13. Pointers, Algorithms, Iterators and Containers II

Iterations with Pointers, Arrays: Indices vs. Pointers, Arrays and Functions, Pointers and const, Algorithms, Container and Iteration, Vector-Iteration, Typdef, Sets, the Concept of Iterators

Recall: Pointers running over the Array

Beispiel

int a[5] = {3, 4, 6, 1, 2};
for (int* p = a; p < a+5; ++p)
 std::cout << *p << ' '; // 3 4 6 1 2</pre>

An array can be converted into a pointer to its first element.

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- Pointers "know" arithmetics and comparisons.
- Pointers can be dereferenced.
- \Rightarrow Pointers can be used to operate on arrays.

```
Arrays and Indices
Arrays: Indices vs. Pointer
                                                                           // Set all elements to value
int a[n];
                                                                           for (int i = 0; i < n; ++i)
                                                                               a[i] = value:
// Task: set all elements to 0
                                                                           Computational costs
// Solution with indices is more readable
for (int i = 0; i < n; ++i)
    a[i] = 0;
                                                                                Adresse von a[0] = a + 0 \cdot s
                                                                                                          address of a[n-1] = a + (n-1), s
// Solution with pointers is faster and more generic
int* begin = a; // Pointer to the first element
int* end = a+n; // Pointer past the end
for (int* p = begin; p != end; ++p)
   *p = 0;
                                                                           \Rightarrow One addition and one multiplication per element
```



Reading a book with in	dices with pointers	Array Arguments: <i>Call by (const) reference</i>
 Random Access open book on page 1 close book open book on pages 2-3 close book open book on pages 4-5 close book 	 Sequential Access open book on page 1 turn the page 	<pre>void print_vector (const int (&v)[3]) { for (int i = 0; i<3 ; ++i) { std::cout << v[i] << " "; } } void make_null_vector (int (&v)[3]) { for (int i = 0; i<3 ; ++i) { v[i] = 0; } }</pre>

Array Arguments: Call by value (not really ...)

```
void make_null_vector (int v[3]) {
  for (int i = 0; i<3 ; ++i) {
    v[i] = 0;
  }
}
...
int a[10];
make_null_vector (a); // only sets a[0], a[1], a[2]
int* b;
make_null_vector (b); // no array at b, crash!</pre>
```

Array Arguments: Call by value does not exist

- Formal argument types T[n] or T[] (array over T) are equivalent to T* (pointer to T)
- For passing an array the pointer to its first element is passed
- length information is lost
- Function cannot work on a part of an array (example: search for an element in the second half of an array)

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Arrays in Functions

Covention of the standard library: pass an array (or a part of it) using two pointers

- begin: pointer to the first element
- end: pointer *behind* the last element
- [begin, end) designates the elements of the part of the array
- *valid* range means: there are array elements "available" here.
- [begin, end) is empty if begin == end

Arrays in Functions:



Pointers are not Integers!

- Addresses can be interpreted as house numbers of the memory, that is, integers
- But integer and pointer arithmetics behave differently.

ptr + 1 is *not* the next house number but the *s*-next, where *s* is the memory requirement of an object of the type behind the pointer **ptr**.

Integers and pointers are not compatible

int* ptr = 5; // error: invalid conversion from int to int* int a = ptr; // error: invalid conversion from int* to int

Null-Pointer

- special pointer value that signals that no object is pointed to
- represented b the integer number 0 (convertible to T*)

int* iptr = 0;

- cannot be dereferenced (checked during runtime)
- to avoid undefined behavior

int* iptr; // iptr points into ''nirvana''
int j = *iptr; // illegal address in *

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Pointer Subtraction

- If p1 and p2 point to elements of the same array a with length n
- and $0 \le k_1, k_2 \le n$ are the indices corresponding to *p1* and *p2*, then

```
p1 - p2 has value k_1 - k_2
```

Only valid if *p1* and p2 point into the same array.

