

# Informatik II

## Übung 8

FS 2020

# Program Today

- 1 Repetition Lectures: Graph representation
- 2 Breadth-First-Search BFS
- 3 In-Class-Exercise

# Quiz: Runtimes of simple Operations

| Operation                                  | Matrix | List |
|--|--------|------|
| Find neighbours/successors of $v \in V$    |        |      |
| find $v \in V$ without neighbour/successor |        |      |
| $(u, v) \in E ?$                           |        |      |
| Insert edge                                |        |      |
| Delete edge                                |        |      |

# Quiz: Runtimes of simple Operations

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| Find neighbours/successors of $v \in V$    | $\Theta(n)$ |      |
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| Find neighbours/successors of $v \in V$    | $\Theta(n)$ | $\Theta(\deg^+ v)$ |
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| Insert edge                                | $\Theta(1)$   | $\Theta(1)$        |
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# Quiz: Runtimes of simple Operations

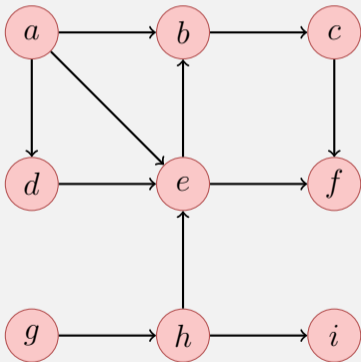
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| Delete edge                                | $\Theta(1)$   | $\Theta(\deg^+ v)$ |

# Breadth-First-Search BFS

BFS starting from  $a$ :



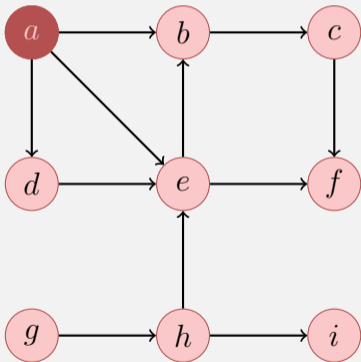
BFS-Tree: Distances and Parents



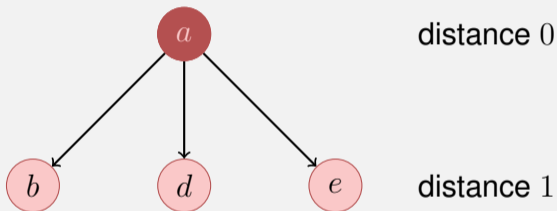
distance 0

# Breadth-First-Search BFS

BFS starting from  $a$ :

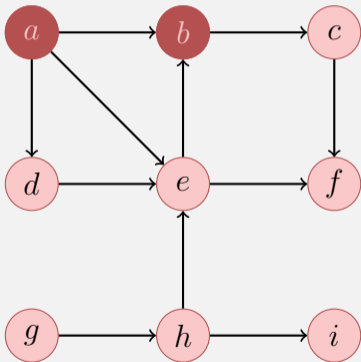


BFS-Tree: Distances and Parents

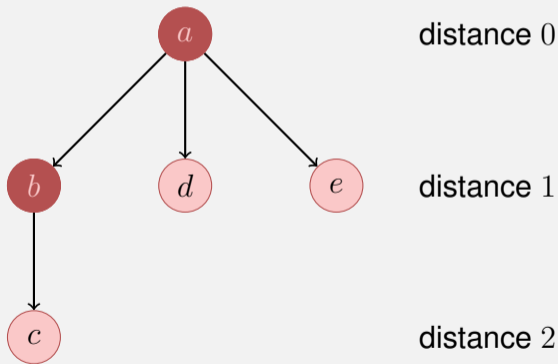


# Breadth-First-Search BFS

BFS starting from  $a$ :



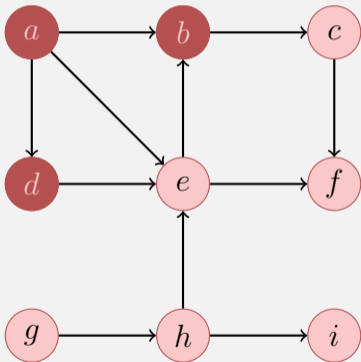
BFS-Tree: Distances and Parents



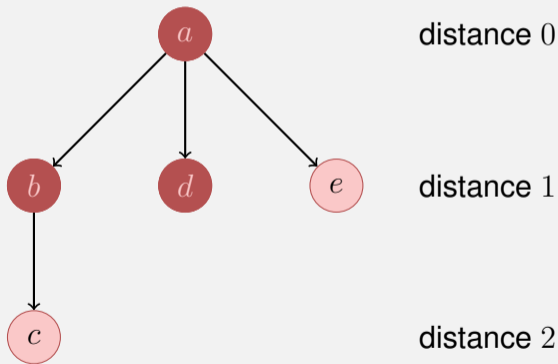


# Breadth-First-Search BFS

BFS starting from  $a$ :

