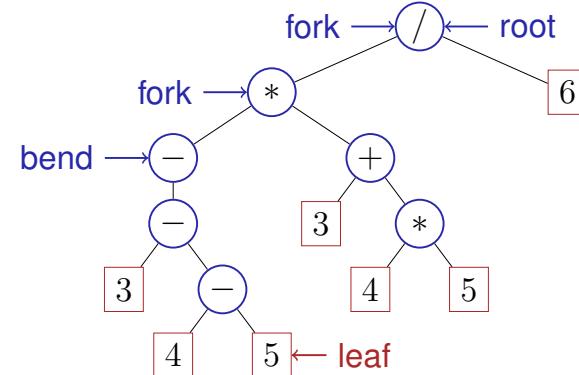


(Expression) Trees

$-(3-(4-5))*(3+4*5)/6$



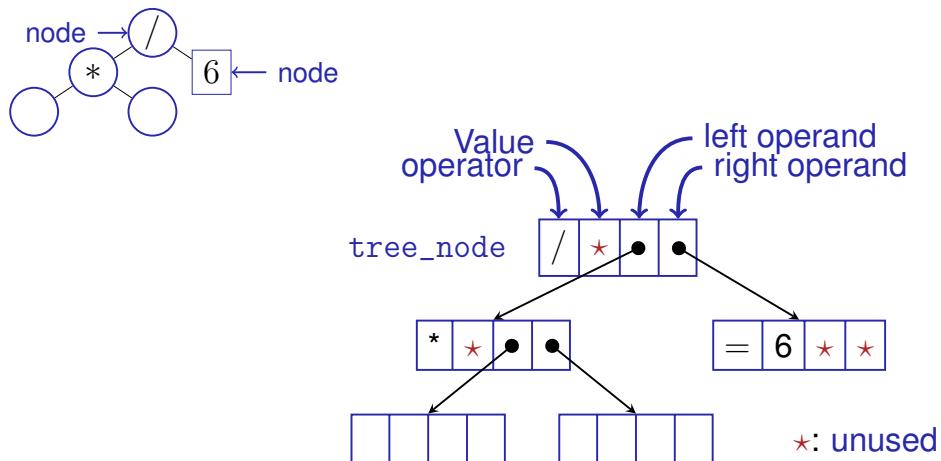
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19. Inheritance and Polymorphism

Expression Trees, Inheritance, Code-Reuse, Virtual Functions, Polymorphism, Concepts of Object Oriented Programming

Nodes: Forks, Bends or Leaves



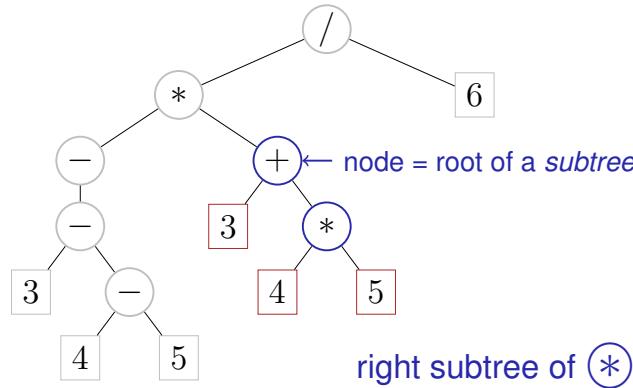
Nodes (struct tree_node)

```
tree_node {  
    char op;  
    // leaf node (op: '=')  
    double val;  
    // internal node ( op: '+', '−', '*', '/')  
    tree_node* left; // == 0 for unary minus  
    tree_node* right;  
    // constructor  
    tree_node (char o, double v, tree_node* l, tree_node* r)  
        : op (o), val (v), left (l), right (r)  
    {}  
};
```

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Nodes and Subtrees



Count Nodes in Subtrees

```
struct tree_node {
    ...
    // POST: returns the size (number of nodes) of
    //       the subtree with root *this
    int size () const
    {
        int s=1;
        if (left) // kurz für left != 0
            s += left->size();
        if (right)
            s += right->size();
        return s;
    }
};
```



