

6. C++ advanced (I)

Repetition: vectors, pointers and iterators, range for, keyword auto, a class for vectors, subscript-operator, move-construction, iterators

We look back...

```
#include <iostream>
#include <vector>

int main(){
    // Vector of length 10
    std::vector<int> v(10,0);
    // Input
    for (int i = 0; i < v.length(); ++i)
        std::cin >> v[i];
    // Output
    for (std::vector::iterator it = v.begin(); it != v.end(); ++it)
        std::cout << *it << " ";
}
```

We want to understand this in depth!

At least this is too pedestrian

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Useful tools (1): auto (C++11)

The keyword `auto`:

The type of a variable is inferred from the initializer.

Examples

```
int x = 10;
auto y = x; // int
auto z = 3; // int
std::vector<double> v(5);
auto i = v[3]; // double
```

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Etwas besser...

```
#include <iostream>
#include <vector>

int main(){
    std::vector<int> v(10,0); // Vector of length 10

    for (int i = 0; i < v.length(); ++i)
        std::cin >> v[i];

    for (auto it = v.begin(); it != v.end(); ++it){
        std::cout << *it << " ";
    }
}
```

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Useful tools (2): range for (C++11)

```
for (range-declaration : range-expression)
    statement;
```

range-declaration: named variable of element type specified via the sequence in range-expression

range-expression: Expression that represents a sequence of elements via iterator pair `begin()`, `end()` or in the form of an initializer list.

Examples

```
std::vector<double> v(5);
for (double x: v) std::cout << x; // 00000
for (int x: {1,2,5}) std::cout << x; // 125
for (double& x: v) x=5;
```

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That is indeed cool!

```
#include <iostream>
#include <vector>

int main(){
    std::vector<int> v(10,0); // Vector of length 10

    for (auto& x: v)
        std::cin >> x;

    for (const auto i: x)
        std::cout << i << " ";
}
```

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For our detailed understanding

We build a vector class with the same capabilities ourselves!

On the way we learn about

- RAII (Resource Acquisition is Initialization) and move construction
- Index operators and other utilities
- Templates
- Exception Handling
- Functors and lambda expressions

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A class for vectors

```
class vector{
    int size;
    double* elem;
public:
    // constructors
    vector(): size{0}, elem{nullptr} {};

    vector(int s):size{s}, elem{new double[s]} {}
    // destructor
    ~vector(){
        delete[] elem;
    }
    // something is missing here
}
```

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Element access

```
class vector{
    ...
    // getter. pre: 0 <= i < size;
    double get(int i) const{
        return elem[i];
    }
    // setter. pre: 0 <= i < size;
    void set(int i, double d){ // setter
        elem[i] = d;
    }
    // length property
    int length() const {
        return size;
    }
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    double get(int i) const;
    void set(int i, double d);
    int length() const;
}
```

What's the problem here?

```
int main(){
    vector v(32);
    for (int i = 0; i<v.length(); ++i)
        v.set(i,i);
    vector w = v;
    for (int i = 0; i<w.length(); ++i)
        w.set(i,i*i);
    return 0;
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    double get(int i);
    void set(int i, double d);
    int length() const;
}
```

```
*** Error in 'vector1': double free or corruption
(!prev): 0x000000000d23c20 ***
===== Backtrace: =====
/lib/x86_64-linux-gnu/libc.so.6(+0x777e5) [0x7fe5a5ac97e5]
```

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Rule of Three!

```
class vector{
    ...
public:
    // Copy constructor
    vector(const vector &v):
        size{v.size}, elem{new double[v.size]} {
        std::copy(v.elem, v.elem+v.size, elem);
    }
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    vector(const vector &v);
    double get(int i);
    void set(int i, double d);
    int length() const;
}
```

Rule of Three!

```
class vector{
    ...
    // Assignment operator
    vector& operator=(const vector&v){
        if (v.elem == elem) return *this;
        if (elem != nullptr) delete[] elem;
        size = v.size;
        elem = new double[size];
        std::copy(v.elem, v.elem+v.size, elem);
        return *this;
    }
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    vector(const vector &v);
    vector& operator=(const vector&v);
    double get(int i);
    void set(int i, double d);
    int length() const;
}
```

Now it is correct, but cumbersome.

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More elegant this way:

```
class vector{
...
// Assignment operator
vector& operator= (const vector&v){
    vector cpy(v);
    swap(cpy);
    return *this;
}
private:
// helper function
void swap(vector& v){
    std::swap(size, v.size);
    std::swap(elem, v.elem);
}
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    vector(const vector &v);
    vector& operator=(const vector&v);
    double get(int i);
    void set(int i, double d);
    int length() const;
}
```

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Syntactic sugar.

Getters and setters are poor. We want an index operator.

Overloading! So?

```
class vector{
...
    double operator[] (int pos) const{
        return elem[pos];
    }
    void operator[] (int pos, double value){
        elem[pos] = value;
    }
}
```

Nein!

