

## 3. Logical Values

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Boolean Functions; the Type `bool`; logical and relational operators; shortcut evaluation

# Our Goal

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
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    std::cout << "odd";
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# Boolean Values in Mathematics

Boolean expressions can take on one of two values:

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- **1** corresponds to **“true”**

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# The Type `bool` in C++

- represents **logical values**
- Literals `false` and `true`
- Domain `{false, true}`

```
bool b = true; // Variable with value true
```

# Relational Operators

`a < b` (smaller than)

arithmetic type  $\times$  arithmetic type  $\rightarrow$  **bool**

R-value  $\times$  R-value  $\rightarrow$  R-value

# Relational Operators

`a < b` (smaller than)

```
bool b = (1 < 3); // b =
```

# Relational Operators

`a < b` (smaller than)

```
bool b = (1 < 3); // b = true
```

# Relational Operators

`a >= b` (greater than)

```
int a = 0;  
bool b = (a >= 3); // b =
```

# Relational Operators

`a >= b` (greater than)

```
int a = 0;  
bool b = (a >= 3); // b = false
```

# Relational Operators

`a == b` (equals)

```
int a = 4;  
bool b = (a % 3 == 1); // b =
```

# Relational Operators

`a == b` (equals)

```
int a = 4;  
bool b = (a % 3 == 1); // b = true
```



# Relational Operators

`a != b` (not equal)

```
int a = 1;  
bool b = (a != 2*a-1); // b =
```

# Relational Operators

`a != b` (not equal)

```
int a = 1;  
bool b = (a != 2*a-1); // b = false
```

# Boolean Functions in Mathematics

- Boolean function

$$f : \{0, 1\}^2 \rightarrow \{0, 1\}$$

- 0 corresponds to “false”.
- 1 corresponds to “true”.

- “logical And”

$$f : \{0, 1\}^2 \rightarrow \{0, 1\}$$

- 0 corresponds to “false”.
- 1 corresponds to “true”.

$x$	$y$	$\text{AND}(x, y)$
0	0	0
0	1	0
1	0	0
1	1	1

# Logical Operator &&

`a && b` (logical and)

```
int n = -1;  
int p = 3;  
bool b = (n < 0) && (0 < p); //
```

# Logical Operator &&

`a && b` (logical and)

```
int n = -1;  
int p = 3;  
bool b = (n < 0) && (0 < p); // b = true
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- “logical Or”

$$f : \{0, 1\}^2 \rightarrow \{0, 1\}$$

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$x$	$y$	$\text{OR}(x, y)$
0	0	0
0	1	1
1	0	1
1	1	1

# Logical Operator ||

`a || b` (logical or)

```
int n = 1;  
int p = 0;  
bool b = (n < 0) || (0 < p); //
```



# Logical Operator ||

`a || b` (logical or)

```
int n = 1;  
int p = 0;  
bool b = (n < 0) || (0 < p); // b = false
```

- “logical Not”

$$f : \{0, 1\} \rightarrow \{0, 1\}$$

- 0 corresponds to “false”.
- 1 corresponds to “true”.

$x$	NOT( $x$ )
0	1
1	0

# Logical Operator !

**!b** (logical not)

**bool** → **bool**

R-value → R-value

# Logical Operator !

**!** (logical not)

```
int n = 1;  
bool b = !(n < 0); //
```

# Logical Operator !

**!b** (logical not)

```
int n = 1;  
bool b = !(n < 0); // b = true
```

# Precedences

`!b && a`

# Precedences

`!b && a`  
⇕  
`(!b) && a`

# Precedences

a && b || c && d



# Precedences

a && b || c && d  
⇕  
(a && b) || (c && d)

# Precedences

a || b && c || d

# Precedences

a || b && c || d  
⇕  
a || (b && c) || d

# Precedences

```
7 + x < y && y != 3 * z || ! b
```

# Precedences

**The unary logical** operator !  
binds more strongly than

```
7 + x < y && y != 3 * z || (!b)
```

# Precedences

**The unary logical** operator !  
binds more strongly than  
**binary arithmetic** operators. These  
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```
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# Precedences

**The unary logical** operator !  
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((7 + x) < y) && (y != (3 * z)) || (!b)
```

# Precedences

**The unary logical** operator !  
binds more strongly than  
**binary arithmetic** operators. These  
bind more strongly than  
**relational** operators,  
and these bind more strongly than  
**binary logical** operators.

```
((7 + x) < y) && (y != (3 * z)) || (!b)
```

Some parentheses on the previous slides were actually redundant.



