19. Classes

Overloading Functions and Operators, Encapsulation, Classes, Member Functions, Constructors

Function Overloading

- A function is defined by name, types, number and order of arguments

```
double sq (double x) { ... }        // f1
int sq (int x) { ... }              // f2
int pow (int b, int e) { ... }      // f3
int pow (int e) { return pow (2,e); } // f4
```

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```
std::cout << sq (3);
```

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```
std::cout << sq (3);   // compiler chooses f2
std::cout << sq (1.414);
```

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std::cout << pow (2);
```

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std::cout << sq (3);   // compiler chooses f2
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std::cout << pow (2);  // compiler chooses f4
std::cout << pow (3,3);
```

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std::cout << sq (1.414); // compiler chooses f1
std::cout << pow (2);  // compiler chooses f4
std::cout << pow (3,3); // compiler chooses f3
```

Operator Overloading

- Operators are special functions and can be overloaded
- Name of the operator *op*:

```
operatorop
```

Adding `rational` Numbers – Before

```
// POST: return value is the sum of a and b
rational add (rational a, rational b)
{
    rational result;
    result.n = a.n * b.d + a.d * b.n;
    result.d = a.d * b.d;
    return result;
}
...
const rational t = add (r, s);
```

Adding `rational` Numbers – After

```
// POST: return value is the sum of a and b
rational operator+ (rational a, rational b)
{
    rational result;
    result.n = a.n * b.d + a.d * b.n;
    result.d = a.d * b.d;
    return result;
}
...
const rational t = r + s;
```

Adding `rational` Numbers – After

```
// POST: return value is the sum of a and b
rational operator+ (rational a, rational b)
{
    rational result;
    result.n = a.n * b.d + a.d * b.n;
    result.d = a.d * b.d;
    return result;
}
...
const rational t = r + s;
```

infix notation (pointing to the `+` in `r + s`)

Adding `rational` Numbers – After

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// POST: return value is the sum of a and b
rational operator+ (rational a, rational b)
{
    rational result;
    result.n = a.n * b.d + a.d * b.n;
    result.d = a.d * b.d;
    return result;
}
...
const rational t = operator+ (r, s);
```

equivalent but less handy: functional notation

Unary Minus

Only one argument:

```
// POST: return value is -a
rational operator- (rational a)
{
    a.n = -a.n;
    return a;
}
```

Comparison Operators

can be defined such that they do the right thing:

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```
// POST: returns true iff a == b
bool operator== (rational a, rational b)
{
    return a.n * b.d == a.d * b.n;
}
```

Comparison Operators

can be defined such that they do the right thing:

```
// POST: returns true iff a == b
bool operator== (rational a, rational b)
{
    return a.n * b.d == a.d * b.n;
}
```

$$\frac{2}{3} = \frac{4}{6} \quad \checkmark$$

Arithmetic Assignment

We want to write

```
rational r;
r.n = 1; r.d = 2;                    // 1/2

rational s;
s.n = 1; s.d = 3;                    // 1/3

r += s;
std::cout << r.n << "/" << r.d;      // 5/6
```

Operator +=

```
rational& operator+= (rational& a, rational b)
{
    a.n = a.n * b.d + a.d * b.n;
    a.d *= b.d;
    return a;
}
```

Operator +=

```
rational& operator+= (rational& a, rational b)
{
    a.n = a.n * b.d + a.d * b.n;
    a.d *= b.d;
    return a;
}
```

- The L-value **a** is increased by the value of **b** and returned as L-value

In/Output Operators

can also be overloaded.

- Before:

```
std::cout << "Sum is " << t.n << "/" << t.d << "\n";
```

- After (desired):

```
std::cout << "Sum is " << t << "\n";
```

In/Output Operators

can be overloaded as well:

```
// POST: r has been written to out
std::ostream& operator<< (std::ostream& out, rational r)
{
    return out << r.n << "/" << r.d;
}
```

In/Output Operators

can be overloaded as well:

```
// POST: r has been written to out
std::ostream& operator<< (std::ostream& out, rational r)
{
    return out << r.n << "/" << r.d;
}
```

writes **r** to the output stream
and returns the stream as L-value.

Input

```
// PRE: in starts with a rational number of the form "n/d"
// POST: r has been read from in
std::istream& operator>> (std::istream& in, rational& r){
    char c; // separating character ’/’
    return in >> r.n >> c >> r.d;
}
```

reads **r** from the input stream
and returns the stream as L-value.

Goal Attained!

```
// input
std::cout << "Rational number r =? ";
rational r;
std::cin >> r;

std::cout << "Rational number s =? ";
rational s;
std::cin >> s;

// computation and output
std::cout << "Sum is " << r + s << ".\n";
```

Goal Attained!

