## 13. Arrays II

Strings, Lindenmayer Systems, Multidimensional Arrays, Vectors of Vectors, Shortest Paths, Arrays and Vectors as Function Arguments

## **Strings as Arrays**

can be represented with underlying type char

char text[] a = ...

can be initialized via string literals

char text[] = "bool"

this is equivalent to the following initialisation

char text[] = {'b', 'o', 'o', 'l', '\0'}

can only be defined with constant size

## Texts

can be represented with the type std::string from the standard library.

std::string text = "bool";

#### defines a string with length 4

- A string is conceptually an array with base type char, plus additional functionality
- Requires #include <string>

## Strings: pimped char-Arrays

- A std::string...
- knows its length

#### text.length()

returns its length as int (call of a member function; will be explained later

can be initialized with variable length

std::string text (n, 'a')

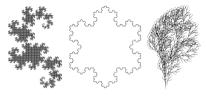
#### text is filled with n 'a's

"understands" comparisons

if (text1 == text2) ...

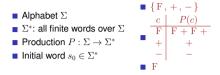
## Lindenmayer-Systems (L-Systems)

#### Fractals made from Strings and Turtles



L-Systems have been invented by the Hungarian biologist Aristid Lindenmayer (1925 – 1989) to model the growth of plants.

## Definition and Example

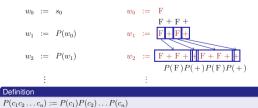


#### Definition

The triple  $\mathcal{L} = (\Sigma, P, s_0)$  is an L-System.

## The Described Language

Words  $w_0, w_1, w_2, \ldots \in \Sigma^*$ :



## **Turtle-Graphics**

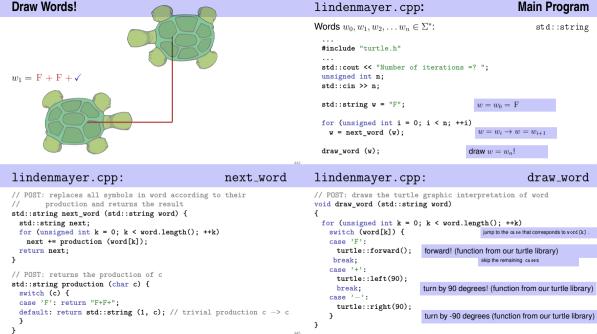
Turtle with position and direction.



#### Turtle understands 3 commands:



 $P(\mathbf{F}) = \mathbf{F} + \mathbf{F} + \mathbf{F}$ 



## L-Systems: Extensions

## L-System-Challenge:

amazing.cpp!

- Additional symbols without graphical interpretation (dragon.cpp)
- Arbitrary angles (snowflake.cpp)
- $\blacksquare$  Saving and restoring the turtle state  $\rightarrow$  plants (bush.cpp)

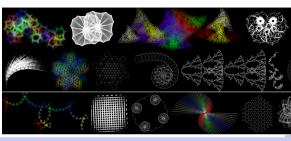


## **Multidimensional Arrays**

- are arrays of arrays
- can be used to store *tables, matrices, ....*

int a[2][3] ↑

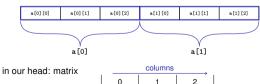
a contains two elements and each of them is an array of length 3 with base type  $\verb"int"$ 



## **Multidimensional Arrays**

rows

In memory: flat



a[0][0]

a[1][0]

a[0][1]

a[1][1]

a[0][2]

a[1][2]

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## **Multidimensional Arrays**

are arrays of arrays of arrays ....

a has *expr*<sub>1</sub> elements and each of them is an array with expr<sub>2</sub> elements each of which is an array of expr<sub>3</sub> elements and ...

## Vectors of Vectors

- How do we get multidimensional arrays with variable dimensions?
- Solution: vectors of vectors

```
Example: vector of length n of vectors with length m:
```

```
std::vector<std::vector<int> > a (n,
                   std::vector<int>(m));
```

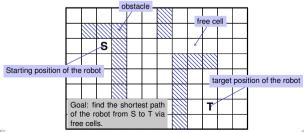
## **Multidimensional Arrays**

#### Initialization



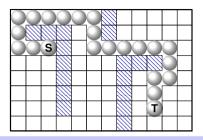
## **Application: Shortest Paths**





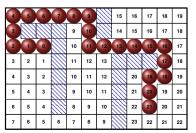
## Application: shortest paths

Solution



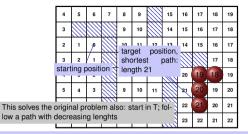
## This problem appears to be different

Find the *lengths* of the shortest paths to *all* possible targets.

