

3. Logical Values

Boolean Functions; the Type `bool`; logical and relational operators; shortcut evaluation

Our Goal

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
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Boolean Values in Mathematics

Boolean expressions can take on one of two values:

0 or **1**

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0 or **1**

- **0** corresponds to **“false”**
- **1** corresponds to **“true”**

The Type `bool` in C++

- represents **logical values**

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- Literals **false** and **true**

The Type `bool` in C++

- represents **logical values**
- Literals `false` and `true`
- Domain `{false, true}`

```
bool b = true; // Variable with value true
```

Relational Operators

`a < b` (smaller than)

arithmetic type \times arithmetic type \rightarrow **bool**

R-value \times R-value \rightarrow R-value

Relational Operators

`a < b` (smaller than)

```
bool b = (1 < 3); // b =
```

Relational Operators

`a < b` (smaller than)

```
bool b = (1 < 3); // b = true
```

Relational Operators

`a >= b` (greater than)

```
int a = 0;  
bool b = (a >= 3); // b =
```

Relational Operators

`a >= b` (greater than)

```
int a = 0;  
bool b = (a >= 3); // b = false
```

Relational Operators

`a == b` (equals)

```
int a = 4;  
bool b = (a % 3 == 1); // b =
```

Relational Operators

`a == b` (equals)

```
int a = 4;  
bool b = (a % 3 == 1); // b = true
```


Relational Operators

`a != b` (not equal)

```
int a = 1;  
bool b = (a != 2*a-1); // b =
```

Relational Operators

`a != b` (not equal)

```
int a = 1;  
bool b = (a != 2*a-1); // b = false
```

Boolean Functions in Mathematics

- Boolean function

$$f : \{0, 1\}^2 \rightarrow \{0, 1\}$$

- 0 corresponds to “false”.
- 1 corresponds to “true”.

- “logical And”

$$f : \{0, 1\}^2 \rightarrow \{0, 1\}$$

- 0 corresponds to “false”.
- 1 corresponds to “true”.

x	y	AND(x, y)
0	0	0
0	1	0
1	0	0
1	1	1

Logical Operator &&

`a && b` (logical and)

```
int n = -1;  
int p = 3;  
bool b = (n < 0) && (0 < p); //
```

Logical Operator &&

`a && b` (logical and)

```
int n = -1;  
int p = 3;  
bool b = (n < 0) && (0 < p); // b = true
```

- “logical Or”

$$f : \{0, 1\}^2 \rightarrow \{0, 1\}$$

- 0 corresponds to “false”.
- 1 corresponds to “true”.

x	y	$\text{OR}(x, y)$
0	0	0
0	1	1
1	0	1
1	1	1

Logical Operator ||

`a || b` (logical or)

```
int n = 1;
int p = 0;
bool b = (n < 0) || (0 < p); //
```


Logical Operator ||

`a || b` (logical or)

```
int n = 1;  
int p = 0;  
bool b = (n < 0) || (0 < p); // b = false
```

- “logical Not”

$$f : \{0, 1\} \rightarrow \{0, 1\}$$

- 0 corresponds to “false”.
- 1 corresponds to “true”.

x	NOT(x)
0	1
1	0

Logical Operator !

!b (logical not)

bool → **bool**

R-value → R-value

Logical Operator !

!b (logical not)

```
int n = 1;  
bool b = !(n < 0); //
```

Logical Operator !

!b (logical not)

```
int n = 1;  
bool b = !(n < 0); // b = true
```

Precedences

`!b && a`

Precedences

`!b && a`
⇕
`(!b) && a`

Precedences

a && b || c && d

Precedences

a && b || c && d
⇕
(a && b) || (c && d)

Precedences

`a || b && c || d`

Precedences

a || b && c || d
⇕
a || (b && c) || d

Precedences

```
7 + x < y && y != 3 * z || ! b
```

Precedences

The unary logical operator !
binds more strongly than

```
7 + x < y && y != 3 * z || (!b)
```

Precedences

The unary logical operator !
binds more strongly than
binary arithmetic operators. These
bind more strongly than

```
(7 + x) < y && y != (3 * z) || (!b)
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Precedences

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relational operators,
and these bind more strongly than

```
((7 + x) < y) && (y != (3 * z)) || (!b)
```

Precedences

The unary logical operator !
binds more strongly than
binary arithmetic operators. These
bind more strongly than
relational operators,
and these bind more strongly than
binary logical operators.