```
// input
std::cout << "Rational number r =? ";
rational r;
std::cin >> r;

std::cout << "Rational number s =? ";
rational s;
std::cin >> s;

// computation and output
std::cout << "Sum is " << r + s << ".\n";
```

operator >>

operator +

operator<<

A new Type with Functionality...

```
struct rational {
    int n;
    int d; // INV: d != 0
};

// POST: return value is the sum of a and b
rational operator+ (rational a, rational b)
{
    rational result;
    result.n = a.n * b.d + a.d * b.n;
    result.d = a.d * b.d;
    return result;
}
...
```

...should be in a Library!

rational.h

- Definition of a struct `rational`
- Function declarations

rational.cpp

- arithmetic operators (`operator+`, `operator+=`, ...)
- relational operators (`operator==`, `operator>`, ...)
- in/output (`operator >>`, `operator <<`, ...)

Thought Experiment

The three core missions of ETH:

- research

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We found a startup: RAT PACK®!

Thought Experiment

The three core missions of ETH:

- research
- education
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We found a startup: RAT PACK®!

- Selling the `rational` library to customers
- ongoing development according to customer's demands

The Customer is Happy

"Buying RAT PACK® has been a game-changing move to put us on the forefront of cutting-edge technology in social media engineering."

B. Labla, CEO

The Customer is Happy

…and programs busily using `rational`.

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- output as `double`-value $\left(\frac{3}{5} \rightarrow 0.6\right)$

The Customer is Happy

. . . and programs busily using `rational`.

- output as `double`-value $(\frac{3}{5} \rightarrow 0.6)$

```
// POST: double approximation of r
double to_double (rational r)
{
  double result = r.n;
  return result / r.d;
}
```

The Customer Wants More

“Can we have rational numbers with an extended value range?”

The Customer Wants More

"Can we have rational numbers with an extended value range?"

- Sure, no problem, e.g.:

```
struct rational {
  int n;
  int d;
};
```

⇒

```
struct rational {
  unsigned int n;
  unsigned int d;
  bool is_positive;
};
```

New Version of RAT PACK®

 **It sucks, nothing works any more!**

New Version of RAT PACK®

It sucks, nothing works any more!

- What is the problem?

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$-\frac{3}{5}$ is sometimes 0.6, this cannot be true!

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$-\frac{3}{5}$ is sometimes 0.6, this cannot be true!

- That is your fault. Your conversion to `double` is the problem, our library is correct.

New Version of RAT PACK®


It sucks, nothing works any more!

- What is the problem?


$-\frac{3}{5}$ is sometimes 0.6, this cannot be true!

- That is your fault. Your conversion to `double` is the problem, our library is correct.


Up to now it worked, therefore the new version is to blame!

Liability Discussion

```
// POST: double approximation of r
double to_double (rational r){
  double result = r.n;
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correct using...

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struct rational {
  int n;
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struct rational {
  int n;
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};
```

…not correct using

```
struct rational {
  unsigned int n;
  unsigned int d;
  bool is_positive;
};
```

Liability Discussion

```
// POST: double approximation of r
double to_double (rational r){
  double result = r.n;
  return result / r.d;
}
```

r.is_positive and result.is_positive do not appear.

correct using…

```
struct rational {
  int n;
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```

…not correct using

```
struct rational {
  unsigned int n;
  unsigned int d;
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- Customer sees and uses our **representation** of rational numbers (initially `r.n, r.d`)

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- Customer sees and uses our **representation** of rational numbers (initially `r.n, r.d`)
- When we change it (`r.n, r.d, r.is_positive`), the customer's programs do not work anymore.
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$\Rightarrow$ RAT PACK® is history...

Idea of Encapsulation (Information Hiding)

- A type is uniquely defined by its *value range* and its *functionality*

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- $\Rightarrow$ The customer is not provided with *representation* but with **functionality**!

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- The *representation* should *not be visible*.
- $\Rightarrow$ The customer is not provided with *representation* but with **functionality**!

