14. Pointers, Algorithms, Iterators and Containers II

Iterations with Pointers, Arrays: Indices vs. Pointers, Arrays and Functions, Pointers and const, Algorithms, Container and Iteration, Vector-Iteration, Typdef, Sets, the Concept of Iterators

Recall: Pointers running over the Array

Beispiel

```
int a[5] = {3, 4, 6, 1, 2};
for (int* p = a; p < a+5; ++p)
   std::cout << *p << ' '; // 3 4 6 1 2</pre>
```

- An array can be converted into a pointer to its first element.
- Pointers "know" arithmetics and comparisons.
- Pointers can be dereferenced.
- ⇒ Pointers can be used to operate on arrays.

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Arrays: Indices vs. Pointer



```
int a[n];

// Task: set all elements to 0

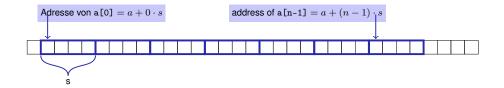
// Solution with indices is more readable
for (int i = 0; i < n; ++i)
    a[i] = 0;

// Solution with pointers is faster and more generic
int* begin = a; // Pointer to the first element
int* end = a+n; // Pointer past the end
for (int* p = begin; p != end; ++p)
    *p = 0;</pre>
```

Arrays and Indices

```
// Set all elements to value
for (int i = 0; i < n; ++i)
   a[i] = value;</pre>
```

Computational costs



⇒ One addition and one multiplication per element

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The Truth about Random Access

The expression

a[i]

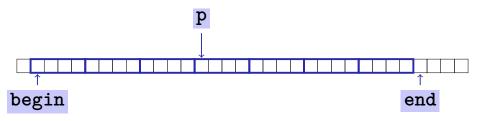
is equivalent to



Arrays and Pointers

```
// set all elements to value
for (int* p = begin; p != end; ++p)
   *p = value;
```

Computational cost



⇒ one **addition** per element

Reading a book ... with indices

... with pointers

Array Arguments: Call by (const) reference

Random Access

- open book on page 1
- close book
- open book on pages 2-3
- close book
- open book on pages 4-5
- close book
- **....**

Sequential Access

- open book on page 1
- turn the page
- ...

```
void print_vector (const int (&v)[3]) {
  for (int i = 0; i<3; ++i) {
    std::cout << v[i] << " ";
  }
}
void make_null_vector (int (&v)[3]) {
  for (int i = 0; i<3; ++i) {
    v[i] = 0;
  }
}</pre>
```

Array Arguments: Call by value (not really ...)

```
void make_null_vector (int v[3]) {
  for (int i = 0; i<3; ++i) {
    v[i] = 0;
  }
}
...
int a[10];
make_null_vector (a); // only sets a[0], a[1], a[2]
int* b;
make_null_vector (b); // no array at b, crash!</pre>
```

Array Arguments: Call by value does not exist

- Formal argument types T[n] or T[] (array over T) are equivalent to T* (pointer to T)
- For passing an array the pointer to its first element is passed
- length information is lost
- Function cannot work on a part of an array (example: search for an element in the second half of an array)

Arrays in Functions

Covention of the standard library: pass an array (or a part of it) using two pointers

- begin: pointer to the first element
- end: pointer behind the last element
- [begin, end) designates the elements of the part of the array
- *valid* range means: there are array elements "available" here.
- [begin, end) is empty if begin == end

Arrays in Functions:

fill

```
// PRE: [begin, end) is a valid range
// POST: every element within [begin, end) will be set to value
void fill (int* begin, int* end, int value) {
  for (int* p = begin; p != end; ++p)
     *p = value;
}
...
expects pointers to the first element of a range
int a[5]:
fill (a, a+5, 1);
for (int i=0; i<5; ++i)
     pass the address (of the first element)
     std::cout << a[i] << " ";</pre>
```

Pointers are not Integers!

- Addresses can be interpreted as house numbers of the memory, that is, integers
- But integer and pointer arithmetics behave differently.

ptr + 1 is *not* the next house number but the s-next, where s is the memory requirement of an object of the type behind the pointer ptr.

Integers and pointers are not compatible

```
int* ptr = 5; // error: invalid conversion from int to int*
int a = ptr; // error: invalid conversion from int* to int
```

Null-Pointer

- special pointer value that signals that no object is pointed to
- represented b the integer number 0 (convertible to T*)

```
int* iptr = 0;
```

- cannot be dereferenced (checked during runtime)
- to avoid undefined behavior

```
int* iptr; // iptr points into ''nirvana''
int j = *iptr; // illegal address in *
```

Pointer Subtraction

- If p1 and p2 point to elements of the same array a with length n
- and $0 \le k_1, k_2 \le n$ are the indices corresponding to p1 and p2, then

$$p$$
1 - p 2 has value k_1 - k_2

Only valid if *p1* and p2 point into the same array.