The pointer difference describes "how far away the elements are from each other"

Pointer Operators

Description	Ор	Arity	Precedence	Associativity	Assignment
Subscript	[]	2	17	left	$\begin{array}{rr} \text{R-value} \rightarrow & \text{L-} \\ \text{value} \end{array}$
Dereference	*	1	16	right	$\begin{array}{ll} R\text{-Wert} & \rightarrow \\ L\text{-Wert} \end{array}$
Address	&	1	16	rechts	L -value \rightarrow R-value

Precedences and associativities of +, -, ++ (etc.) like in chapter 2

Mutating Functions



Const Correctness

There are also non-mutating functions that access elements of an array only in a read-only fashion

```
// PRE: [begin , end) is a valid and nonempty range
// POST: the smallest value in [begin, end) is returned
int min (const int* begin ,const int* end)
{
    assert (begin != end);
    int m = *begin; // current minimum candidate
    for (const int* p = ++begin; p != end; ++p)
        if (*p < m) m = *p;
    return m;
}</pre>
```

mark with const: value of objects cannot be modified through such const-pointers.

const is not absolute

The value at an address can change even if a const-pointer stores this address.

beispiel

```
int a[5];
const int* begin1 = a;
int* begin2 = a;
*begin1 = 1; // error *begin1 is constt
*begin2 = 1; // ok, although *begin will be modified
```

const is a promise from the point of view of the const-pointer, not an absolute guarantee

Wow – Palindromes!

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```
// PRE: [begin end) is a valid range of characters
// POST: returns true if the range forms a palindrome
bool is_palindrome (const char* begin, const char* end) {
   while (begin < end)
      if (*(begin++) != *(--end)) return false;
   return true;
}
begin end
</pre>
```

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Algorithms

For many problems there are prebuilt solutions in the standard library

Example: filling an array



Algorithms

Advantages of using the standard library

- simple programs
- less sources of errors
- good, efficient code
- code independent from the data type
- there are also algorithms for more complicated problems such as the efficient sorting of an array

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Algorithms

The same prebuilt algorithms work for many different data types.

Example: filling an array

```
#include <algorithm> // needed for std::fill
...
char c[3];
std::fill (c, c+3, "!");
for (int i=0; i<3; ++i)
    std::cout << c[i]; // !!!</pre>
```

Excursion: Templates

- Templates permit the provision of a type as argument
- The compiler finds the matching type from the call arguments

Example fill with templates template <typename T> void fill(T* begin 1 T* end, T value) { for (T* p = begin, p != end; ++p) *p = value; } int a[5]; fill (a, a+5, 1); // 1 1 1 1 1 char c[3]; fill (c, c+3, '!'); // !!! The triangular brackets we already know from vectors. Vectors are also implemented as templates.

std::fill is also implemented as template!

Containers and Traversal

- **Container:** Container (Array, Vector, ...) for elements
- Traversal: Going over all elements of a container
 - Initialization of all elements (fill)
 - Find the smallest element (min)
 - Check properties (is_palindrome)
 - ••••
- There are a lot of different containers (sets, lists, ...)

Iteration Tools

- Arrays: indices (random access) or pointers (natural)
- Array algorithms (std::) use pointers

int a[5]; std::fill (a, a+5, 1); // 1 1 1 1 1

How do you traverse vectors and other containers?

std::vector<int> v (5, 0); // 0 0 0 0 0
std::fill (?, ?, 1); // 1 1 1 1 1

Vectors: too sexy for pointers

- Our fill with templates does not work for vectors...
- ... and std::fill also does not work in the following way:

```
std::vector<int> v (5, 0);
std::fill (v, v+5, 1); // Compiler error message !
```

Vectors are snobby...

- they refuse to be converted to pointers,...
- ... and cannot be traversed using pointers either.
- They consider this far too primitive.

Also in memory: Vector \neq Array

bool a[8] = {true, true, true, true, true, true, true};



std::vector<bool> v (8, true);



bool*-pointer does not fit here because it runs byte-wise and not bit-wise

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Vector-Iterators

Iterator: a "pointer" that fits to the container.

Example: fill a vector using std::fill - this works