```
str.length(),
v.push_back(1),...
```

Classes

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- are a variant of structs

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- provide the concept for **encapsulation** in C++
- are a variant of structs
- are provided in many *object oriented programming languages*

Encapsulation: `public` / `private`

```
class rational {
  int n;
  int d; // INV: d != 0
};
```

is used instead of **`struct`** if anything at all shall be “hidden”

Encapsulation: `public` / `private`

```
class rational {
  int n;
  int d; // INV: d != 0
};
```

is used instead of **`struct`** if anything at all shall be "hidden"

only difference

- **`struct`**: by default **nothing** is hidden
- **`class`** : by default **everything** is hidden

Encapsulation: `public` / `private`

```
class rational {
  int n;
  int d; // INV: d != 0
};
```

Application Code

```
rational r;
r.n = 1;      // error: n is private
r.d = 2;      // error: d is private
int i = r.n; // error: n is private
```

Encapsulation: `public` / `private`

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class rational {
  int n;
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```

Good news: `r.d = 0` cannot happen any more by accident.

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Encapsulation: public / private

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class rational {
  int n;
  int d; // INV: d != 0
};
```

Good news: `r.d = 0` cannot happen any more by accident.

Bad news: the customer cannot do anything any more ...

...and we can't, either.
(no `operator+`,...)

Application Code

```
rational r;
r.n = 1;      // error: n is private
r.d = 2;      // error: d is private
int i = r.n; // error: n is private
```

Member Functions: Declaration

```
class rational {
public:
   // POST: return value is the numerator of this instance
   int numerator () const {
     return n;
   }
   // POST: return value is the denominator of this instance
   int denominator () const {
     return d;
   }
private:
   int n;
   int d; // INV: d!= 0
};
```

Member Functions: Declaration

public area

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  int n;
  int d; // INV: d!= 0
};
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private:
    int n;
    int d; // INV: d!= 0
};
```

public area

member function

member functions have access to private data

Member Functions: Call

```
// Definition des Typs
class rational {
    ...
};
...
// Variable des Typs
rational r;
```

member access

```
int n = r.numerator();    // Zaehler
int d = r.denominator(); // Nenner
```

Member Functions: Definition

```
// POST: returns numerator of this instance
int numerator () const
{
  return n;
}
```

Member Functions: Definition ???

```
// POST: returns numerator of this instance
int numerator ()  const
{
   return n;
}
```

Member Functions: Definition

```
// POST: returns numerator of this instance
int numerator () const
{
  return n;                              r.numerator()
}
```

- A member function is called for an expression of the class.

Member Functions: Definition

```
// POST: returns numerator of this instance
int numerator () const
{
  return n;
}
```

`r.numerator()`

- A member function is called for an expression of the class. in the function, **this** is the name of this *implicit argument.*

Member Functions: Definition

```
// POST: returns numerator of this instance
int numerator ()  const
{
  return n;                          r.numerator()
}
```

- A member function is called for an expression of the class. in the function, **this** is the name of this *implicit argument*.
- *const* refers to the instance **this**

Member Functions: Definition

```
// POST: returns  numerator of this instance
int numerator () const
{
  return n;
}
```

`r.numerator()`

- A member function is called for an expression of the class. in the function, **`this`** is the name of this *implicit argument*.
- *const* refers to the instance **`this`**
- **`n`** is the shortcut for **`this->n`** (precise explanation of "**`->`**" next week)

const and Member Functions

```
class rational {
public:
  int numerator () const
  { return n; }
  void set_numerator (int N)
  { n = N;}
...
}
```

```
rational x;
x.set_numerator(10); // ok;
const rational y = x;
int n = y.numerator(); // ok;
y.set_numerator(10); // error;
```

The **const** at a member function is to promise that an instance cannot be changed via this function.

const items can only call **const** member functions.

Comparison

```
class rational {
    int n;
    ...
public:
    int numerator () const
    {
        return n;
    }
};

rational r;
...
std::cout << r.numerator();
```

Comparison

```
class rational {
    int n;
    ...
public:
    int numerator () const
    {
        return this->n;
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};

rational r;
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std::cout << r.numerator();
```

Comparison

Roughly like this it were ...

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class rational {
    int n;
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rational r;
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```

Comparison

Roughly like this it were …

```
class rational {
    int n;
    ...
public:
    int numerator () const
    {
        return this->n;
    }
};

rational r;
...
std::cout << r.numerator();
```

… without member functions

```
struct bruch {
    int n;
    ...
};

int numerator (const bruch& dieser)
{
    return dieser.n;
}

bruch r;
..
std::cout << numerator(r);
```

Member-Definition: In-Class

```
class rational {
    int n;
    ...
public:
    int numerator () const
    {
        return n;
    }
    ....
};
```

- No separation between declaration and definition (bad for libraries)

Member-Definition: In-Class vs. Out-of-Class

```
class rational {
    int n;
    ...
public:
    int numerator () const
    {
        return n;
    }
    ....
};
```

- No separation between declaration and definition (bad for libraries)

```
class rational {
    int n;
    ...
public:
    int numerator () const;
    ...
};

int rational::numerator () const
{
  return n;
}
```

- This also works.

Initialisation? Constructors!

