

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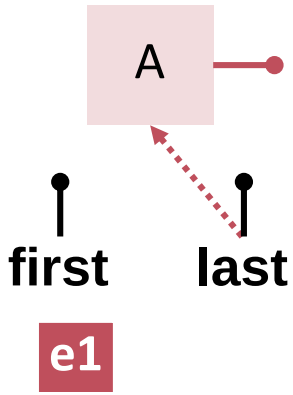

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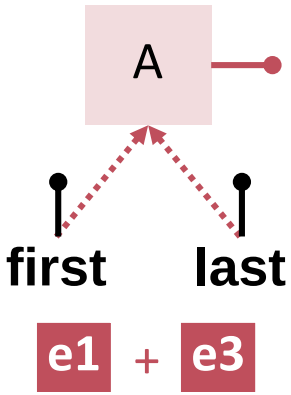

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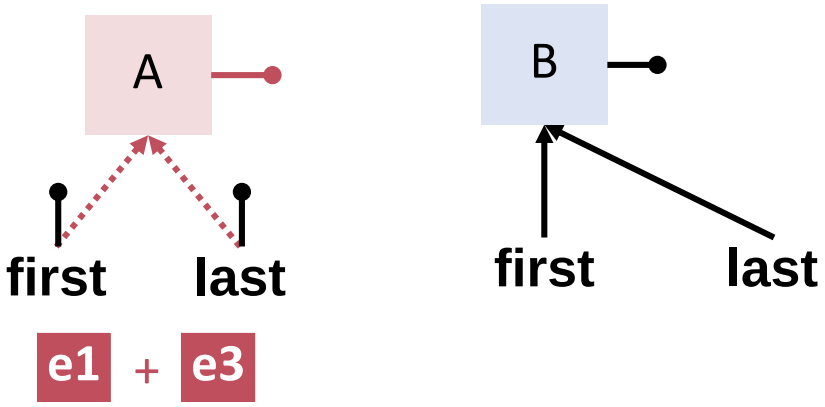

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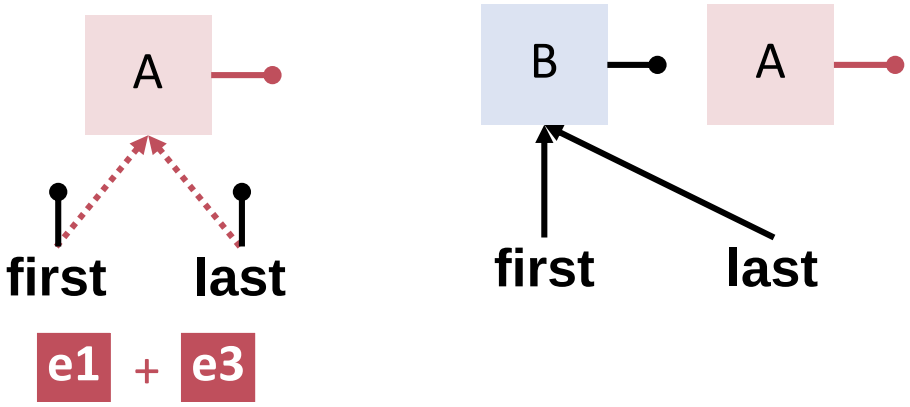

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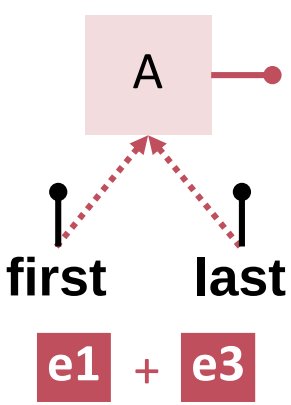

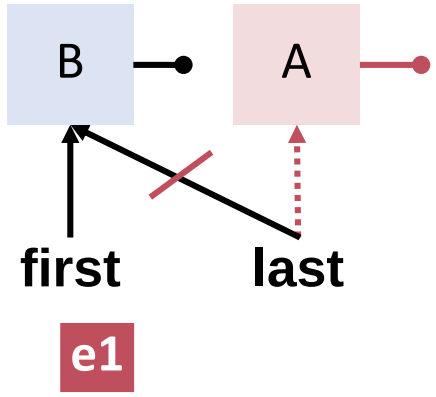

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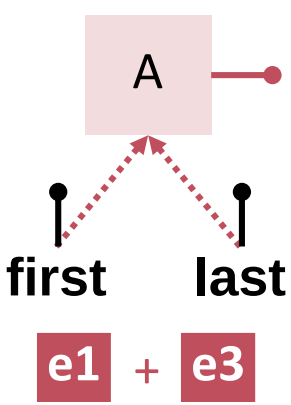

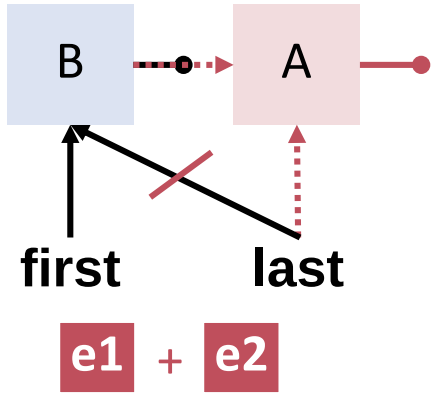

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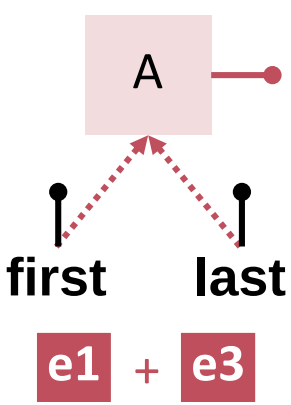