■ The pointer difference describes "how far away the elements are from each other"

Pointer Operators

Description	Ор	Arity	Precedence	Associativity	Assignment
Subscript	[]	2	17	left	R-value \rightarrow L-value
Dereference	*	1	16	right	$\begin{array}{ccc} \text{R-Wert} & \rightarrow \\ \text{L-Wert} & \end{array}$
Address	&	1	16	rechts	L-value \rightarrow R-value

Precedences and associativities of +, -, ++ (etc.) like in chapter 2

Mutating Functions

■ Pointers can (like references) be used for functions with effect

Beispiel int a[5]; fill(a, a+5, 1); // modifies a pass address of the element past a pass address of the first element of a

Such functions are called mutating

Const Correctness

■ There are also *non*-mutating functions that access elements of an array only in a read-only fashion

```
// PRE: [begin , end) is a valid and nonempty range
// POST: the smallest value in [begin, end) is returned
int min (const int* begin ,const int* end)
{
   assert (begin != end);
   int m = *begin; // current minimum candidate
   for (const int* p = ++begin; p != end; ++p)
      if (*p < m) m = *p;
   return m;
}</pre>
```

mark with const: value of objects cannot be modified through such const-pointers.

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Const and Pointers

Where does the const-modifier belong to?

const T is equivalent to T const and can be written like this

Read the declaration from right to left

```
int const a;
    a is a constant inteher
int const* a;
    a is a pointer to a constant integer
int* const a;
    a is a constant pointer to an integer
int const* const a;
    a is a constant pointer to a constant integer
```

const is not absolute

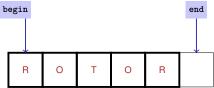
■ The value at an address can change even if a const-pointer stores this address.

```
beispiel
int a[5];
const int* begin1 = a;
int* begin2 = a;
*begin1 = 1;  // error *begin1 is constt
*begin2 = 1;  // ok, although *begin will be modified
```

const is a promise from the point of view of the const-pointer, not an absolute guarantee

Wow - Palindromes!

```
// PRE: [begin end) is a valid range of characters
// POST: returns true if the range forms a palindrome
bool is_palindrome (const char* begin, const char* end) {
  while (begin < end)
    if (*(begin++) != *(--end)) return false;
  return true;
}</pre>
```



Algorithms

For many problems there are prebuilt solutions in the standard library

```
#include <algorithm> // needed for std::fill
...
int a[5];
std::fill (a, a+5, 1);
for (int i=0; i<5; ++i)
    std::cout << a[i] << " "; // 1 1 1 1 1</pre>
```

+5+

Algorithms

Advantages of using the standard library

- simple programs
- less sources of errors
- good, efficient code
- code independent from the data type
- there are also algorithms for more complicated problems such as the efficient sorting of an array

Algorithms

The same prebuilt algorithms work for many different data types.

```
#include <algorithm> // needed for std::fill
...

char c[3];
std::fill (c, c+3, '!');

for (int i=0; i<3; ++i)
    std::cout << c[i]; // !!!</pre>
```

Excursion: Templates

- Templates permit the provision of a type as argument
- The compiler finds the matching type from the call arguments

std::fill is also implemented as template!

Containers and Traversal

- Container: Container (Array, Vector, ...) for elements
- Traversal: Going over all elements of a container
 - Initialization of all elements (fill)
 - Find the smallest element (min)
 - Check properties (is_palindrome)
 - . . .
- There are a lot of different containers (sets, lists, ...)

Iteration Tools

- Arrays: indices (random access) or pointers (natural)
- Array algorithms (std::) use pointers

```
int a[5];
std::fill (a, a+5, 1); // 1 1 1 1 1
```

How do you traverse vectors and other containers?

```
std::vector<int> v (5, 0); // 0 0 0 0 0 std::fill (?, ?, 1); // 1 1 1 1 1
```

Vectors: too sexy for pointers

- Our fill with templates does not work for vectors...
- ...and std::fill also does not work in the following way:

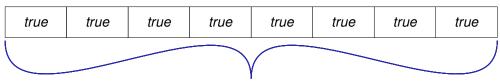
```
std::vector<int> v (5, 0);
std::fill (v, v+5, 1); // Compiler error message !
```

Vectors are snobby...