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Evaluate Subtrees

```
struct tree_node {
    ...
    // POST: evaluates the subtree with root *this
    double eval () const {
        if (op == '=') return val; ← leaf...
        double l = 0;           ... or fork:
        if (left) l = left->eval(); ← op unary, or left branch
        double r = right->eval(); ← right branch
        if (op == '+') return l + r;
        if (op == '-') return l - r;
        if (op == '*') return l * r;
        if (op == '/') return l / r;
        return 0;
    }
};
```



Cloning Subtrees

```
struct tree_node {
    ...
    // POST: a copy of the subtree with root *this is
    //       made, and a pointer to its root node is
    //       returned
    tree_node* copy () const {
        tree_node* to = new tree_node (op, val, 0, 0);
        if (left)
            to->left = left->copy();
        if (right)
            to->right = right->copy();
        return to;
    }
};
```



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Cloning Subtrees – more Compact Notation

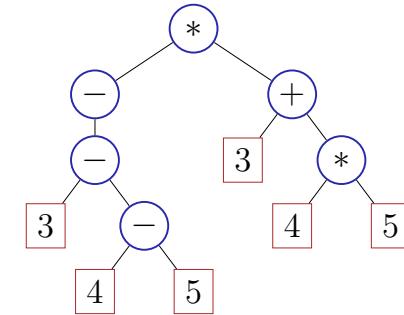
```
struct tree_node {  
    ...  
    // POST: a copy of the subtree with root *this is  
    // made, and a pointer to its root node is  
    // returned  
    tree_node* copy () const {  
        return new tree_node (op, val,  
            left ? left->copy() : 0,  
            right ? right->copy() : 0);  
    }  
};
```

cond ? *expr1* : *expr2* has value *expr1*, if *cond* holds, *expr2* otherwise



Felling Subtrees

```
struct tree_node {  
    ...  
    // POST: all nodes in the subtree with root  
    // *this are deleted  
    void clear() {  
        if (left) {  
            left->clear();  
        }  
        if (right) {  
            right->clear();  
        }  
        delete this;  
    }  
};
```



Powerful Subtrees!

```
struct tree_node {  
    ...  
    // constructor  
    tree_node (char o, tree_node* l,  
              tree_node* r, double v)  
  
    // functionality  
    double eval () const;  
    void print (std::ostream& o) const;  
    int size () const;  
    tree_node* copy () const;  
    void clear ();  
};
```

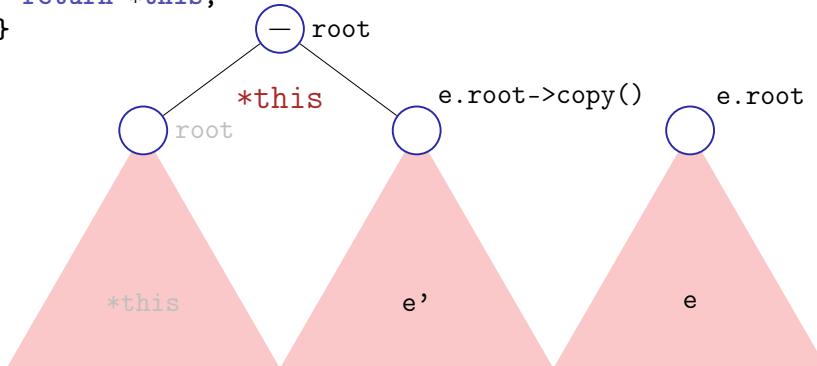
Planting Trees

```
class texpression {  
private:  
    tree_node* root;  
public:  
    ...  
    texpression (double d) ←  
        : root (new tree_node ('=', d, 0, 0)) {}  
    ...  
};
```

creates a tree with
one leaf

Letting Trees Grow

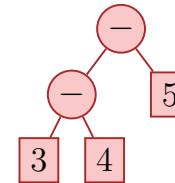
```
texpression& operator-= (const texpression& e)
{
    assert (e.root);
    root = new tree_node ('-', 0, root, e.root->copy());
    return *this;
}
```



Raising Trees

```
texpression operator- (const texpression& l,
                      const texpression& r)
{
    texpression result = l;
    result -= r;
    return result;
}
```

```
texpression a = 3;
texpression b = 4;
texpression c = 5;
texpression d = a-b-c;
```