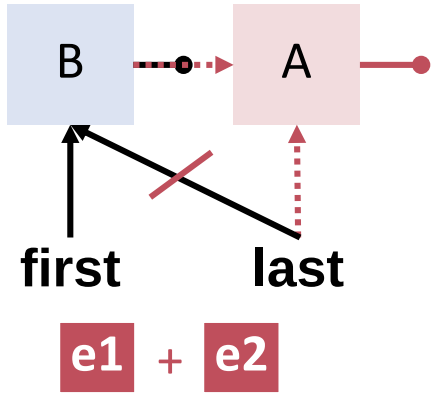

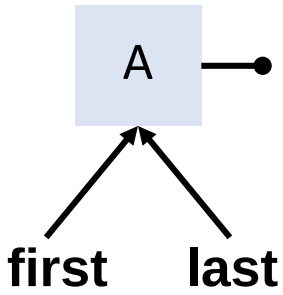

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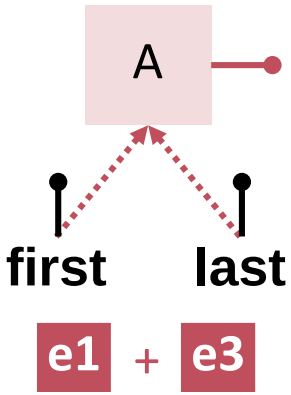

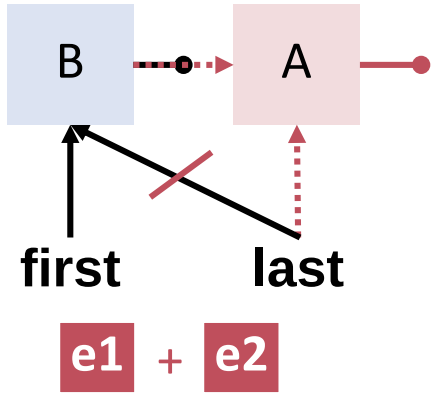

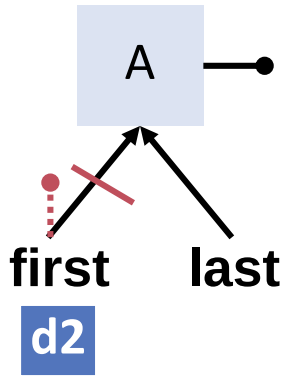

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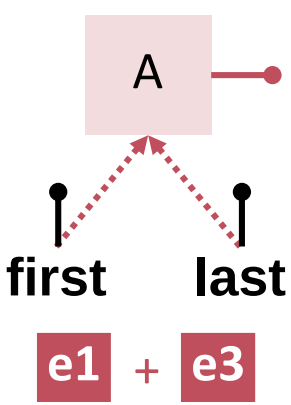

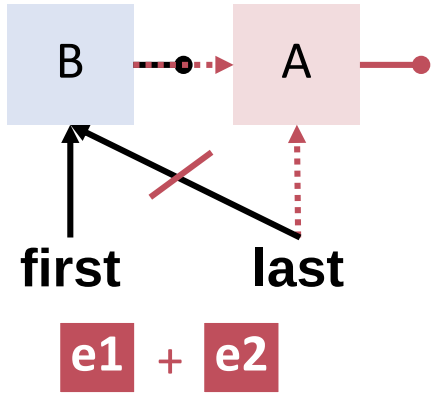

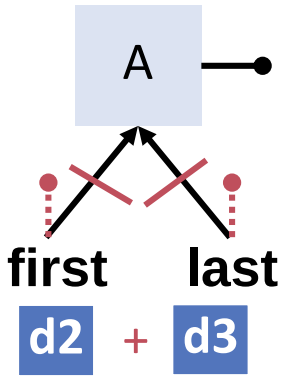

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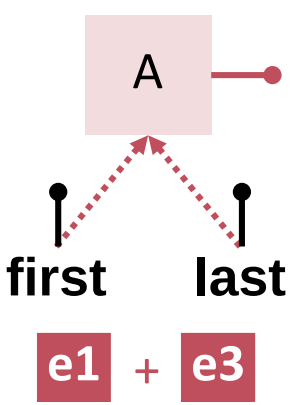

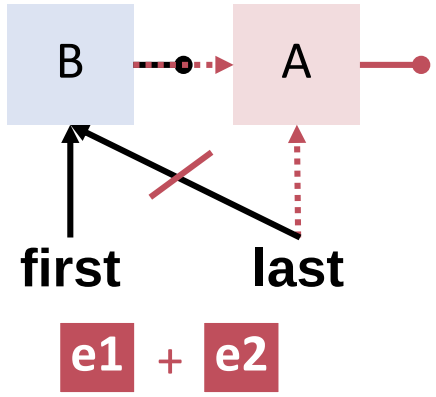

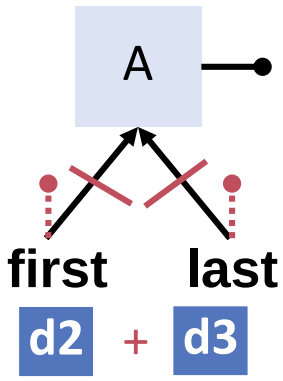

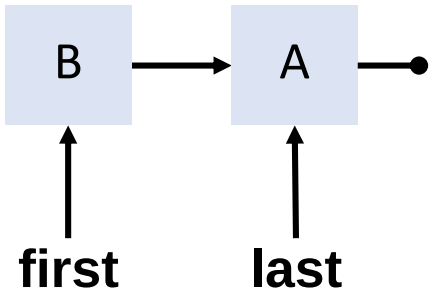

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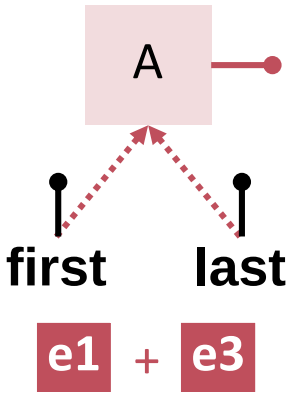

