

Informatik II

Übung 3

FS 2019

Program Today

1 Feedback of last exercise

2 Python Short Exercises

Throwing eggs

- What would be your strategy if you would have an arbitrary number of eggs?

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 - Binary search. Worst case: $\log_2 n$ tries.
- What would you do if you only had one egg?
 - Start from the bottom. n tries.

Throwing Eggs

Strategy using two eggs

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Minimize maximum number of trials:

$$f'(k) = 1 - n/k^2 = 0 \Rightarrow k = \sqrt{n}.$$

$$n = 100 \Rightarrow 19 \text{ Trials. } \Theta(\sqrt{n})$$

- Second approach: take first throw trial into account by considering decreasing interval sizes. Choose smallest s such that $s + s - 1 + s - 2 + \dots + 1 = s(s + 1)/2 \geq 100 \Rightarrow s = 14$.

Maximum number of trials: $s \in \Theta(\sqrt{n})$

Asymptotically both approaches are equally good. Practically the second way is better.

Hottest Path

```
int current = 0;
List<Integer> route = new ArrayList<Integer>();
route.add(0);
while (!food[current]) { // termination criterion
    float max = -1;
    int next = -1;
    for (int j = 0; j < edges.length; ++j) {
        if (edges[current][j] != 0 && max < popularity[current][j]) {
            max = popularity[current][j];
            next = j;
        }
    }
    route.add(next);
    current = next;
}
```

Quiz

Consider the following three sequences of snap-shots (steps) of the algorithms (a) Insertion Sort, (b) Selection Sort and (c) Bubblesort. Below each sequence provide the corresponding algorithm name.

5	4	1	3	2
<hr/>				
1	4	5	3	2
<hr/>				
1	2	5	3	4
<hr/>				
1	2	3	5	4
<hr/>				
1	2	3	4	5

5	4	1	3	2
<hr/>				
4	1	3	2	5
<hr/>				
1	3	2	4	5
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selection

5	4	1	3	2
<hr/>				
4	1	3	2	5
<hr/>				
1	3	2	4	5
<hr/>				
1	2	3	4	5

bubblesort

5	4	1	3	2
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1	3	4	5	2
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insertion

Quiz

Execute two further iterations of the algorithm Quicksort on the following array.
The first element of the (sub-)array serves as the pivot.

8	7	10	15	3	6	9	5	2	13
2	7	5	6	3	<u>8</u>	9	15	10	13

Quiz

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<u>2</u>	7	5	6	3	<u>8</u>	<u>9</u>	15	10	13
<u>2</u>	3	5	6	<u>7</u>	<u>8</u>	<u>9</u>	13	10	<u>15</u>

2. Python Short Exercises

Questions / Suggestions?