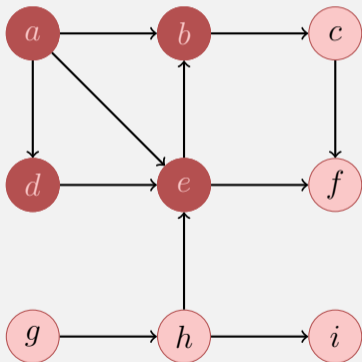


BFS-Tree: Distances and Parents

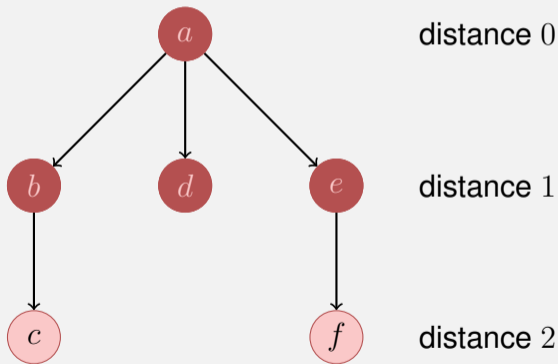


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BFS starting from  $a$ :

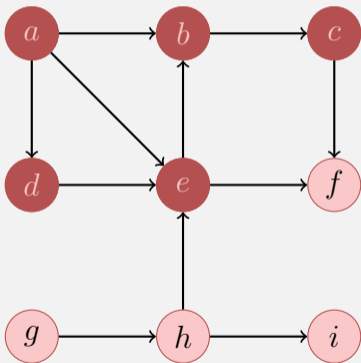


BFS-Tree: Distances and Parents

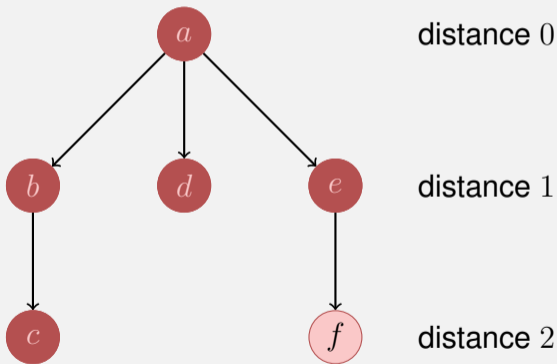


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BFS starting from  $a$ :

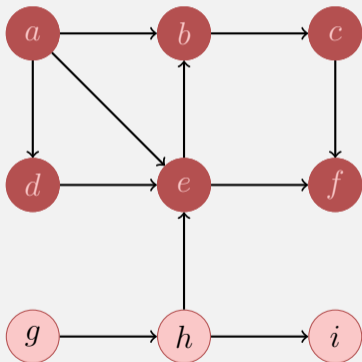


BFS-Tree: Distances and Parents

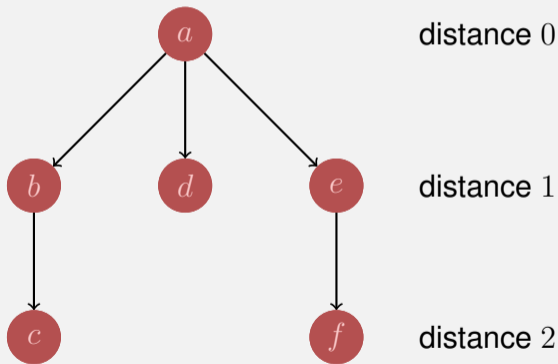


# Breadth-First-Search BFS

BFS starting from  $a$ :

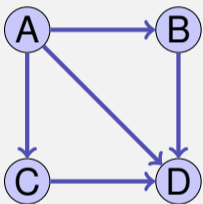


BFS-Tree: Distances and Parents



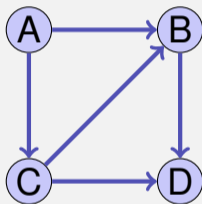
# Quiz: Topological Sorting

In how many ways can the following directed graphs be topologically sorted each?



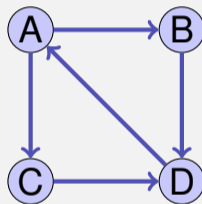
number sortings

?



number sortings

?

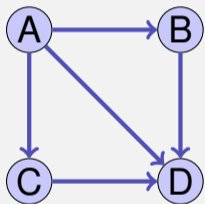


number sortings

?

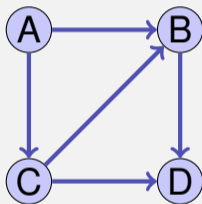
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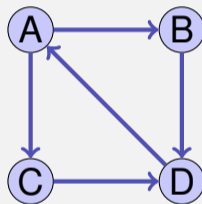
number sortings

2



number sortings

1



number sortings

0

# Graph Visualisation

Implement a function to visualize a graph that is given in the form of an adjacency matrix

The visualization of a graph that is given as an adjacency list is already provided.

Questions / Suggestions?