

Exercise 1

Exercise 1

Find **PRE-** and **POST-**conditions for this function.

1. Function:

```
double f (double i,  
          double j,  
          double k)  
{  
    if (i > j)  
        if (i > k)  
            return i;  
        else  
            return k;  
    else  
        if (j > k)  
            return j;  
        else  
            return k;  
}
```

Exercise 1

PRE-Condition:

(not needed)

POST-Condition:

```
// POST: return value is
//       the maximum of
//       i, j and k
```

1. Function:

```
double f (double i,
          double j,
          double k)
{
    if (i > j)
        if (i > k)
            return i;
        else
            return k;
    else
        if (j > k)
            return j;
        else
            return k;
}
```

Exercise 1

Find **PRE-** and **POST-conditions** for this function.

2. Function:

```
double g (int i, int j)
{
    double r = 0.0;
    for (int k = i; k <= j; ++k)
        r += 1.0 / k;
    return r;
}
```

Exercise 1

2. Function:

```
double g (int i, int j)
{
    double r = 0.0;
    for (int k = i; k <= j; ++k)
        r += 1.0 / k;
    return r;
}
```

```
PRE-Condition:    // PRE: 0 not contained in {i, ..., j}
POST-Condition:   // POST: return value is the sum
                  //          1/i + 1/(i+1) + ... + 1/j
```

Exercise 2

Exercise 2

- Fix the **problems** in the following functions.
- Then add suitable **PRE- and POST-conditions**.

1. Function:

```
bool is_even (int i)
{
    if (i % 2 == 0) return true;
}
```

Exercise 2

- Problem: just a **return value** for even inputs

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bool is_even (int i)
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Exercise 2

- Problem: just a **return value** for even inputs
- Fix: e.g. **direct return** of `i % 2 == 0`

1. Function:

```
bool is_even (int i)
{
    if (i % 2 == 0) return true;
}
```



```
bool is_even (int i)
{
    return (i % 2 == 0);
}
```

Exercise 2

- Problem: just a **return value** for even inputs
- Fix: e.g. **direct return** of `i % 2 == 0`

1. Function:

```
bool is_even (int i)
{
    if (i % 2 == 0) return true;
}
```



```
bool is_even (int i)
{
    return (i % 2 == 0);
}
```

PRE-Condition: (not needed)

POST-Condition: `// POST: return value is true if and only`
`// if i is even`

Exercise 2

- Fix the **problems** in the following functions.
- Then add suitable **PRE- and POST-conditions**.

2. Function:

```
double inverse (double x) {  
    double result;  
    if (x != 0.0)  
        result = 1.0 / x;  
    return result;  
}
```

Exercise 2

- Problem: no return value for $x=0$

2. Function:

```
double inverse (double x) {  
    double result;  
    if (x != 0.0)  
        result = 1.0 / x;  
    return result;  
}
```

Exercise 2

- Problem: no return value for $x=0$
- Fix: $x \neq 0.0$ as PRE-condition (and `assert`)

2. Function:

```
double inverse (double x) {  
    double result;  
    if (x != 0.0)  
        result = 1.0 / x;  
    return result;  
}
```



```
// PRE: x != 0.0  
// POST: ...  
double inverse (double x) {  
    assert(x != 0.0);  
    return 1.0 / x;  
}
```

Exercise 2

- Problem: no return value for $x=0$
- Fix: $x \neq 0.0$ as PRE-condition (and `assert`)

2. Function:

```
double inverse (double x) {  
    double result;  
    if (x != 0.0)  
        result = 1.0 / x;  
    return result;  
}
```



```
// PRE: x != 0.0  
// POST: ...  
double inverse (double x) {  
    assert(x != 0.0);  
    return 1.0 / x;  
}
```

```
PRE-Condition:    // PRE: x != 0.0  
POST-Condition:  // POST: return value is 1/x
```

Exercise 2

Another solution:

Exercise 2

Another solution:

`else` with special return value

```
double inverse (double x)
{
    double result;
    if (x != 0.0)
        result = 1.0 / x;
    else
        result = 0.0;
    return result;
}
```


Exercise 2

Another solution:

`else` with special return value

```
double inverse (double x)
{
    double result;
    if (x != 0.0)
        result = 1.0 / x;
    else
        result = 0.0;
    return result;
}
```

PRE-Condition: (not needed)

POST-Condition: // POST: return value is $1/x$ if $x \neq 0.0$
// return value is 0.0 else