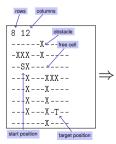


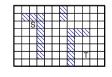
## This problem appears to be different

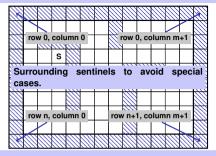
Find the *lengths* of the shortest paths to *all* possible targets.



## **Preparation: Input Format**







## The Shortest Path Program

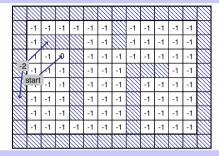
 Read in dimensions and provide a two dimensional array for the path lengths finclude<forcemark finclude<forcemark</li>

```
int main()
```

```
// read floor dimensions
int n; std::cin >> n; // number of rows
int m; std::cin >> m; // number of columns Sentinel
```

```
// define a two-dimensional
// array of dimensions
// (n+2) x (m+2) to hold the floor plus extra walls around
sdd::wector<std::wector<int>> floor (n+2, std::wector<int>(m+2));
```

#### **Preparation: Initial Marking**



## The Shortest Path Program

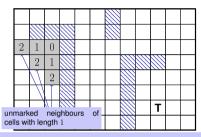
Input the assignment of the hall and intialize the lengths

```
int tr = 0;
int tc = 0;
for (int r=1; r<n+1; ++r)
for (int c=1; c<m+1; ++c) {
    char entry = '-';
    std::cin >> entry;
    if (entry == 'S') floor[r][c] = 0;
    else if (entry == 'T') floor[tr = r][tc = c] = -1;
    else if (entry == 'X') floor[r][c] = -2;
    else if (entry == '-') floor[r][c] = -1;
}
```

#### Das Kürzeste-Wege-Programm

## Mark all Cells with their Path Lengths

Step 2: all cells with path length 2



#### Add the surrounding walls

```
for (int r=0; r<n+2; ++r)
floor[r][0] = floor[r][m+1] = -2;</pre>
```

```
for (int c=0; c<m+2; ++c)
floor[0][c] = floor[n+1][c] = -2;</pre>
```

#### Main Loop

```
Find and mark all cells with path lengths i = 1, 2, 3...
for (int i=1;; ++i) {
    bool progress = false;
    for (int r=1; r<+i; ++r)
        for (int c=1; c<m+1; ++c) {
            if (floor[r][c] != -1) continue;
            if (floor[r][c] != i-1 || floor[r+1][c] == i-1 ||
            floor[r][c-1] == i-1 || floor[r][c+1] == i-1 ) {
            floor[r][c] = i; // label cell with i
            progress = true;
        }
    }
    if (!progress) break;
}</pre>
```

## The Shortest Paths Program

Mark the shortest path by walking backwards from target to start.

```
int r = tr; int c = tc;
while (floor[r][c] > 0) {
    const int d = floor[r][c] - 1;
    floor[r][c] = -3;
    if        (floor[r-1][c] == d) --r;
    else if (floor[r-1][c] == d) ++r;
    else if (floor[r][c-1] == d) --c;
    else ++c; // (floor[r][c+1] == d)
}
```

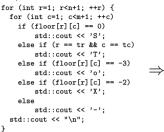
#### Finish

-3	-3	-3	-3	-3	-3		15	16	17	18	19	
-3				9	-3		14	15	16	17	18	
-3	-3	0		10	-3	-3	-3	-3	-3	-3	17	
3	2	1		11	12	13				-3	18	
4	3	2		10	11	12		20	-3	-3	19	
5	4	3		9	10	11		21	-3	19	20	
6	5	4		8	9	10		22	-3	20	21	
7	6	5	6	7	8	9		23	22	21	22	

#### The Shortest Paths Program

#### The Shortest Path Program: output

#### Output





## **Arrays as Function Arguments**

- Algorithm: Breadth First Search
- The program can become pretty slow because for each i all cells are traversed
- Improvement: for marking with i, traverse only the neighbours of the cells marked with i 1.
- Improvement: stop once the goal has been reached

Arrays can also be passed as *reference* arguments to a function. (here: const because v is read-only)

```
void print_vector(const int (&v)[3]) {
  for (int i = 0; i<3 ; ++i) {
    std::cout << v[i] << " ";
  }
}</pre>
```

## Arrays as Function Argumenbts

This also works for multidimensional arrays.

```
void print_matrix(const int (&m)[3][3]) {
  for (int i = 0; i<3 ; ++i) {
    print_vector (m[i]);
    std::cout << "\n";
  }
}</pre>
```

## **Vectors as Function Arguments**

Vectors can be passed by value or by reference

```
void print_vector(const std::vector<int>& v) {
  for (int i = 0; i<v.size() ; ++i) {
    std::cout << v[i] << " ";
  }
}</pre>
```

Here: *call by reference* is more efficient because the vector could be very long