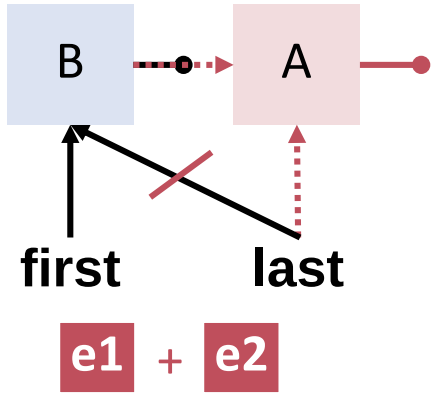

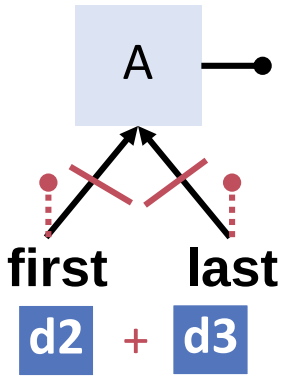

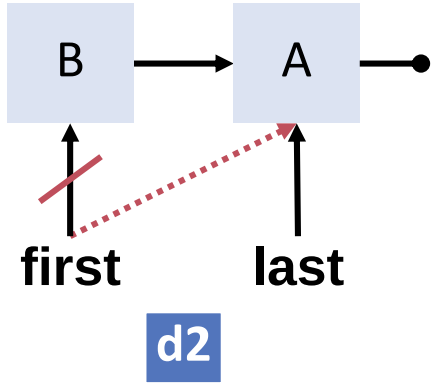

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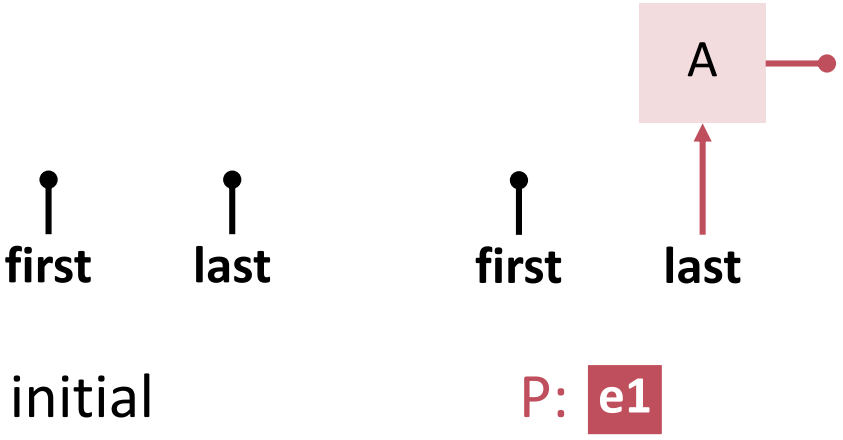

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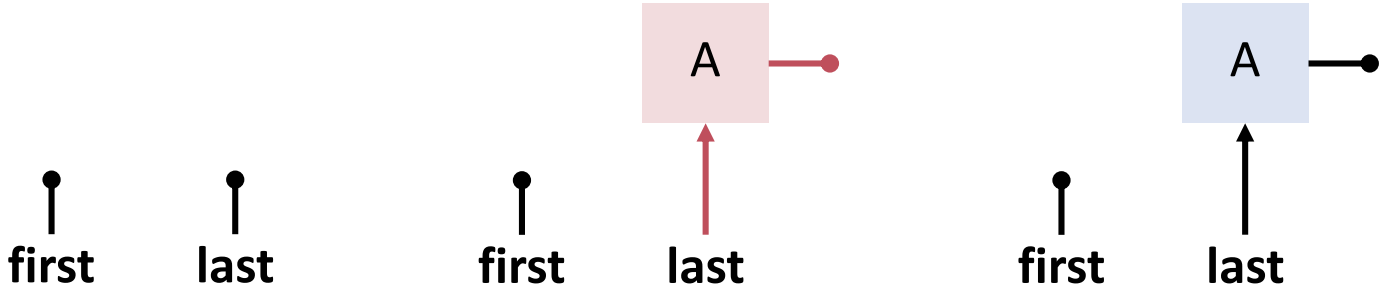

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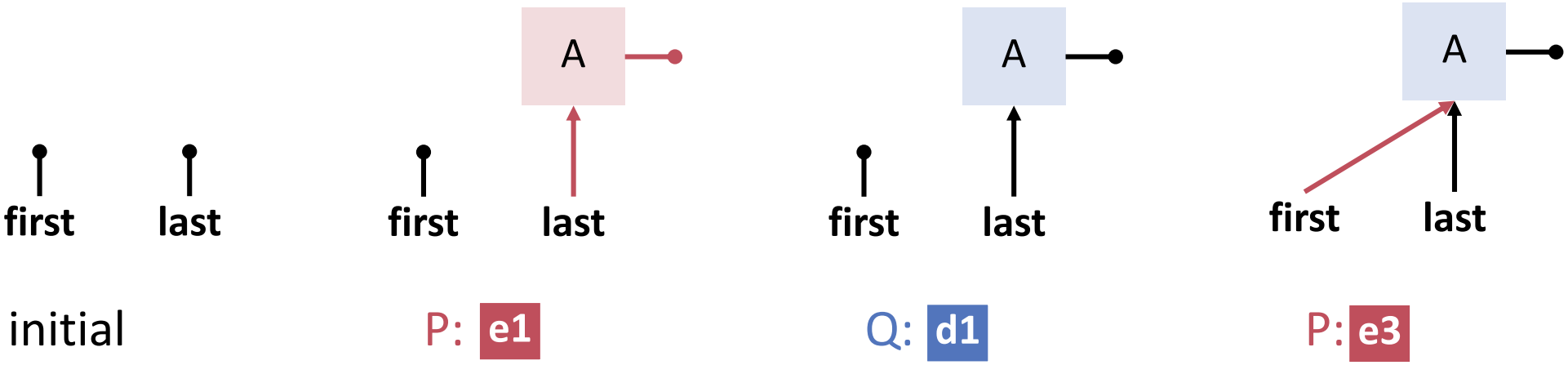