```
((7 + x) < y) && (y != (3 * z)) || (!b)
```

Some parentheses on the previous slides were actually redundant.

Completeness

- AND, OR and NOT are the boolean functions available in C++.

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- Any other *binary* boolean function can be generated from them.

x	y	$\text{XOR}(x, y)$
0	0	0
0	1	1
1	0	1
1	1	0

$$\text{XOR}(x, y) = \text{AND}(\text{OR}(x, y), \text{NOT}(\text{AND}(x, y))).$$

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$$x \oplus y = (x \vee y) \wedge \neg(x \wedge y).$$

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$$x \oplus y = (x \vee y) \wedge \neg(x \wedge y).$$

$$(x \ || \ y) \ \&\& \ !(x \ \&\& \ y)$$

Completeness Proof

- Identify binary boolean functions with their characteristic vector.

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characteristic vector: 0110

Completeness Proof

- Identify binary boolean functions with their characteristic vector.

x	y	XOR(x, y)
0	0	0
0	1	1
1	0	1
1	1	0

characteristic vector: 0110

$$\text{XOR} = f_{0110}$$

Completeness Proof

- Step 1: generate the *fundamental* functions f_{0001} , f_{0010} , f_{0100} , f_{1000}

$$f_{0001} = \text{AND}(x, y)$$

$$f_{0010} = \text{AND}(x, \text{NOT}(y))$$

$$f_{0100} = \text{AND}(y, \text{NOT}(x))$$

$$f_{1000} = \text{NOT}(\text{OR}(x, y))$$

Completeness Proof

- Step 2: generate all functions by applying logical or

$$f_{1101} = \text{OR}(f_{1000}, \text{OR}(f_{0100}, f_{0001}))$$

Completeness Proof

- Step 2: generate all functions by applying logical or

$$f_{1101} = \text{OR}(f_{1000}, \text{OR}(f_{0100}, f_{0001}))$$

- Step 3: generate f_{0000}

$$f_{0000} = 0.$$

bool vs int: Conversion

- `bool` can be used whenever `int` is expected

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<code>bool</code>	→	<code>int</code>
<i>true</i>	→	1
<i>false</i>	→	0

bool vs int: Conversion

- **bool** can be used whenever **int** is expected – and vice versa.

bool	→	int
<i>true</i>	→	1
<i>false</i>	→	0
int	→	bool
$\neq 0$	→	<i>true</i>
0	→	<i>false</i>

bool vs int: Conversion

- **bool** can be used whenever **int** is expected – and vice versa.

bool	→	int
<i>true</i>	→	1
<i>false</i>	→	0
int	→	bool
$\neq 0$	→	<i>true</i>
0	→	<i>false</i>

```
bool b = 3; // b=true
```


bool vs int: Conversion

- `bool` can be used whenever `int` is expected – and vice versa.
- Many existing programs use `int` instead of `bool`

This is bad style originating from the language C.

<code>bool</code>	→	<code>int</code>
<i>true</i>	→	1
<i>false</i>	→	0
<code>int</code>	→	<code>bool</code>
<code>≠0</code>	→	<i>true</i>
0	→	<i>false</i>