## Vectors as Function Arguments

This also works for multidimensional vectors.

```
void print_matrix(const std::vector<std::vector<int> >& m) {
  for (int i = 0; irm.size(); ++i) {
    print_vector (m[i]);
    std::cout << "\n";
  }
}</pre>
```

# 14. Pointers, Algorithms, Iterators and Containers I

Pointers, Address operator, Dereference operator, Array-to-Pointer Conversion

## **Random Access is Useful**

Adresse von a  $[0] = a + 0 \cdot s$ 

int a[] = ...; // large array

a[13] = ...; a[77] = ...; a[50] = ...;

## **Random Access is Useful**

int a[] = ...; // large array

a[13] =;	compute $a + 13 \cdot s$
a[77] =;	compute $a + 77 \cdot s$
a[50] =;	compute $a + 50 \cdot s$

One addition and one multiplication per element access

## **Random Access is Often Unnecessary**

address of a [n-1] = a + (n-1), s

- Access pattern is called sequential access
- Should only "cost" one addition per element access

# Reading a book ... with random access sequential access

#### **Random Access**

- open book on page 1
- close book
- open book on pages 2-3
- close book
- open book on pages 4-5
- close book
- ....

#### Sequential Access

- open book on page 1
- turn the page
- …

...with

## Wanted: Pointers into Arrays

```
for (pointer p = begin of a;
     p < end of a;
     increment p memory width of int)
a[i] = ...;
```

# int

We need to be able to use memory addresses directly!

- Queries: Begin/end of a
- Comparisons: p < ...</p>
- Arithmetic: increment p

## Pointers: Where is Anakin?

```
int anakin_skywalker = 9;
int* here = &anakin_skywalker;
std::cout << here; // Address
*here = 22;
```

// anakin\_skywalker = 22

"Anakins address is 0x7fff6bdd1b54."



## **References: Where is Anakin?**

"Search for Vader, and Anakin find you will"

```
int anakin_skywalker = 9;
int& darth_vader = anakin_skywalker;
darth_vader = 22;
```

// anakin\_skywalker = 22

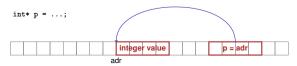


## **Pointer Types**

Value of a pointer to T is the address of an object of type T.

#### Beispiele

int\* p; Variable p is pointer to an int.
float\* q; Variable q is pointer to a float.



## **Address Operator**

## **Address Operator**

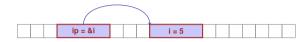


L-value of type ⊤ ↓ & /va/

Example	
<pre>int i = 5; int* ip = &amp;i</pre>	<pre>// ip initialized // with address of i.</pre>

provides, as R-value, a *pointer* of type  $T^*$  to an object at the address of *lval* 

The operator & is called Address-Operator.

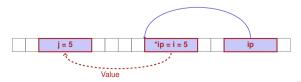




returns as L-value the *value* of the object at the address represented by *rval*.

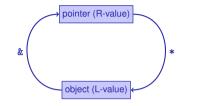
The operator \* is called Derecerence Operator.





## **Address and Dereference Operators**





Do not point with a double\* to an int!

Examples				
int* i =;	// at address i "lives" an int			
<pre>double* j = i;</pre>	//and at j lives a double: error!			

#### The declaration

T\* p; p is of the type "pointer to T"

#### can be read as

T \*p; \*p is of type T

Although this is legal, we do not write it like this!

## Pointer Arithemtics: Pointer plus int

- **p**tr: Pointer to element a[k] of the array a with length n
- Value of *expr*: integer i , such that  $0 \le k + i \le n$

#### ptr + expr

#### is a pointer to a[k+i].

For k + i = n we get a *past-the-end*-pointer that must not be dereferenced.

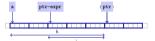
## Pointer Arithemtics: Pointer minus int

- If ptr is a pointer to the element with index k in an array a with length n
- and the value of *expr* is an integer  $i, 0 \le k i \le n$ ,

then the expression

#### ptr - expr

provides a pointer to an element of a with index k - i.



## The Truth about Random Access



a[i]

is equivalent to



## Conversion Array $\Rightarrow$ Pointer

How do we get a pointer to the first element of an array?

Static array of type T[n] is convertible to T\*



Length information is lost ("arrays are primitive")

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## Finally: Iteration over an Array of Pointers

Examp	le
-------	----

int a[5] = {3, 4, 6, 1, 2};
for (int\* p = a; p < a+5; ++p)
 std::cout << \*p << ' '; // 3 4 6 1 2</pre>

- a+5 is a pointer behind the end of the array (past-the-end) that must not be dereferenced.
- The pointer comparison (p < a+5) refers to the order of the two addresses in memory.