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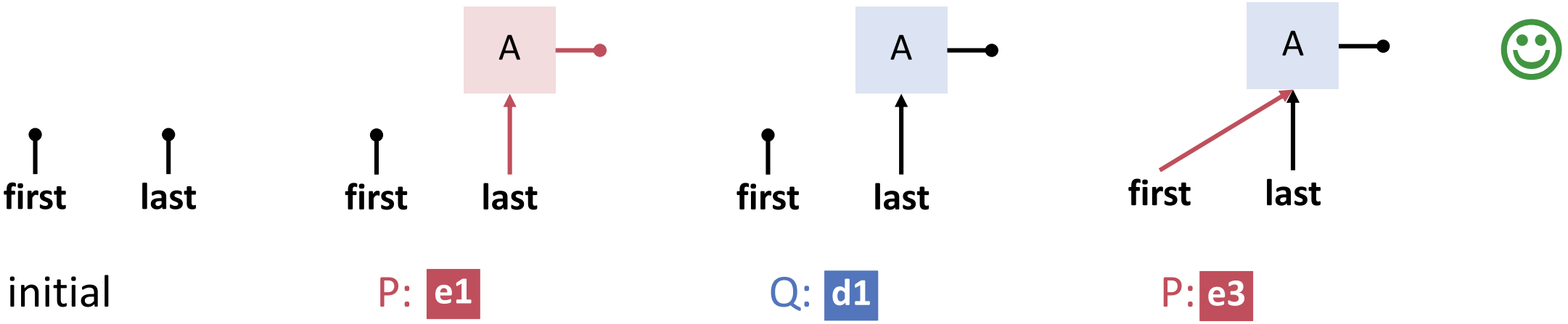

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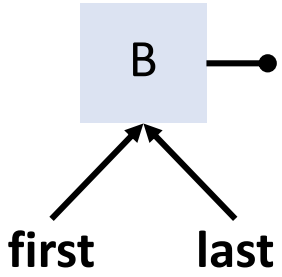

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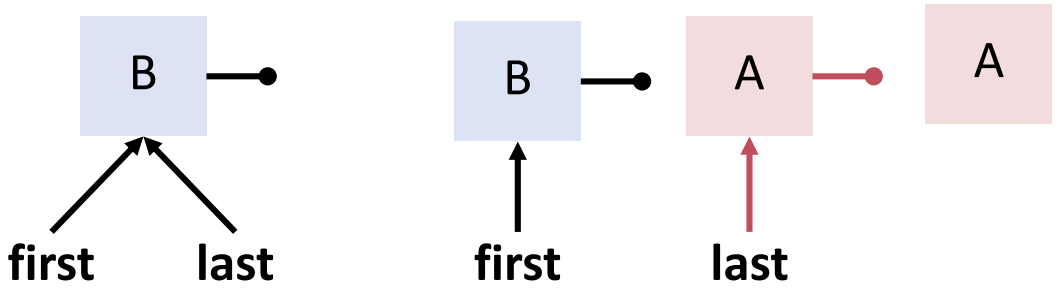

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P: e1

Scenario

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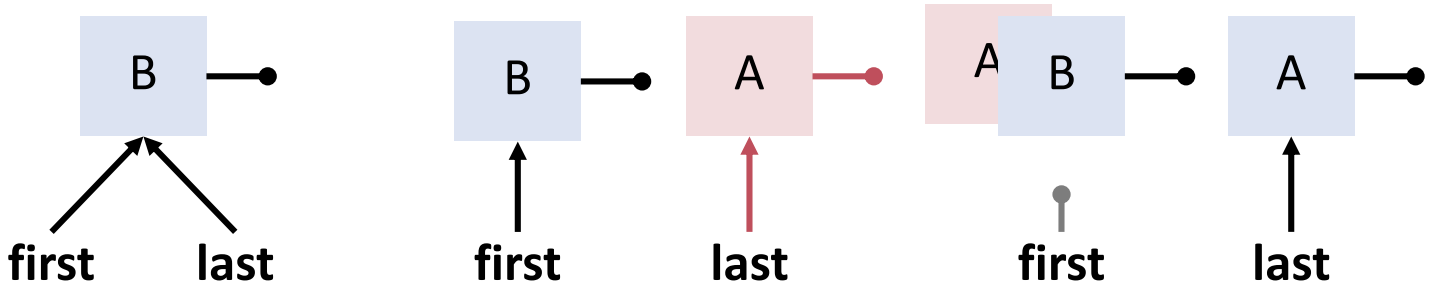

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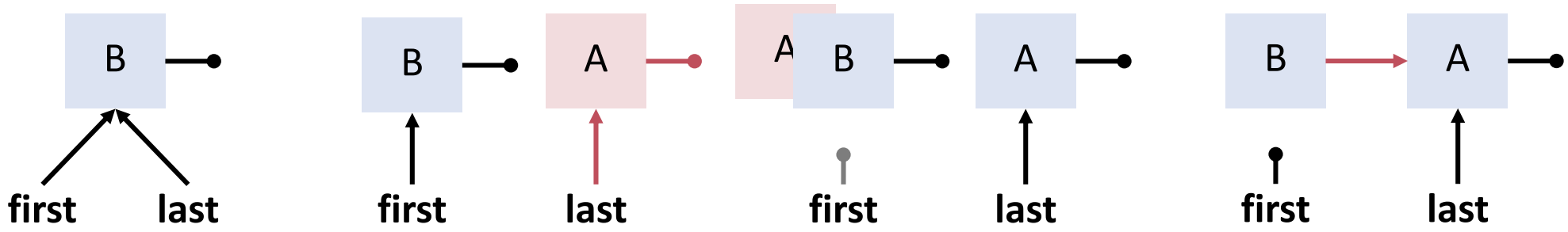