```
bool b = 3; // b=true
```

DeMorgan Rules

■ `!(a && b) == (!a || !b)`

DeMorgan Rules

■ $!(a \ \&\& \ b) == (!a \ || \ !b)$

$!(\text{rich } \textit{and} \ \text{beautiful}) == (\text{poor } \textit{or} \ \text{ugly})$

DeMorgan Rules

- $!(a \ \&\& \ b) == (!a \ || \ !b)$
- $!(a \ || \ b) == (!a \ \&\& \ !b)$

$!(\text{rich } \textit{and} \ \text{beautiful}) == (\text{poor } \textit{or} \ \text{ugly})$

Application: either ... or (XOR)

`(x || y) && !(x && y)`

Application: either ... or (XOR)

`(x || y) && !(x && y)` `x or y, and not both`

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`(x || y) && !(x && y)` x or y, and not both

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`!(!x && !y) && !(x && y)`

Application: either ... or (XOR)

`(x || y) && !(x && y)` x or y, and not both

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`!(!x && !y) && !(x && y)` not none and not both

Application: either ... or (XOR)

`(x || y) && !(x && y)` x or y, and not both

`(x || y) && (!x || !y)` x or y, and one of them not

`!(!x && !y) && !(x && y)` not none and not both

`!(!x && !y || x && y)`

Application: either ... or (XOR)

$(x \ || \ y) \ \&\& \ !(x \ \&\& \ y)$ x or y , and not both

$(x \ || \ y) \ \&\& \ (!x \ || \ !y)$ x or y , and one of them not

$!(\!x \ \&\& \ !y) \ \&\& \ !(x \ \&\& \ y)$ not none and not both

$!(\!x \ \&\& \ !y \ || \ x \ \&\& \ y)$ not: both or none

Short circuit Evaluation

- Logical operators `&&` and `||` evaluate the *left operand first*.
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```
x != 0 && z / x > y
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Short circuit Evaluation

- Logical operators `&&` and `||` evaluate the *left operand first*.
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x has value 0 \Rightarrow

```
false && z / x > y
```

Short circuit Evaluation

- Logical operators `&&` and `||` evaluate the *left operand first*.
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x has value 0 ⇒

false

Short circuit Evaluation

- Logical operators `&&` and `||` evaluate the *left operand first*.
- If the result is then known, the right operand will *not be* evaluated.

x has value 0 \Rightarrow

```
x != 0 && z / x > y
```

\Rightarrow No division by 0

4. Defensive Programming

Constants and Assertions

Sources of Errors

- Errors that the compiler can find:
syntactical and some semantical errors

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- Errors that the compiler can find:
syntactical and some semantical errors
- Errors that the compiler cannot find:
runtime errors (always semantical)

The Compiler as Your Friend: Constants

Constants

- are variables with immutable value

```
const int speed_of_light = 299792458;
```

- Usage: `const` before the definition

The Compiler as Your Friend: Constants

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The Compiler as Your Friend: Constants

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- Usage: **const** before the definition

The Compiler as Your Friend: Constants

- Compiler checks that the **const**-promise is kept

```
const int speed_of_light = 299792458;  
...  
speed_of_light = 300000000;
```

compiler: error



- Tool to avoid errors: constants guarantee the promise :*“value does not change”*

The Compiler as Your Friend: Constants

- Compiler checks that the **const**-promise is kept

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The Compiler as Your Friend: Constants

- Compiler checks that the `const`-promise is kept

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const int speed_of_light = 299792458;  
...  
speed_of_light = 300000000;
```

compiler: error



- Tool to avoid errors: constants guarantee the promise :*“value does not change”*

Constants: Variables behind Glass



The `const`-guideline

const-guideline

For *each variable*, think about whether it will change its value in the lifetime of a program. If not, use the keyword **`const`** in order to make the variable a constant.

A program that adheres to this guideline is called **`const`**-correct.

Avoid Sources of Bugs

1. Exact knowledge of the wanted program behavior

Avoid Sources of Bugs

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» It's not a bug, it's a feature! «

Avoid Sources of Bugs

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2. Check at many places in the code if the program is still on track

Avoid Sources of Bugs

1. Exact knowledge of the wanted program behavior
2. Check at many places in the code if the program is still on track
3. Question the (seemingly) obvious, there could be a typo in the code

Against Runtime Errors: *Assertions*

`assert(expr)`

- halts the program if the boolean expression **expr** is false

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- halts the program if the boolean expression `expr` is false
- requires `#include <cassert>`

Against Runtime Errors: *Assertions*

`assert(expr)`

- halts the program if the boolean expression `expr` is false
- requires `#include <cassert>`
- can be switched off (potential performance gain)

Assertions for the $\text{gcd}(x, y)$

Check if the program is on track ...

```
// Input x and y
std::cout << "x =? ";
std::cin >> x;
std::cout << "y =? ";
std::cin >> y;
```

Input arguments for calculation

```
// Check validity of inputs
assert(x > 0 && y > 0);
```

```
... // Compute gcd(x,y), store result in variable a
```

Assertions for the $\text{gcd}(x, y)$

Check if the program is on track ...

```
// Input x and y
std::cout << "x =? ";
std::cin >> x;
std::cout << "y =? ";
std::cin >> y;

// Check validity of inputs
assert(x > 0 && y > 0); ← Precondition for the ongoing computation

... // Compute gcd(x,y), store result in variable a
```


Assertions for the $\text{gcd}(x, y)$

... and question the obvious! ...