```
#include <vector>
#include <algorithm> // needed for std::fill
...
std::vector<int> v(5, 0);
std::fill (v.begin(), v.end(), 1);
for (int i=0; i<5; ++i)
    std::cout << v[i] << " "; // 1 1 1 1 1</pre>
```

Vector Iterators

For each vector there are two iterator types defined

- std::vector<int>::const_iterator
 - for non-mutating access
 - in analogy with const int* for arrays

std::vector<int>::iterator

- for mutating access
- in analogy with int* for arrays

A vector-iterator it is no pointer, but it behaves like a pointer:

- it points to a vector element and can be dereferenced (*it)
- it knows arithmetics and comparisons (++it, it+2, it < end,...)

Vector-Iterators: begin() and end()

- v.begin() points to the first element of v
- v.end() points past the last element of v
- We can traverse a vector using the iterator...

... or fill a vector.

```
std::fill (v.begin(), v.end(), 1);
```

Type names in C++ can become loooooong

std::vector<int>::const_iterator

■ The declaration of a *type alias* helps with



typedef std::vector<int> int_vec; typedef int_vec::const_iterator Cvit;



Other Containers: Sets Sets: Example Application

A set is an unordered collection of elements, where each element is contained only once.

 $\{1, 2, 1\} = \{1, 2\} = \{2, 1\}$

■ C++: std::set<T> for a set with elements of type T

Determine if a given text contains a question mark and output all pairwise different characters!

Letter Salad (1)

Consider a text as a set of characters.

#include<set>

```
typedef std::set<char>::const_iterator Csit;
...
std::string text =
"What are the distinct characters in this string?";
std::set<char> s (text.begin(),text.end());
```

Set is initialized with String iterator range
[text.begin(), text.end())

Letter Salad (2)

Determine if the text contains a question mark and output all characters

Search algorithm, can be called with arbitrary iterator range

// check whether text contains a question mark
if (std::find (s.begin(), s.end(), '?') != s.end())
 std::cout << "Good question!\n";</pre>

```
// output all distinct characters
for (Csit it = s.begin(); it != s.end(); ++it)
    std::cout << *it;
    Ausgabe:</pre>
```

Good question! ?Wacdeghinrst

Sets and Indices?

Can you traverse a set using random access? No.

for (int i=0; i<s.size(); ++i)
 std::cout << s[i];</pre>

error message: no subscript operator

- Sets are unordered.
 - There is no "*i*th element".
 - Iterator comparison it != s.end() works, but not it < s.end()!</pre>

- The Concept of Iterators
- C++knows different iterator types
- Each container provides an associated iterator type.
- All iterators can dereference (*it) and traverse (++it)
- Some can do more, e.g. random access (it[k], or, equivalently *(it + k)), traverse backwards (--it),...

The Concept of Iterators

Every container algorithm is generic, that means:

- The container is passed as an iterator-range
- The algorithm works for all containers that fulfil the requirements of the algorithm
- std::find only requires * and ++ , for instance
- The implementation details of a container are irrelevant.

Why Pointers and Iterators?

Would you not prefer the code

```
for (int i=0; i<n; ++i)
        a[i] = 0;</pre>
```

over the following code?

```
for (int* ptr=a; ptr<a+n; ++ptr)
    *ptr = 0;</pre>
```

Maybe, but in order to use the generic std::fill(a, a+n, 0);, we *have to* work with pointers.

 Why Pointers and Iterators?

 Why Pointers and Iterators?

 Example: To search the smallest element of a container in the range

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In order to use the standard library, we have to know that:

- a static array a is a the same time a pointer to the first element of a
- a+i is a pointer to the element with index i

Using the standard library with different containers: Pointers \Rightarrow Iterators

Example: To search the smallest element of a container in the range [begin, end) use the function call