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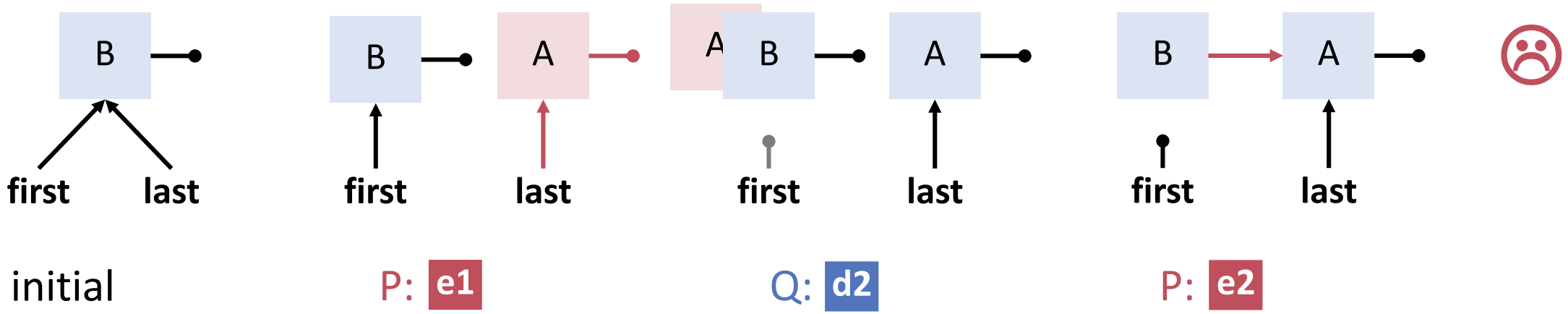

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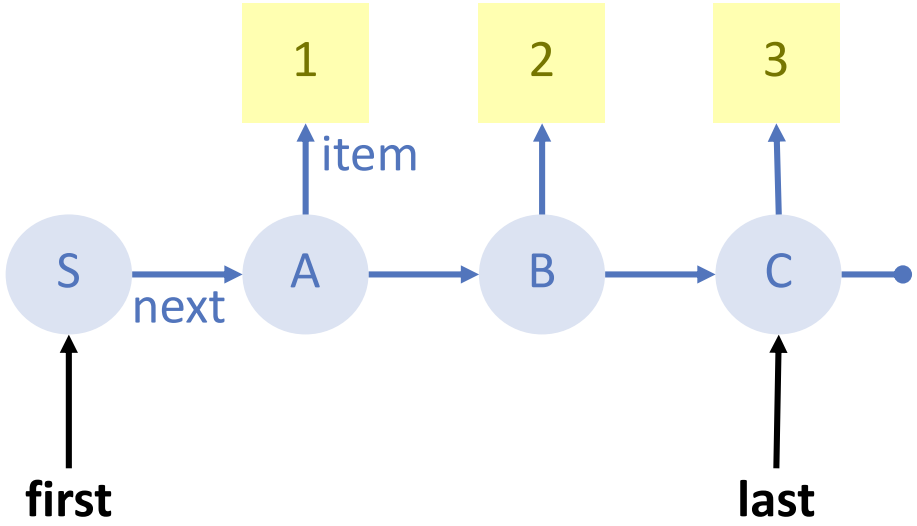
- The problem is that enqueue and dequeue do under some circumstances have to update **several pointers at once** [first, last, next]
- The transient inconsistency can lead to permanent data structure corruption
- Solutions to this particular problem are not easy to find if no double compare and swap (or similar) is available
- Need another approach: Decouple enqueue and dequeue with a sentinel. A consequence is that the **queue cannot be in-place.**

Queues with Sentinel



Queue empty:	first = last
Queue nonempty:	first # last
Invariants:	first # NIL
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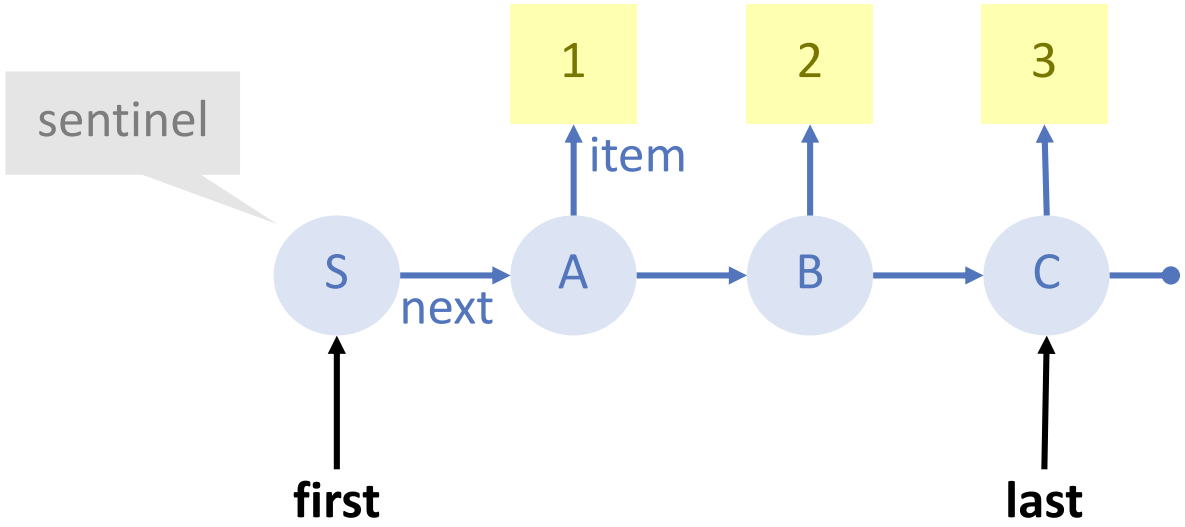