...

```
assert(x > 0 && y > 0);
```

← Precondition for the ongoing computation

```
... // Compute gcd(x,y), store result in variable a
```

```
assert (a >= 1);
```

```
assert (x % a == 0 && y % a == 0);
```

```
for (int i = a+1; i <= x && i <= y; ++i)
```

```
    assert(!(x % i == 0 && y % i == 0));
```

Assertions for the $\text{gcd}(x, y)$

... and question the obvious! ...

...

```
assert(x > 0 && y > 0);
```

```
... // Compute gcd(x,y), store result in variable a
```

```
assert (a >= 1);
```

```
assert (x % a == 0 && y % a == 0);
```

```
for (int i = a+1; i <= x && i <= y; ++i)
```

```
    assert(!(x % i == 0 && y % i == 0));
```

Properties of the
gcd

Switch off Assertions

```
#define NDEBUG // To ignore assertions  
#include<cassert>
```

```
...
```

```
assert(x > 0 && y > 0); // Ignored
```

```
... // Compute gcd(x,y), store result in variable a
```

```
assert(a >= 1); // Ignored
```

```
...
```

Fail-Fast with Assertions

- Real software: many C++ files, complex control flow



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Fail-Fast with Assertions

- Real software: many C++ files, complex control flow
- Errors surface late(r) → impedes error localisation



Fail-Fast with Assertions

- Real software: many C++ files, complex control flow
- Errors surface late(r) → impedes error localisation
- Assertions: Detect errors early

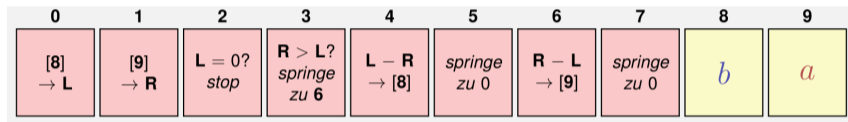


5. Control Structures I

Selection Statements, Iteration Statements, Termination, Blocks

Control Flow

- Up to now: *linear* (from top to bottom)
- Interesting programs require “branches” and “jumps”



Selection Statements

implement branches

- **if** statement
- **if-else** statement

if-Statement

```
if ( condition )  
    statement
```

if-Statement

```
if ( condition )  
    statement
```

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";
```

if-Statement

```
if ( condition )  
    statement
```

If *condition* is true then *statement* is executed

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";
```

if-Statement

```
if ( condition )  
    statement
```

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";
```

If *condition* is true then *statement* is executed

- *statement*: arbitrary statement (*body* of the **if**-Statement)
- *condition*: convertible to **bool**

if-else-statement

```
if ( condition )  
    statement1  
else  
    statement2
```

if-else-statement

```
if ( condition )  
    statement1  
else  
    statement2
```

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```


if-else-statement

```
if ( condition )  
    statement1  
else  
    statement2
```

If *condition* is true then *statement1* is executed, otherwise *statement2* is executed.

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```

if-else-statement

```
if ( condition )  
    statement1  
else  
    statement2
```

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```

If *condition* is true then *statement1* is executed, otherwise *statement2* is executed.

- *condition*: convertible to **bool**.
- *statement1*: body of the **if**-branch
- *statement2*: body of the **else**-branch

Layout!

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```

Layout!

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```

Indentation

Indentation

Iteration Statements

implement loops

- **for**-statement
- **while**-statement
- **do**-statement

Compute $1 + 2 + \dots + n$

```
// input
std::cout << "Compute the sum 1+...+n for n=?";
unsigned int n;
std::cin >> n;

// computation of sum_{i=1}^n i
unsigned int s = 0;
for (unsigned int i = 1; i <= n; ++i)
    s += i;