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Raising Trees

For texpression we also provide

- default constructor, copy constructor, assignment operator, destructor
- arithmetic assignments `+=`, `*=`, `/=`
- binary operators `+`, `*`, `/`
- the unary `-`

From Values to Trees!

```
typedef texpression result_type; // Typ-Alias
```

```
// term = factor { "*" factor | "/" factor }
result_type term (std::istream& is){
{
    result_type value = factor (is);
    while (true) {
        if (consume (is, '*'))
            value *= factor (is);
        else if (consume (is, '/'))
            value /= factor (is);
        else
            return value;
    }
}
```

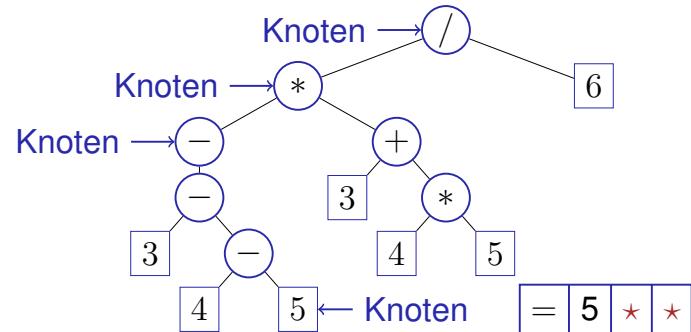
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double_calculator.cpp
(expression value)
→
texpression_calculator_l.cpp
(expression tree)

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Motivation Inheritance:

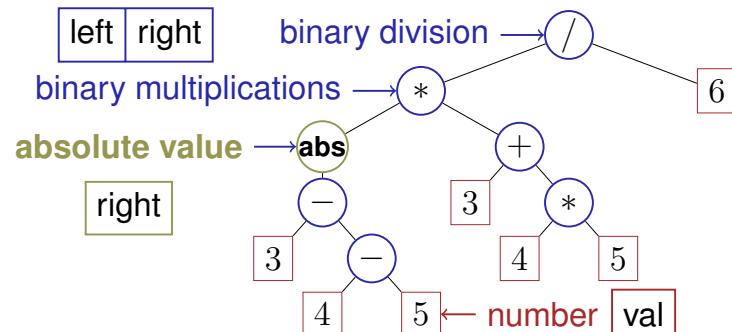
Previously



- Nodes: Forks, Leafs and Bends
- ⇒ unused member variables *

Motivation Inheritance:

The Idea



- Everywhere only the necessary member variables
- Extension of “operator zoo” with new species!

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Inheritance – The Hack, First...

Scenario: extension of the expression tree by mathematical functions `abs`, `sin`, `cos`:

- extension of the class `tree_node` by even more member variables

```
struct tree_node{
    char op; // neu: op = 'f' -> Funktion
    ...
    std::string name; // function name;
}
```

Disadvantages:

- Modification of the original code (undesirable)
- even more member variables...

Inheritance – The Hack, Second...

Scenario: extension of the expression tree by mathematical functions `abs`, `sin`, `cos`:

- Adaption of every single member function

```
double eval () const
{
    ...
    else if (op == 'f')
        if (name == "abs")
            return std::abs(right->eval());
    ...
}
```

Disadvantages:

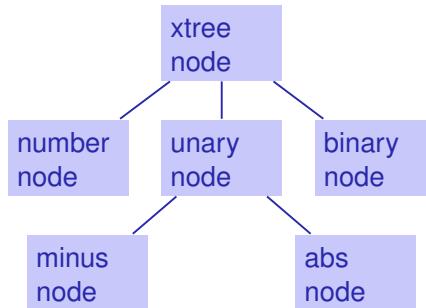
- Loss of clarity
- hard to work in a team of developers

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Inheritance – the Clean Solution

- “Split-up” of `tree_node`
- Common properties stay in the *base class* `xtree_node` (will be explained)



Inheritance

classes can *inherit* properties

```
struct xtree_node{  
    virtual int size() const;  
    virtual double eval () const;  
};  
struct number_node : public xtree_node {  
    double val;  
};  
int size () const; ← members of xtree_node  
double eval () const; ← are overwritten
```

Annotations: 'erbt von' points to the colon in the inheritance line. 'inheritance visible' points to the `xtree_node` in the base class. 'only for number_node' points to the `val` member.