# Completeness

- AND, OR and NOT are the boolean functions available in C++.

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- Any other *binary* boolean function can be generated from them.

$x$	$y$	$\text{XOR}(x, y)$
0	0	0
0	1	1
1	0	1
1	1	0

$$\text{XOR}(x, y) = \text{AND}(\text{OR}(x, y), \text{NOT}(\text{AND}(x, y))).$$

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$$x \oplus y = (x \vee y) \wedge \neg(x \wedge y).$$

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$$x \oplus y = (x \vee y) \wedge \neg(x \wedge y).$$

$$(x \ || \ y) \ \&\& \ !(x \ \&\& \ y)$$

# Completeness Proof

- Identify binary boolean functions with their characteristic vector.

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- Identify binary boolean functions with their characteristic vector.

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characteristic vector: 0110



# Completeness Proof

- Identify binary boolean functions with their characteristic vector.

$x$	$y$	XOR( $x, y$ )
0	0	0
0	1	1
1	0	1
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characteristic vector: 0110

$$\text{XOR} = f_{0110}$$

# Completeness Proof

- Step 1: generate the *fundamental* functions  $f_{0001}$ ,  $f_{0010}$ ,  $f_{0100}$ ,  $f_{1000}$

$$f_{0001} = \text{AND}(x, y)$$

$$f_{0010} = \text{AND}(x, \text{NOT}(y))$$

$$f_{0100} = \text{AND}(y, \text{NOT}(x))$$

$$f_{1000} = \text{NOT}(\text{OR}(x, y))$$

# Completeness Proof

- Step 2: generate all functions by applying logical or

$$f_{1101} = \text{OR}(f_{1000}, \text{OR}(f_{0100}, f_{0001}))$$

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- Step 2: generate all functions by applying logical or

$$f_{1101} = \text{OR}(f_{1000}, \text{OR}(f_{0100}, f_{0001}))$$

- Step 3: generate  $f_{0000}$

$$f_{0000} = 0.$$

# bool vs int: Conversion

- `bool` can be used whenever `int` is expected

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<code>bool</code>	→	<code>int</code>
<i>true</i>	→	1
<i>false</i>	→	0

# bool vs int: Conversion

- **bool** can be used whenever **int** is expected – and vice versa.

<b>bool</b>	→	<b>int</b>
<i>true</i>	→	1
<i>false</i>	→	0
<b>int</b>	→	<b>bool</b>
≠0	→	<i>true</i>
0	→	<i>false</i>

# bool vs int: Conversion

- **bool** can be used whenever **int** is expected – and vice versa.

<b>bool</b>	→	<b>int</b>
<i>true</i>	→	1
<i>false</i>	→	0
<b>int</b>	→	<b>bool</b>
$\neq 0$	→	<i>true</i>
0	→	<i>false</i>

```
bool b = 3; // b=true
```



# bool vs int: Conversion

- `bool` can be used whenever `int` is expected – and vice versa.
- Many existing programs use `int` instead of `bool`

**This is bad style originating from the language C.**

<code>bool</code>	→	<code>int</code>
<i>true</i>	→	1
<i>false</i>	→	0
<code>int</code>	→	<code>bool</code>
<code>≠0</code>	→	<i>true</i>
0	→	<i>false</i>

```
bool b = 3; // b=true
```

# DeMorgan Rules

- $!(a \ \&\& \ b) == (!a \ || \ !b)$

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! (rich *and* beautiful) == (poor *or* ugly)

# DeMorgan Rules

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$!(\text{rich } \textit{and} \ \text{beautiful}) == (\text{poor } \textit{or} \ \text{ugly})$

# Application: either ... or (XOR)

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`(x || y) && !(x && y)`    x or y, and not both

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`!(!x && !y) && !(x && y)`

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# Application: either ... or (XOR)

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`!(!x && !y) && !(x && y)` not none and not both

`!(!x && !y || x && y)`

# Application: either ... or (XOR)

$(x \ || \ y) \ \&\& \ !(x \ \&\& \ y)$     x or y, and not both

$(x \ || \ y) \ \&\& \ (!x \ || \ !y)$     x or y, and one of them not

$!(\!x \ \&\& \ !y) \ \&\& \ !(x \ \&\& \ y)$     not none and not both

$!(\!x \ \&\& \ !y \ || \ x \ \&\& \ y)$     not: both or none

# Short circuit Evaluation

- Logical operators `&&` and `||` evaluate the *left operand first*.
- If the result is then known, the right operand will *not be* evaluated.