Exercise 3

Exercise 3

- What is the **output** of this program?
- You can neglect possible over- or underflows for this exercise.

```
#include <iostream>

int f (int i) {
    return i * i;
}

int g (int i) {
    return i * f(i) * f(f(i));
}

void h (int i) {
    std::cout << g(i) << "\n";
}

int main () {
    int i;
    std::cin >> i;
    h(i);
    return 0;
}
```

Exercise 3

```
i * f(i) * f(f(i))
```

```
#include <iostream>

int f (int i) {
    return i * i;
}

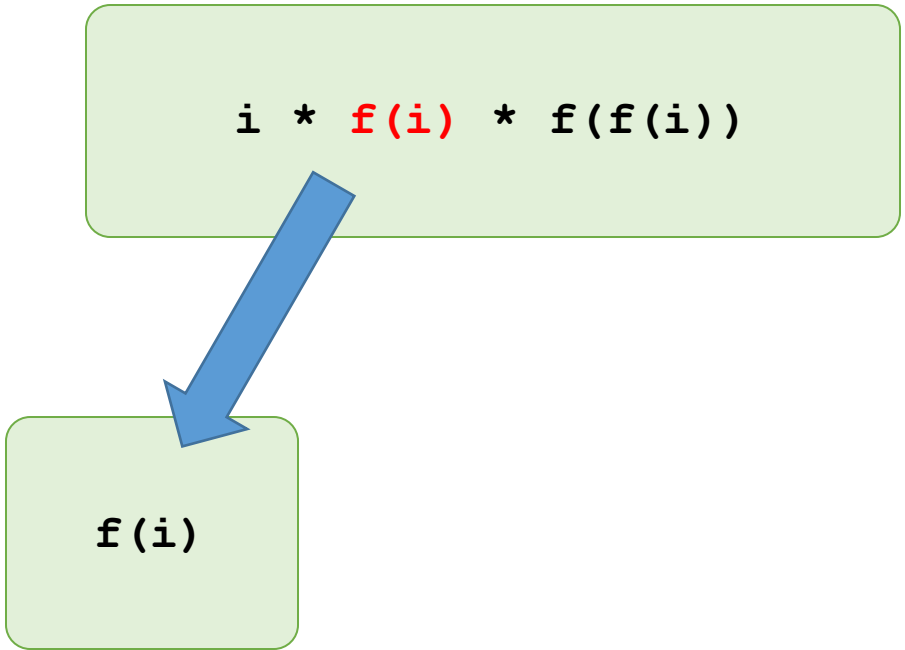
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void h (int i) {
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int main () {
    int i;
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    return 0;
}
```

Exercise 3

`i * f(i) * f(f(i))`



`f(i)`

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#include <iostream>

int f (int i) {
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int main () {
    int i;
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Exercise 3

`i * f(i) * f(f(i))`



`i*i`

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int main () {
    int i;
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    h(i);
    return 0;
}
```

Exercise 3

`i * (i*i) * f(f(i))`

`i*i`



```
#include <iostream>

int f (int i) {
    return i * i;
}

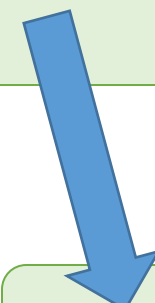
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}

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    std::cout << g(i) << "\n";
}

int main () {
    int i;
    std::cin >> i;
    h(i);
    return 0;
}
```

Exercise 3

```
i * (i*i) * f(f(i))
```



```
f(f(i))
```

```
#include <iostream>

int f (int i) {
    return i * i;
}

int g (int i) {
    return i * f(i) * f(f(i));
}

void h (int i) {
    std::cout << g(i) << "\n";
}

int main () {
    int i;
    std::cin >> i;
    h(i);
    return 0;
}
```


Exercise 3

```
i * (i*i) * f(f(i))
```



```
f(f(i))
```

```
f(i)
```

```
#include <iostream>

int f (int i) {
    return i * i;
}

int g (int i) {
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void h (int i) {
    std::cout << g(i) << "\n";
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    return 0;
}
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Exercise 3

```
i * (i*i) * f(f(i))
```



```
f(f(i))
```

```
i*i
```

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Exercise 3

```
i * (i*i) * f(f(i))
```



```
f(i*i)
```

```
i*i
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    std::cin >> i;
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Exercise 3

```
i * (i*i) * f(f(i))
```



```
(i*i) * (i*i)
```

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    h(i);
    return 0;
}
```

Exercise 3

```
i * (i*i) * ((i*i)*(i*i))
```

```
(i*i)*(i*i)
```



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int g (int i) {
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Exercise 3

```
i * (i*i) * ((i*i)*(i*i))
```

This is
 i^7

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