- they refuse to be converted to pointers,...
- ... and cannot be traversed using pointers either.
- They consider this far too primitive. ⓐ

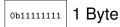
Also in memory: Vector \neq Array

bool a[8] = {true, true, true, true, true, true, true};



8 Byte (Speicherzelle = 1 Byte = 8 Bit)

std::vector<bool> v (8, true);



bool*-pointer does not fit here because it runs byte-wise and not bit-wise

Vector-Iterators

Iterator: a "pointer" that fits to the container.

```
#include <vector>
#include <algorithm> // needed for std::fill

...
std::vector<int> v(5, 0);
std::fill (v.begin(), v.end(), 1);
for (int i=0; i<5; ++i)
    std::cout << v[i] << " "; // 1 1 1 1 1</pre>
```

E0

Vector Iterators

For each vector there are two iterator types defined

- std::vector<int>::const_iterator
 - for non-mutating access
 - in analogy with const int* for arrays
- std::vector<int>::iterator
 - for mutating access
 - in analogy with int* for arrays
- A vector-iterator it is no pointer, but it behaves like a pointer:
 - it points to a vector element and can be dereferenced (*it)
 - it knows arithmetics and comparisons (++it, it+2, it < end,...)

Vector-Iterators: begin() and end()

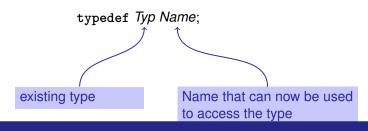
- v.begin() points to the first element of v
- v.end() points past the last element of v
- We can traverse a vector using the iterator...

... or fill a vector.

```
std::fill (v.begin(), v.end(), 1);
```

Type names in C++ can become loooooong

- std::vector<int>::const_iterator
- The declaration of a *type alias* helps with



Examples

typedef std::vector<int> int_vec; typedef int_vec::const_iterator Cvit;

Vector Iterators work like Pointers

Vector Iterators work like Pointers

```
typedef std::vector<int>::iterator Vit;

// manually set all elements to 1
for (Vit it = v.begin(); it != v.end(); ++it)
    *it = 1;

increment the iterator

// output all elements again, using random access
for (int i=0; i<5; ++i)
    std::cout << v[i] << " ";

    short term for
    *(v.begin()+i)</pre>
```

Other Containers: Sets

■ A set is an unordered collection of elements, where each element is contained only once.

$$\{1,2,1\} = \{1,2\} = \{2,1\}$$

■ C++: std::set<T> for a set with elements of type T

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Sets: Example Application

Determine if a given text contains a question mark and output all pairwise different characters!

Letter Salad (1)

Consider a text as a set of characters.

```
#include<set>
...

typedef std::set<char>::const_iterator Csit;
...

std::string text =
"What are the distinct characters in this string?";

std::set<char> s (text.begin(),text.end());

Set is initialized with String iterator range
[text.begin(), text.end())
```

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Letter Salad (2)

Determine if the text contains a question mark and output all characters

```
Search algorithm, can be called with arbitrary iterator range

// check whether text contains a question mark

if (std::find (s.begin(), s.end(), '?') != s.end())

std::cout << "Good question!\n";

// output all distinct characters

for (Csit it = s.begin(); it != s.end(); ++it)

std::cout << *it;

Ausgabe:
Good question!
?Wacdeghinrst
```

Sets and Indices?

■ Can you traverse a set using random access? No.

```
for (int i=0; i<s.size(); ++i)
    std::cout << s[i];
error message: no subscript operator</pre>
```

- Sets are unordered.
 - There is no "ith element".
 - lterator comparison it != s.end() works, but not it < s.end()!</pre>

The Concept of Iterators

The Concept of Iterators

C++knows different iterator types

- Each container provides an associated iterator type.
- All iterators can dereference (*it) and traverse (++it)
- Some can do more, e.g. random access (it[k], or, equivalently *(it + k)), traverse backwards (--it),...

Every container algorithm is generic, that means:

- The container is passed as an iterator-range
- The algorithm works for all containers that fulfil the requirements of the algorithm
- std::find only requires * and ++, for instance
- The implementation details of a container are irrelevant.

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Why Pointers and Iterators?

Would you not prefer the code

```
for (int i=0; i<n; ++i)
a[i] = 0;
```

over the following code?

```
for (int* ptr=a; ptr<a+n; ++ptr)
    *ptr = 0;</pre>
```

Maybe, but in order to use the generic std::fill(a, a+n, 0);, we *have to* work with pointers.

Why Pointers and Iterators?