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Inheritance – Notation

```
class A {  
    ...  
}  
  
class B: public A{  
    ...  
}  
  
class C: public B{  
    ...  
}
```

Base/Super Class

“B and C *inherit* from A”
“C inherits from B”

Separation of Concerns: The Number Node

```
struct number_node: public xtree_node{  
    double val;  
  
    number_node (double v) : val (v) {}  
  
    double eval () const {  
        return val;  
    }  
  
    int size () const {  
        return 1;  
    }  
};
```

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A Number Node is a Tree Node...

- A (pointer to) an inheriting object can be used where (a pointer to) a base object is required, **but not vice versa**.

```
number_node* num = new number_node (5);

xtree_node* tn = num; // ok, number_node is
                      // just a special xtree_node

xtree_node* bn = new add_node (tn, num); // ok

number_node* nn = tn; //error:invalid conversion
```

Application

```
class xexpression {
private:
    xtree_node* root; ← static type
public:
    xexpression (double d) ← dynamic type
        : root (new number_node (d)) {}

    xexpression& operator-= (const xexpression& t)
    {
        assert (t.root);
        root = new sub_node (root, t.root->copy());
        return *this;
    }
    ...
}
```

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Polymorphism

- `struct xtree_node { virtual double eval(); ... };`
- Without Virtual the *static type* determines which function is executed

We do not go into further details.

Separation of Concerns: Binary Nodes

```
struct binary_node : public xtree_node {
    xtree_node* left; // INV != 0
    xtree_node* right; // INV != 0

    binary_node (xtree_node* l, xtree_node* r) :
        left (l), right (r)
    {
        assert (left);           size works for all binary
        assert (right);          nodes. Derived classes
    }                           (add_node, sub_node...) inherit this function!
                                ←
                                int size () const { ←
                                    return 1 + left->size() + right->size();
                                }
};

};
```

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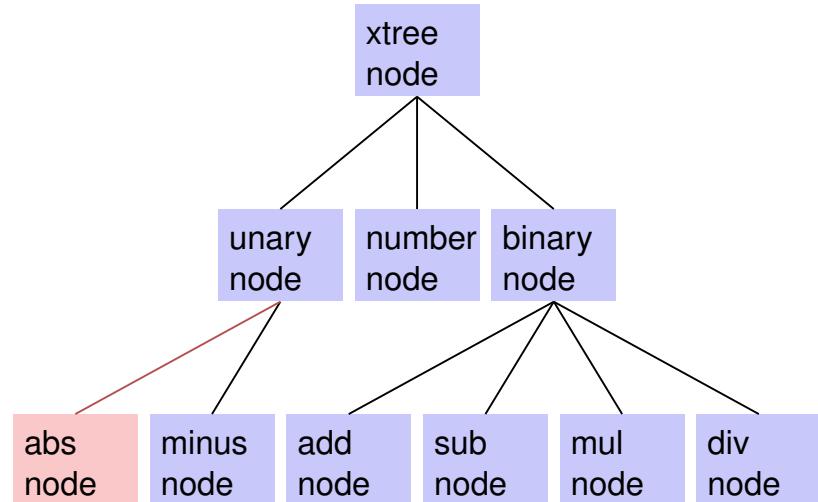
Separation of Concerns: +, -, *, ...

```
struct sub_node : public binary_node {
    sub_node (xtree_node* l, xtree_node* r)
        : binary_node (l, r) {}

    double eval () const {
        return left->eval() - right->eval();
    }
};
```

eval specific
for +, -, *, /

Extension by abs Function



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Extension by abs Function

```
struct unary_node: public xtree_node
{
    xtree_node* right; // INV != 0
    unary_node (xtree_node* r);
    int size () const;
};

struct abs_node: public unary_node
{
    abs_node (xtree_node* arg) : unary_node (arg) {}

    double eval () const {
        return std::abs (right->eval());
    }
};
```

Do not forget...

Memory Management

```
struct xtree_node {
    ...
    // POST: a copy of the subtree with root
    //        *this is made, and a pointer to
    //        its root node is returned
    virtual xtree_node* copy () const;

    // POST: all nodes in the subtree with
    //        root *this are deleted
    virtual void clear () {};
};
```

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Do not forget...