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Queue nonempty: first # last

Invariants: first # NIL

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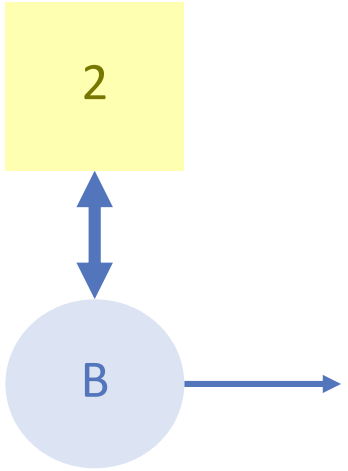
Node Reuse

simple idea:

link from node to item
and from item to node



Enqueue and Dequeue with Sentinel

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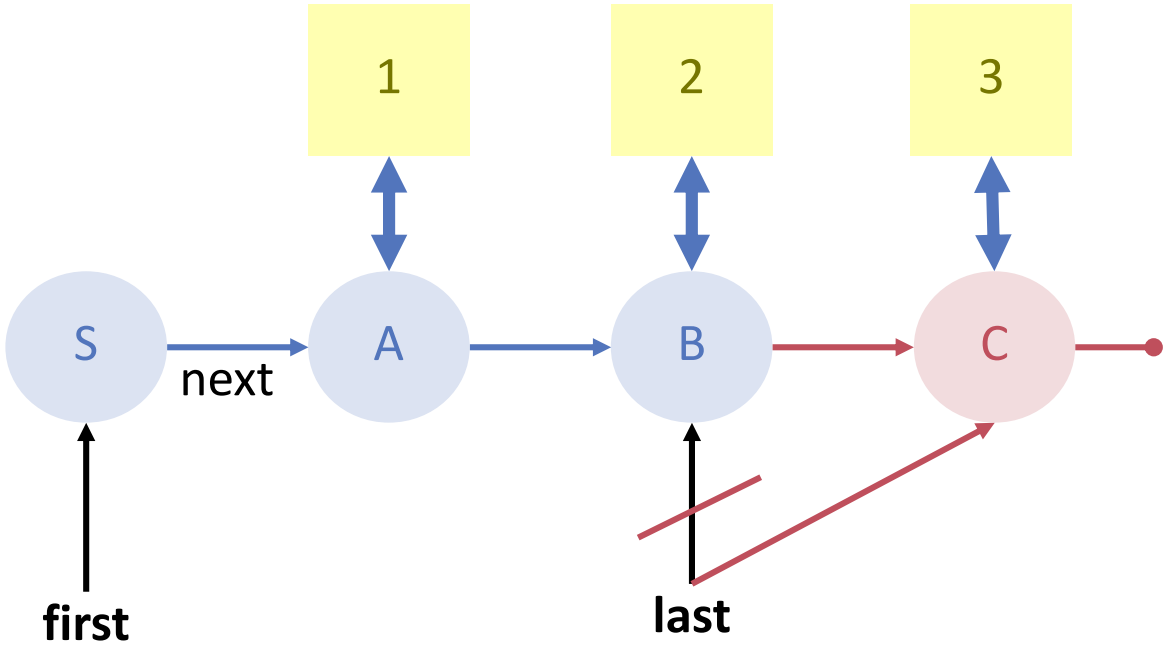