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# Short circuit Evaluation

- Logical operators `&&` and `||` evaluate the *left operand first*.
- If the result is then known, the right operand will *not be* evaluated.

x has value 0  $\Rightarrow$

```
false && z / x > y
```

# Short circuit Evaluation

- Logical operators `&&` and `||` evaluate the *left operand first*.
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***false***

# Short circuit Evaluation

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- If the result is then known, the right operand will *not be* evaluated.

x has value 0  $\Rightarrow$

```
x != 0 && z / x > y
```

$\Rightarrow$  No division by 0

# 4. Defensive Programming

---

Constants and Assertions

# Sources of Errors

- Errors that the compiler can find:  
syntactical and some semantical errors

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- Errors that the compiler can find:  
syntactical and some semantical errors
- Errors that the compiler cannot find:  
runtime errors (always semantical)

# The Compiler as Your Friend: Constants

## Constants

- are variables with immutable value

```
const int speed_of_light = 299792458;
```

- Usage: `const` before the definition



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# The Compiler as Your Friend: Constants

- Compiler checks that the **const**-promise is kept

```
const int speed_of_light = 299792458;  
...  
speed_of_light = 300000000;
```

compiler: error



- Tool to avoid errors: constants guarantee the promise :*“value does not change”*

# The Compiler as Your Friend: Constants

- Compiler checks that the **const**-promise is kept

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# The Compiler as Your Friend: Constants

- Compiler checks that the `const`-promise is kept

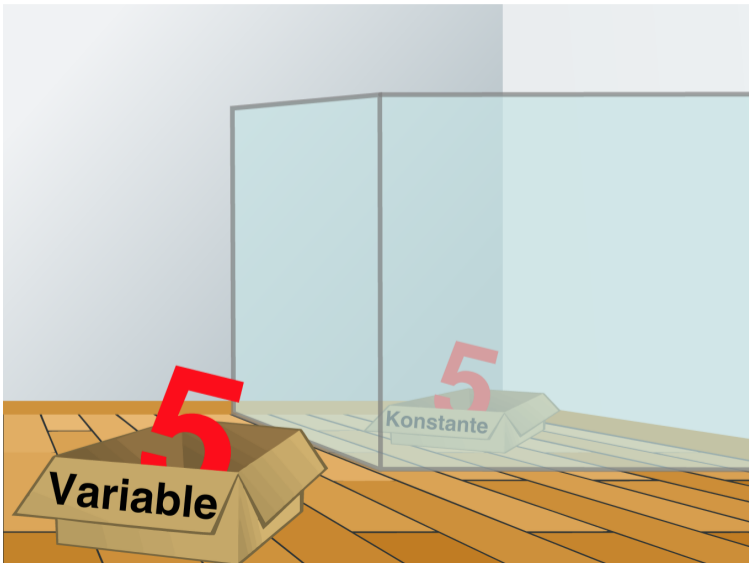
```
const int speed_of_light = 299792458;  
...  
speed_of_light = 300000000;
```

**compiler: error**



- Tool to avoid errors: constants guarantee the promise :“*value does not change*”

# Constants: Variables behind Glass



# The `const`-guideline

## const-guideline

For *each variable*, think about whether it will change its value in the lifetime of a program. If not, use the keyword **`const`** in order to make the variable a constant.

A program that adheres to this guideline is called **`const`**-correct.

# Avoid Sources of Bugs

1. Exact knowledge of the wanted program behavior



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» It's not a bug, it's a feature! «

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2. Check at many places in the code if the program is still on track

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1. Exact knowledge of the wanted program behavior
2. Check at many places in the code if the program is still on track
3. Question the (seemingly) obvious, there could be a typo in the code

# Against Runtime Errors: *Assertions*

`assert(expr)`

- halts the program if the boolean expression **expr** is false

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# Against Runtime Errors: *Assertions*

`assert(expr)`

- halts the program if the boolean expression **expr** is false
- requires `#include <cassert>`
- can be switched off (potential performance gain)

# Assertions for the $\text{gcd}(x, y)$

Check if the program is on track ...

```
// Input x and y
std::cout << "x =? ";
std::cin >> x;
std::cout << "y =? ";
std::cin >> y;
```

Input arguments for calculation

```
// Check validity of inputs
assert(x > 0 && y > 0);
```

```
... // Compute gcd(x,y), store result in variable a
```

# Assertions for the $\text{gcd}(x, y)$

Check if the program is on track ...

```
// Input x and y
std::cout << "x =? ";
std::cin >> x;
std::cout << "y =? ";
std::cin >> y;

// Check validity of inputs
assert(x > 0 && y > 0); ← Precondition for the ongoing computation

... // Compute gcd(x,y), store result in variable a
```



# Assertions for the $\text{gcd}(x, y)$

... and question the obvious! ...