In order to use the standard library, we have to know that:

- a static array a is a the same time a pointer to the first element of a
- \blacksquare a+i is a pointer to the element with index i

Using the standard library with different containers: Pointers \Rightarrow Iterators

Why Pointers and Iterators?

Example: To search the smallest element of a container in the range [begin, end) use the function call

std::min_element(begin, end)

- returns an *iterator* to the smallest element
- To read the smallest element, we need to dereference:

*std::min_element(begin, end)

15. Recursion 1

Mathematical Recursion, Termination, Call Stack, Examples, Recursion vs. Iteration

That is Why: Pointers and Iterators

- Even for non-programmers and "dumb" users of the standard library: expressions of the form
 - *std::min_element(begin, end)
 cannot be understood without knowing pointers and iterators.
- Behind the scenes of the standard library: working with dynamic memory based on pointers is indispensible. More about this later in this course.

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Mathematical Recursion

- Many mathematical functions can be naturally defined recursively.
- This means, the function appears in its own definition

$$n! = \begin{cases} 1, & \text{if } n \le 1\\ n \cdot (n-1)!, & \text{otherwise} \end{cases}$$

Recursion in C++: In the same Way!

$$n! = \begin{cases} 1, & \text{if } n \le 1\\ n \cdot (n-1)!, & \text{otherwise} \end{cases}$$

```
// POST: return value is n!
unsigned int fac (unsigned int n)
{
  if (n <= 1)
    return 1;
  else
    return n * fac (n-1);
}</pre>
```

Infinite Recursion

- is as bad as an infinite loop...
- ...but even worse: it burns time and memory

```
void f()
{
  f(); // f() -> f() -> ... stack overflow
}
```

Recursive Functions: Termination

As with loops we need

progress towards termination

```
fac(n):
```

terminates immediately for $n \leq 1,$ otherwise the function is called recusively with $<{\bf n}$.

"n is getting smaller for each call."

Recursive Functions: Evaluation

```
Example: fac(4)

// POST: return value is n!
unsigned int fac (unsigned int n)
{
  if (n <= 1) return 1;
  return n * fac(n-1); // n > 1
}
```

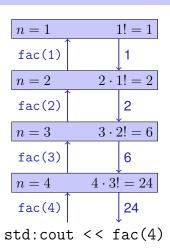
```
Initialization of the formal argument: n = 4 recursive call with argument n - 1 == 3
```

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The Call Stack

For each function call:

- push value of the call argument onto the stack
- always work with the top value
- at the end of the call the top value is removed from the stack



Euclidean Algorithm

- finds the greatest common divisor gcd(a, b) of two natural numbers a and b
- is based on the following mathematical recursion (proof in the lecture notes):

$$\gcd(a,b) = \begin{cases} a, & \text{if } b = 0\\ \gcd(b, a \bmod b), & \text{otherwise} \end{cases}$$

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Euclidean Algorithm in C++

$$\gcd(a,b) = \begin{cases} a, & \text{if } b = 0\\ \gcd(b, a \bmod b), & \text{otherwise} \end{cases}$$

```
unsigned int gcd
  (unsigned int a, unsigned int b)
{
  if (b == 0)
    return a;
  else
    return gcd (b, a % b);
}
Termination: a mod b < b, thus b
gets smaller in each recursive call.
```

Fibonacci Numbers

$$F_n := \begin{cases} 0, & \text{if } n = 0 \\ 1, & \text{if } n = 1 \\ F_{n-1} + F_{n-2}, & \text{if } n > 1 \end{cases}$$

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89...

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Fibonacci Numbers in C++

Laufzeit

```
fib (50) takes "forever" because it computes F_{48} two times, F_{47} 3 times, F_{46} 5 times, F_{45} 8 times, F_{44} 13 times, F_{43} 21 times ... F_{1} ca. 10^{9} times (!)
```

Fast Fibonacci Numbers

Idea:

- Compute each Fibonacci number only once, in the order $F_0, F_1, F_2, \dots, F_n$!
- Memorize the most recent two numbers (variables a and b)!
- Compute the next number as a sum of a and b!

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Fast Fibonacci Numbers in C++

unsigned int fib (unsigned int n){ if (n == 0) return 0; if (n <= 2) return 1; unsigned int a = 1; // F_1 unsigned int b = 1; // F_2 for (unsigned int i = 3; i <= n; ++i){ unsigned int a_old = a; // F_i-2 a = b; // F_i-1 b += a_old; // F_i-1 += F_i-2 -> F_i } return b; }

Recursion and Iteration

Recursion can always be simulated by

- Iteration (loops)
- explicit "call stack" (e.g. array)

Often recursive formulations are simpler, but sometimes also less efficient.