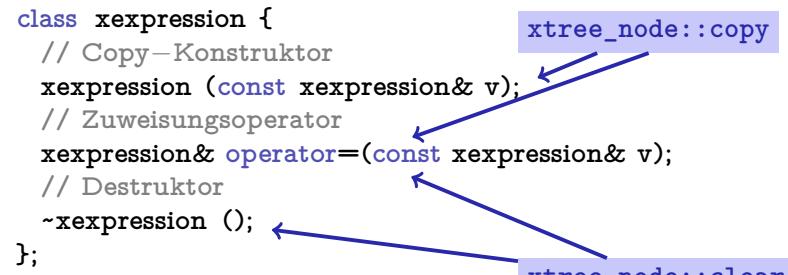
```
struct unary_node: public xtree_node {  
    ...  
    virtual void clear () {  
        right->clear();  
        delete this;  
    }  
};  
  
struct minus_node: public unary_node {  
    ...  
    xtree_node* copy () const  
    {  
        return new minus_node (right->copy());  
    }  
};
```

Memory Management

xtree_node is no dynamic data type ??

- We do not have any variables of type `xtree_node` with automatic memory lifetime
- copy constructor, assignment operator and destructor are unnecessary
- memory management in the *container class*

```
class xexpression {  
    // Copy-Konstruktor  
    xexpression (const xexpression& v);  
    // Zuweisungsoperator  
    xexpression& operator=(const xexpression& v);  
    // Destruktor  
    ~xexpression ();  
};
```

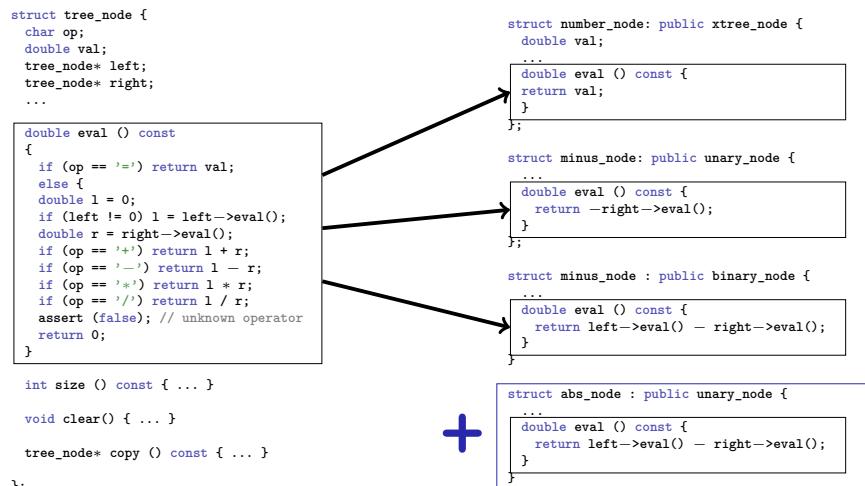


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Mission: Monolithic → Modular ✓

```
struct tree_node {  
    char op;  
    double val;  
    tree_node* left;  
    tree_node* right;  
    ...  
  
    double eval () const  
    {  
        if (op == '+') return val;  
        else {  
            double l = 0;  
            if (left != 0) l = left->eval();  
            double r = right->eval();  
            if (op == '+') return l + r;  
            if (op == '-') return l - r;  
            if (op == '*') return l * r;  
            if (op == '/') return l / r;  
            assert (false); // unknown operator  
            return 0;  
        }  
  
    int size () const { ... }  
    void clear() { ... }  
    tree_node* copy () const { ... }  
};
```



Summary of the Concepts

.. of Object Oriented Programming

Encapsulation

- hide the implementation details of types
- definition of an interface for access to values and functionality (public area)
- make possible to ensure invariants and the modification of the implementation

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Summary of Concepts

.. of Object Oriented Programming

Inheritance

- types can inherit properties of types
- inheriting types can provide new properties and overwrite existing ones
- allows to reuse code and data

Summary of Concepts

.. of Object Oriented Programming

Polymorphism

- A pointer may, depending on its use, have different underlying types
- the different underlying types can react differently on the same access to their common interface
- makes it possible to extend libraries “non invasively”