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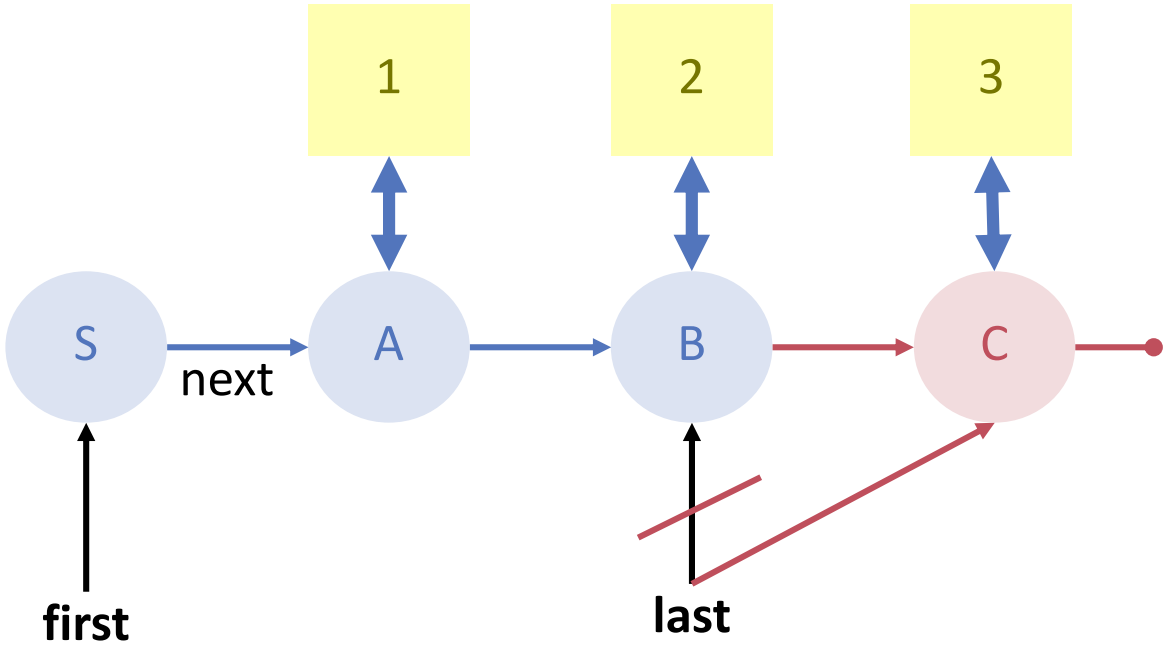
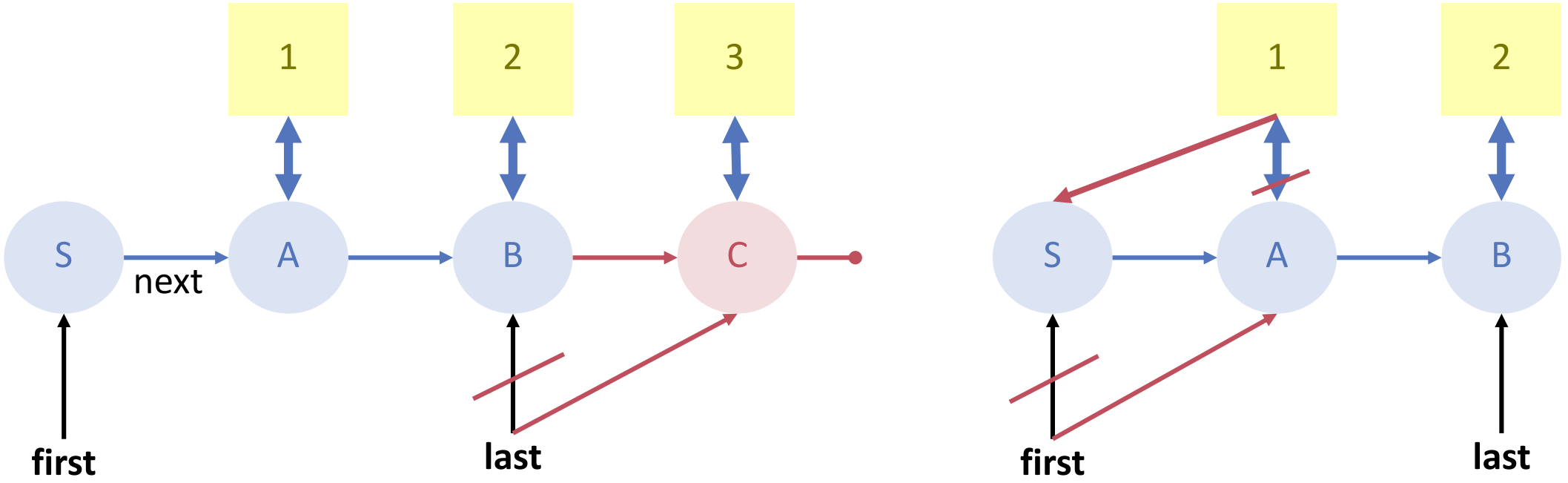


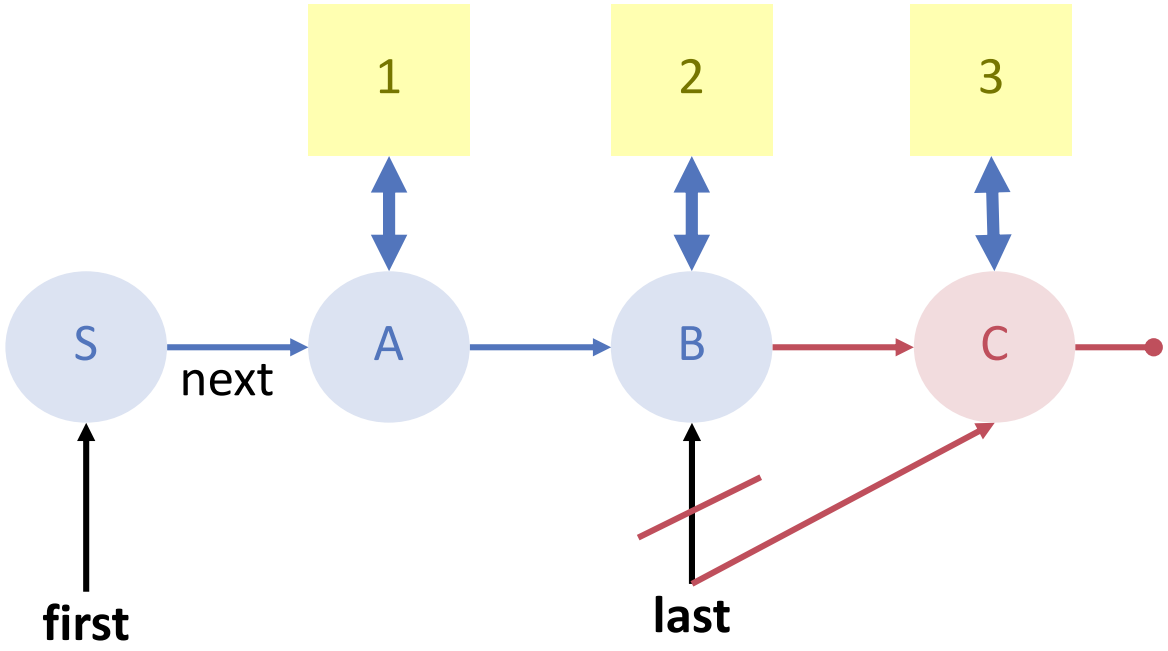
Item enqueued together with associated node.