// output
std::cout << "1+...+" << n << " = " << s << ".\n";
```

Compute $1 + 2 + \dots + n$

```
// input
std::cout << "Compute the sum 1+...+n for n=?";
unsigned int n;
std::cin >> n;

// computation of sum_{i=1}^n i
unsigned int s = 0;
for (unsigned int i = 1; i <= n; ++i)
    s += i;

// output
std::cout << "1+...+" << n << " = " << s << ".\n";
```

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

i

s

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

<i>i</i>	<i>s</i>
<hr/>	
<i>i==1</i>	

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

i	s
$i==1$	$i \leq 2?$

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

i		s
$i==1$	wahr	

for-Statement Example

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Assumptions: $n == 2, s == 0$

i		s
$i==1$	wahr	$s == 1$

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

i		s
$i==1$	wahr	$s == 1$
$i==2$		

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

i		s
i==1	wahr	s == 1
i==2	i <= 2?	

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

<i>i</i>		<i>s</i>
<i>i</i> ==1	wahr	<i>s</i> == 1
<i>i</i> ==2	wahr	

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

i		s
i==1	wahr	s == 1
i==2	wahr	s == 3

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

i		s
i==1	wahr	s == 1
i==2	wahr	s == 3
i==3		

for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: $n == 2, s == 0$

<i>i</i>		<i>s</i>
<i>i</i> ==1	wahr	<i>s</i> == 1
<i>i</i> ==2	wahr	<i>s</i> == 3
<i>i</i> ==3	<i>i</i> <= 2?	

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for-Statement: Syntax

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for (init statement; condition; expression)  
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- *condition*: convertible to **bool**
- *expression*: any expression
- *body statement*: any statement (*body* of the for-statement)

for-Statement: Termination

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for (unsigned int i = 1; i <= n; ++i)
    s += i;
```

Here and in most cases:

- *expression* changes its value that appears in *condition* .

for-Statement: Termination

```
for (unsigned int i = 1; i <= n; ++i)
    s += i;
```

Here and in most cases:

- After a finite number of iterations *condition* becomes false: **Termination**

Infinite Loops

- Infinite loops are easy to generate:

```
for ( ; ; ) ;
```

- Die *empty condition* is true.
- Die *empty expression* has no effect.
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- ... but can in general not be automatically detected.

```
for (init; cond; expr) stmt;
```

Halting Problem

Undecidability of the Halting Problem

There is no C++ program that can determine for each C++-Program P and each input I if the program P terminates with the input I .

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Halting Problem

Undecidability of the Halting Problem

There is no C++ program that can determine for each C++-Program P and each input I if the program P terminates with the input I .

This means that the correctness of programs can in general *not* be automatically checked.³

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Example: Prime Number Test

Def.: a natural number $n \geq 2$ is a prime number, if no $d \in \{2, \dots, n - 1\}$ divides n .

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A loop that can test this:

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unsigned int d;  
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```

(body is the null statement)

Example: Termination

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- Progress: Initial value **d=2**, then plus 1 in every iteration (**++d**)
- Exit: **n%d != 0** evaluates to **false** as soon as a divisor is found — at the latest, once **d == n**
- Progress guarantees that the exit condition will be reached

Example: Correctness

```
unsigned int d;  
for (d=2; n%d != 0; ++d); // for n >= 2
```

Every potential divisor $2 \leq d \leq n$ will be tested. If the loop terminates with $d == n$ then and only then is n prime.

Blocks

- Blocks group a number of statements to a new statement

```
{statement1 statement2 ... statementN}
```

Blocks

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- Example: body of the main function

```
int main() {  
    ...  
}
```


Blocks

- Blocks group a number of statements to a new statement
- Example: loop body

```
for (unsigned int i = 1; i <= n; ++i) {  
    s += i;  
    std::cout << "partial sum is " << s << "\n";  
}
```

Blocks

- Blocks group a number of statements to a new statement
- Beispiel: if / else

```
if (d < n) // d is a divisor of n in {2,...,n-1}
    std::cout << n << " = " << d << " * " << n / d << ".\n";
else {
    assert (d == n);
    std::cout << n << " is prime.\n";
}
```