...

```
assert(x > 0 && y > 0);
```

← Precondition for the ongoing computation

```
... // Compute gcd(x,y), store result in variable a
```

```
assert (a >= 1);
```

```
assert (x % a == 0 && y % a == 0);
```

```
for (int i = a+1; i <= x && i <= y; ++i)
```

```
    assert(!(x % i == 0 && y % i == 0));
```

# Assertions for the $\text{gcd}(x, y)$

... and question the obvious! ...

...

```
assert(x > 0 && y > 0);
```

```
... // Compute gcd(x,y), store result in variable a
```

```
assert (a >= 1);
```

```
assert (x % a == 0 && y % a == 0);
```

```
for (int i = a+1; i <= x && i <= y; ++i)
```

```
    assert(!(x % i == 0 && y % i == 0));
```

Properties of the  
gcd

# Switch off Assertions

```
#define NDEBUG // To ignore assertions
#include<cassert>
```

```
...
```

```
assert(x > 0 && y > 0); // Ignored
```

```
... // Compute gcd(x,y), store result in variable a
```

```
assert(a >= 1); // Ignored
```

```
...
```

# Fail-Fast with Assertions

- Real software: many C++ files, complex control flow



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- Errors surface late(r) → impedes error localisation



# Fail-Fast with Assertions

- Real software: many C++ files, complex control flow
- Errors surface late(r) → impedes error localisation
- Assertions: Detect errors early



# 5. Control Structures I

---

Selection Statements, Iteration Statements, Termination, Blocks



# Control Flow

- Up to now: *linear* (from top to bottom)
- Interesting programs require “branches” and “jumps”

```
// Project Hangman
...
while (game_not_over) {
    ...
    if (word.contains(guess)) {
        ...
    } else {
        ...
    }
}
...
}
```

# Selection Statements

implement branches

- **if** statement
- **if-else** statement

# if-Statement

```
if ( condition )  
    statement
```

# if-Statement

```
if ( condition )  
    statement
```

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";
```

# if-Statement

```
if ( condition )  
    statement
```

If *condition* is true then *statement* is executed

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";
```

# if-Statement

```
if ( condition )  
    statement
```

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";
```

If *condition* is true then *statement* is executed

- *statement*: arbitrary statement (*body* of the **if**-Statement)
- *condition*: convertible to **bool**

# if-else-statement

```
if ( condition )  
    statement1  
else  
    statement2
```

# if-else-statement

```
if ( condition )  
    statement1  
else  
    statement2
```

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```



# if-else-statement

```
if ( condition )  
    statement1  
else  
    statement2
```

If *condition* is true then *statement1* is executed, otherwise *statement2* is executed.

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```

# if-else-statement

```
if ( condition )  
    statement1  
else  
    statement2
```

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```

If *condition* is true then *statement1* is executed, otherwise *statement2* is executed.

- *condition*: convertible to **bool**.
- *statement1*: *body* of the **if**-branch
- *statement2*: *body* of the **else**-branch

# Layout!

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
    std::cout << "odd";
```

# Layout!

```
int a;  
std::cin >> a;  
if (a % 2 == 0)  
    std::cout << "even";  
else  
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```

Indentation

Indentation

# Iteration Statements

implement loops

- **for**-statement
- **while**-statement
- **do**-statement

# Compute $1 + 2 + \dots + n$

```
// input
std::cout << "Compute the sum 1+...+n for n=";
unsigned int n;
std::cin >> n;

// computation of sum_{i=1}^n i
unsigned int s = 0;
for (unsigned int i = 1; i <= n; ++i)
    s += i;

// output
std::cout << "1+...+" << n << " = " << s << ".\n";
```

# Compute $1 + 2 + \dots + n$

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// input
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// output
std::cout << "1+...+" << n << " = " << s << ".\n";
```