Enqueue and Dequeue with Sentinel

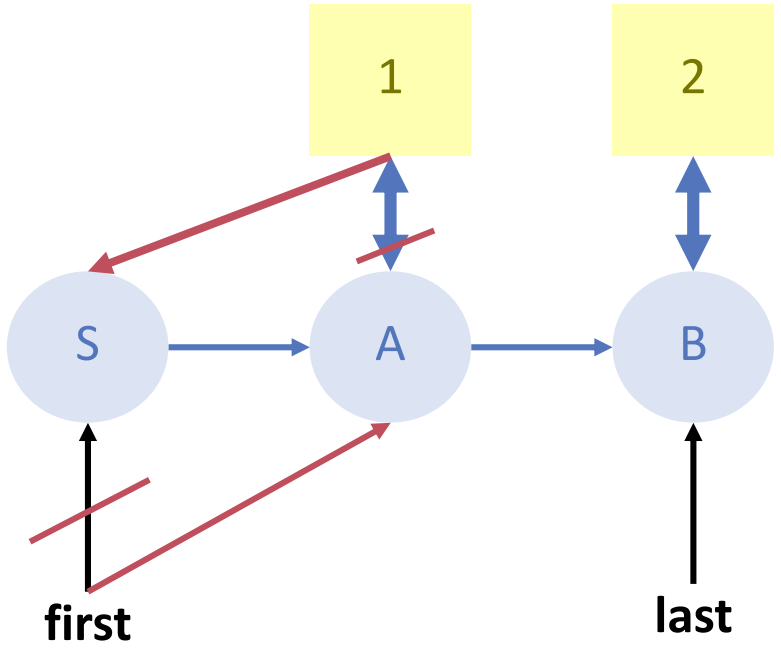


Item enqueued together with associated node.

Enqueue and Dequeue with Sentinel



Item enqueued together with associated node.



A becomes the new sentinel.
S associated with free item.

Enqueue

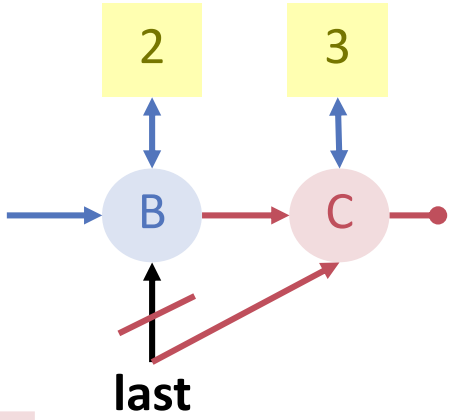
```
PROCEDURE Enqueue- (item: Item; VAR queue: Queue);
VAR node, last, next: Node;
BEGIN
   node := Allocate();
   node.item := Item:
   LOOP
      last := CAS (queue.last, NIL, NIL);
      next := CAS (last.next, NIL, node);
      IF next = NIL THEN EXIT END;
      IF CAS (queue.last, last, next) # last THEN CPU.Backoff END;
   END;
   ASSERT (CAS (queue.last, last, node) # NIL);
END Enqueue;
```

Set last node's next pointer

If setting last pointer failed, then **help other processes to update last node → Progress guarantee**

Set last node, can fail but then others have already helped

Enqueue




```
PROCEDURE Enqueue- (item: Item; VAR queue: Queue);
VAR node, last, next: Node;
BEGIN
   node := Allocate();
   node.item := Item:
   LOOP
      last := CAS (queue.last, NIL, NIL);
      next := CAS (last.next, NIL, node);
      IF next = NIL THEN EXIT END;
      IF CAS (queue.last, last, next) # last THEN CPU.Backoff END;
   END;
   ASSERT (CAS (queue.last, last, node) # NIL);
END Enqueue;
```

Set last node's next pointer

If setting last pointer failed, then **help other processes to update last node → Progress guarantee**

Set last node, can fail but then others have already helped

Dequeue

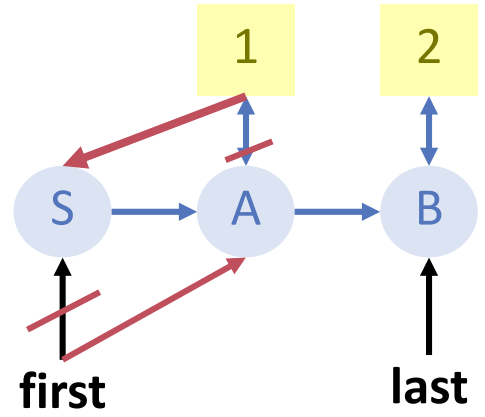
```
PROCEDURE Dequeue- (VAR item: Item; VAR queue: Queue): BOOLEAN;
VAR first, next, last: Node;
BEGIN
   LOOP
      first := CAS (queue.first, NIL, NIL);
      next := CAS (first.next, NIL, NIL);
      IF next = NIL THEN RETURN FALSE END;
      last := CAS (queue.last, first, next);
      item := next.item;
      IF CAS (queue.first, first, next) = first THEN EXIT END;
      CPU.Backoff;
   END;
   item.node := first;
   RETURN TRUE;
END Dequeue;
```

Remove potential inconsistency, **help other processes to set last pointer**

set first pointer

associate node with first

Dequeue




```
PROCEDURE Dequeue- (VAR item: Item; VAR queue: Queue): BOOLEAN;
VAR first, next, last: Node;
BEGIN
   LOOP
      first := CAS (queue.first, NIL, NIL);
      next := CAS (first.next, NIL, NIL);
      IF next = NIL THEN RETURN FALSE END;
      last := CAS (queue.last, first, next);
      item := next.item;
      IF CAS (queue.first, first, next) = first THEN EXIT END;
      CPU.Backoff;
   END;
   item.node := first;
   RETURN TRUE;
END Dequeue;
```

Remove potential inconsistency, **help other processes to set last pointer**

set first pointer

associate node with first