```
class rational
{
public:
    rational (int num, int den)
        : n (num), d (den)
    {
        assert (den != 0);
    }
...
};
...
rational r (2,3); // r = 2/3
```

Initialisation? Constructors!

```
class rational
{
public:
    rational (int num, int den)
        : n (num), d (den)    ← Initialization of the member variables
    {
        assert (den != 0);    ← function body.
    }
...
};
...
rational r (2,3); // r = 2/3
```

Initialisation “rational = int”?

```
class rational
{
public:
    rational (int num)
        : n (num), d (1)
    {}
...
};
...
rational r (2); // explicit initialization with 2
rational s = 2; // implicit conversion
```

Initialisation “`rational = int`”?

```
class rational
{
public:
    rational (int num)
        : n (num), d (1)
    {}    ⟵ empty function body
...
};
...
rational r (2); // explicit initialization with 2
rational s = 2; // implicit conversion
```

The Default Constructor

```
class rational
{
public:
    ...
    rational ()
        : n (0), d (1)
    {}
...
};
...
rational r;   // r = 0
```

empty list of arguments (annotation pointing to `()`)

The Default Constructor

```
class rational
{
public:
    ...
    rational ()
        : n (0), d (1)
    {}
...
};
...
rational r;   // r = 0
```

empty list of arguments

⇒ There are no uninitiatlized variables of type rational any more!

Alterantively: Deleting a Default Constructor

```
class rational
{
public:
    ...
    rational () = delete;
...
};
...
rational r;   // error:  use of deleted function ’rational::rational()
```

⇒ There are no uninitiatlized variables of type rational any more!

User Defined Conversions

are defined via constructors with exactly *one* argument

```
rational (int num)
    : n (num), d (1)
  {}

rational r = 2; // implizite Konversion
```

User Defined Conversions

are defined via constructors with exactly *one* argument

```
rational (int num)
    : n (num), d (1)
  {}
```

← User defined conversion from **int** to **rational**. values of type **int** can now be converted to **rational**.

```
rational r = 2; // implizite Konversion
```

RAT PACK® Reloaded ...

Customer's program now looks like this:

```
// POST: double approximation of r
double to_double (const rational r)
{
  double result = r.numerator();
  return result / r.denominator();
}
```

RAT PACK® Reloaded ...

Customer's program now looks like this:

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// POST: double approximation of r
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  double result = r.numerator();
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}
```

- We can adapt the member functions together with the representation ✓

RAT PACK® Reloaded ...

before

```
class rational {
...
private:
  int n;
  int d;
};
```

RAT PACK® Reloaded ...

before

```
class rational {
...
private:
  int n;
  int d;
};
```

```
int numerator () const
{
  return n;
}
```

RAT PACK® Reloaded ...

before

```
class rational {
...
private:
  int n;
  int d;
};
```

```
int numerator () const
{
  return n;
}
```

after

```
class rational {
...
private:
  unsigned int n;
  unsigned int d;
  bool is_positive;
};
```

RAT PACK® Reloaded ...

before

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```
int numerator () const{
  if (is_positive)
    return n;
  else {
    int result = n;
    return -result;
  }
}
```

RAT PACK® Reloaded ?

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- value range of nominator and denominator like before

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```

- value range of nominator and denominator like before
- possible overflow in addition

Encapsulation still Incompleete

Customer's point of view (`rational.h`):

```
class rational {
public:
   // POST: returns numerator of *this
   int numerator () const;
   ...
private:
  // none of my business
};
```

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- We determined denominator and nominator type to be **`int`**

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- We determined denominator and nominator type to be **`int`**
- Solution: encapsulate not only data but alsoe types.

Fix: “our” type `rational::integer`

Customer’s point of view (`rational.h`):

```
public:
    using integer = long int; // might change
    // POST: returns numerator of *this
    integer numerator () const;
```

Fix: “our” type `rational::integer`

Customer’s point of view (`rational.h`):

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- We provide an additional type!

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- Determine only **Functionality**, e.g:
  - implicit conversion `int` → `rational::integer`

Fix: “our” type `rational::integer`

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```

- We provide an additional type!
- Determine only **Functionality**, e.g:
  - implicit conversion `int` → `rational::integer`
  - function `double to_double (rational::integer)`

RAT PACK® Revolutions

Finally, a customer program that remains stable

```
// POST: double approximation of r
double to_double (const rational r)
{
  rational::integer n = r.numerator();
  rational::integer d = r.denominator();
  return to_double (n) / to_double (d);
}
```