# for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions:  $n == 2, s == 0$

i

s



# for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
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```

Assumptions:  $n == 2, s == 0$

<i>i</i>	<i>s</i>
<i>i</i> ==1	

# for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions:  $n == 2, s == 0$

$i$	$s$
$i==1$	$i \leq 2?$

# for-Statement Example

```
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    s += i;
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Assumptions:  $n == 2, s == 0$

$i$		$s$
$i==1$	wahr	

# for-Statement Example

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```

Assumptions:  $n == 2, s == 0$

$i$		$s$
$i==1$	wahr	$s == 1$

# for-Statement Example

```
for ( unsigned int i=1; i <= n ; ++i )  
    s += i;
```

Assumptions: `n == 2, s == 0`

<code>i</code>		<code>s</code>
<code>i==1</code>	wahr	<code>s == 1</code>
<code>i==2</code>		

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i==1	wahr	s == 1
i==2	i <= 2?	

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$i==2$	wahr	$s == 3$
$i==3$	$i <= 2?$	

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# for-Statement: Syntax

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for (init statement; condition; expression)  
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- *init statement*: expression statement, declaration statement, null statement
- *condition*: convertible to **bool**
- *expression*: any expression
- *body statement*: any statement (*body* of the for-statement)

# for-Statement: Termination

```
for (unsigned int i = 1; i <= n; ++i)  
    s += i;
```

Here and in most cases:

- *expression* changes its value that appears in *condition* .

# for-Statement: Termination

```
for (unsigned int i = 1; i <= n; ++i)  
    s += i;
```

Here and in most cases:

- After a finite number of iterations *condition* becomes false: **Termination**

# Infinite Loops

- Infinite loops are easy to generate:

```
for ( ; ; ) ;
```

- Die *empty condition* is true.
- Die *empty expression* has no effect.
- Die *null statement* has no effect.

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- Infinite loops are easy to generate:

```
for ( ; ; ) ;
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- Die *empty condition* is true.
  - Die *empty expression* has no effect.
  - Die *null statement* has no effect.
- ... but can in general not be automatically detected.

```
for (init; cond; expr) stmt;
```

# Halting Problem

## Undecidability of the Halting Problem

There is no C++ program that can determine for each C++-Program  $P$  and each input  $I$  if the program  $P$  terminates with the input  $I$ .

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<sup>4</sup>Alan Turing, 1936. Theoretical questions of this kind were the main motivation for Alan Turing to construct a computing machine.

# Halting Problem

## Undecidability of the Halting Problem

There is no C++ program that can determine for each C++-Program  $P$  and each input  $I$  if the program  $P$  terminates with the input  $I$ .

This means that the correctness of programs can in general *not* be automatically checked.<sup>4</sup>

---

<sup>4</sup>Alan Turing, 1936. Theoretical questions of this kind were the main motivation for Alan Turing to construct a computing machine.

# Example: Prime Number Test

**Def.:** a natural number  $n \geq 2$  is a prime number, if no  $d \in \{2, \dots, n - 1\}$  divides  $n$ .



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A loop that can test this:

```
unsigned int d;  
for (d=2; n%d != 0; ++d);
```

(body is the null statement)

# Example: Termination

```
unsigned int d;  
for (d=2; n%d != 0; ++d); // for n >= 2
```

- Progress: Initial value **d=2**, then plus 1 in every iteration (**++d**)

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- Progress: Initial value **d=2**, then plus 1 in every iteration (**++d**)
- Exit: **n%d != 0** evaluates to **false** as soon as a divisor is found — at the latest, once **d == n**
- Progress guarantees that the exit condition will be reached

# Example: Correctness

```
unsigned int d;  
for (d=2; n%d != 0; ++d); // for n >= 2
```

Every potential divisor  $2 \leq d \leq n$  will be tested. If the loop terminates with  $d == n$  then and only then is  $n$  prime.

# Blocks

- Blocks group a number of statements to a new statement

```
{statement1 statement2 ... statementN}
```

# Blocks

- Blocks group a number of statements to a new statement
- Example: body of the main function

```
int main() {  
    ...  
}
```



# Blocks

- Blocks group a number of statements to a new statement
- Example: loop body

```
for (unsigned int i = 1; i <= n; ++i) {  
    s += i;  
    std::cout << "partial sum is " << s << "\n";  
}
```

# Blocks

- Blocks group a number of statements to a new statement
- Beispiel: if / else

```
if (d < n) // d is a divisor of n in {2,...,n-1}
    std::cout << n << " = " << d << " * " << n / d << ".\n";
else {
    assert (d == n);
    std::cout << n << " is prime.\n";
}
```