```
std::min_element(begin, end)
```

- returns an *iterator* to the smallest element
- To read the smallest element, we need to dereference:

*std::min_element(begin, end)

That is Why: Pointers and Iterators

- Even for non-programmers and "dumb" users of the standard library: expressions of the form
 *std::min_element(begin, end) cannot be understood without knowing pointers and iterators.
- Behind the scenes of the standard library: working with dynamic memory based on pointers is indispensible. More about this later in this course.

14. Recursion 1

Mathematical Recursion, Termination, Call Stack, Examples, Recursion vs. Iteration

Mathematical Recursion

Recursion in C++: In the same Way!

$$n! = \begin{cases} 1, & \text{if } n \le 1\\ n \cdot (n-1)!, & \text{otherwise} \end{cases}$$

- Many mathematical functions can be naturally defined recursively.
- This means, the function appears in its own definition

$$n! = \begin{cases} 1, & \text{if } n \le 1\\ n \cdot (n-1)!, & \text{otherwise} \end{cases}$$

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Infinite Recursion

Recursive Functions: Termination

- is as bad as an infinite loop...
- ... but even worse: it burns time and memory

recursive call with argument n-1 == 3

void f() { f(); // $f() \rightarrow f() \rightarrow \dots$ stack overflow }

- As with loops we need
- progress towards termination

fac(n):

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terminates immediately for $n \leq 1$, otherwise the function is called recusively with < n.

"n is getting smaller for each call."

Recursive Functions: Evaluation The Call Stack Example: fac(4) n = 1fac(1)// POST: return value is n! For each function call: n=2unsigned int fac (unsigned int n) push value of the call argument onto ſ fac(2)the stack if $(n \le 1)$ return 1; n = 3return n * fac(n-1); // n > 1always work with the top value fac(3)} at the end of the call the top value is n=4removed from the stack fac(4)std:cout << fac(4)</pre> Initialization of the formal argument: n = 4

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1! = 1

1

 $2 \cdot 1! = 2$

2

 $3 \cdot 2! = 6$

6

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 $4 \cdot 3! = 24$

Euclidean Algorithm

- finds the greatest common divisor gcd(a, b) of two natural numbers a and b
- is based on the following mathematical recursion (proof in the lecture notes):

$$gcd(a,b) = \begin{cases} a, & \text{if } b = 0\\ gcd(b, a \mod b), & \text{otherwise} \end{cases}$$

Euclidean Algorithm in C++

$$gcd(a, b) = \begin{cases} a, & \text{if } b = 0\\ gcd(b, a \mod b), & \text{otherwise} \end{cases}$$

unsigned int gcd
(unsigned int a, unsigned int b)
{
if (b == 0)
return a;
else
return gcd (b, a % b);
}

Fibonacci Numbers

$$F_n := \begin{cases} 0, & \text{if } n = 0\\ 1, & \text{if } n = 1\\ F_{n-1} + F_{n-2}, & \text{if } n > 1 \end{cases}$$

 $0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89 \dots$

Fibonacci Numbers in C++

Laufzeit

fib(50) takes "forever" because it computes F_{48} two times, F_{47} 3 times, F_{46} 5 times, F_{45} 8 times, F_{44} 13 times, F_{43} 21 times ... F_1 ca. 10^9 times (!)

```
unsigned int fib (unsigned int n)
{
    Correctness
    if (n == 0) return 0;
        if (n == 1) return 1;
        return fib (n-1) + fib (n-2); // n > 1
        are clear.
}
```

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Fast Fibonacci Numbers

Idea:

- Compute each Fibonacci number only once, in the order $F_0, F_1, F_2, \ldots, F_n!$
- Memorize the most recent two numbers (variables a and b)!
- Compute the next number as a sum of a and b!

Fast Fibonacci Numbers in C++



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Recursion and Iteration

Recursion can always be simulated by

- Iteration (loops)
- explicit "call stack" (e.g. array)

Often recursive formulations are simpler, but sometimes also less efficient.