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Reference types!

```
class vector{
...
// for const objects
double operator[] (int pos) const{
    return elem[pos];
}
// for non-const objects
double& operator[] (int pos){
    return elem[pos]; // return by reference!
}
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    vector(const vector &v);
    vector& operator=(const vector&v);
    double operator[] (int pos) const;
    double& operator[] (int pos);
    int length() const;
}
```

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So far so good.

```
int main(){
    vector v(32); // Constructor
    for (int i = 0; i<v.length(); ++i)
        v[i] = i; // Index-Operator (Referenz!)

    vector w = v; // Copy Constructor
    for (int i = 0; i<w.length(); ++i)
        w[i] = i*i;

    const auto u = w;
    for (int i = 0; i<u.length(); ++i)
        std::cout << v[i] << ":" << u[i] << " "; // 0:0 1:1 2:4 ...
    return 0;
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    vector(const vector &v);
    vector& operator=(const vector&v);
    double operator[] (int pos) const;
    double& operator[] (int pos);
    int length() const;
}
```

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Number copies

How often is `v` being copied?

```
vector operator+ (const vector& l, double r){
    vector result (l); // Kopie von l nach result
    for (int i = 0; i < l.length(); ++i) result[i] = l[i] + r;
    return result; // Dekonstruktion von result nach Zuweisung
}

int main(){
    vector v(16); // allocation of elems[16]
    v = v + 1; // copy when assigned!
    return 0; // deconstruction of v
}
```

`v` is copied twice

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Move construction and move assignment

```
class vector{
...
    // move constructor
    vector (vector&& v){
        swap(v);
    };
    // move assignment
    vector& operator=(vector&& v){
        swap(v);
        return *this;
    };
};
```

```
class vector{
public:
    vector ();
    vector(int s);
    ~vector ();
    vector(const vector &v);
    vector& operator=(const vector&v);
    vector (vector&& v);
    vector& operator=(vector&& v);
    double operator[] (int pos) const;
    double& operator[] (int pos);
    int length() const;
};
```

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Explanation

When the source object of an assignment will not continue existing after an assignment the compiler can use the move assignment instead of the assignment operator.³ A potentially expensive copy operations is avoided this way.

Number of copies in the previous example goes down to 1.

³Analogously so for the copy-constructor and the move constructor

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Range for

We wanted this:

```
vector v = ...;
for (auto x: v)
    std::cout << x << " ";
```

In order to support this, an iterator must be provided via `begin` and `end`.

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Iterator for the vector

```
class vector{
...
    // Iterator
    double* begin(){
        return elem;
    }
    double* end(){
        return elem+size;
    }
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    vector(const vector &v);
    vector& operator=(const vector&v);
    vector(vector&& v);
    vector& operator=(vector&& v);
    double operator[] (int pos) const;
    double& operator[] (int pos);
    int length() const;
    double* begin();
    double* end();
}
```

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Const Iterator for the vector

```
class vector{
...
    // Const-Iterator
    const double* begin() const{
        return elem;
    }
    const double* end() const{
        return elem+size;
    }
}
```

```
class vector{
public:
    vector();
    vector(int s);
    ~vector();
    vector(const vector &v);
    vector& operator=(const vector&v);
    vector(vector&& v);
    vector& operator=(vector&& v);
    double operator[] (int pos) const;
    double& operator[] (int pos);
    int length() const;
    double* begin();
    double* end();
    const double* begin() const;
    const double* end() const;
}
```

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Intermediate result

```
vector Natural(int from, int to){
    vector v(to-from+1);
    for (auto& x: v) x = from++;
    return v;
}
```

```
int main(){
    vector v = Natural(5,12);
    for (auto x: v)
        std::cout << x << " "; // 5 6 7 8 9 10 11 12
    std::cout << "\n";
    std::cout << "sum="
        << std::accumulate(v.begin(), v.end(),0); // sum = 68
    return 0;
}
```

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Useful tools (3): using (C++11)

`using` replaces in C++11 the old `typedef`.

```
using identifier = type-id;
```

Beispiel

```
using element_t = double;
class vector{
    std::size_t size;
    element_t* elem;
...
}
```

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7. Sorting I

Simple Sorting

7.1 Simple Sorting

Selection Sort, Insertion Sort, Bubblesort [Ottman/Widmayer, Kap. 2.1, Cormen et al, Kap. 2.1, 2.2, Exercise 2.2-2, Problem 2-2

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Problem

Input: An array $A = (A[1], \dots, A[n])$ with length n .

Output: a permutation A' of A , that is sorted: $A'[i] \leq A'[j]$ for all $1 \leq i \leq j \leq n$.

Algorithm: IsSorted(A)

Input : Array $A = (A[1], \dots, A[n])$ with length n .

Output : Boolean decision “sorted” or “not sorted”

```
for  $i \leftarrow 1$  to  $n - 1$  do
  if  $A[i] > A[i + 1]$  then
    return “not sorted”;
return “sorted”;
```

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Observation

IsSorted(A): "not sorted", if $A[i] > A[i + 1]$ for an i .

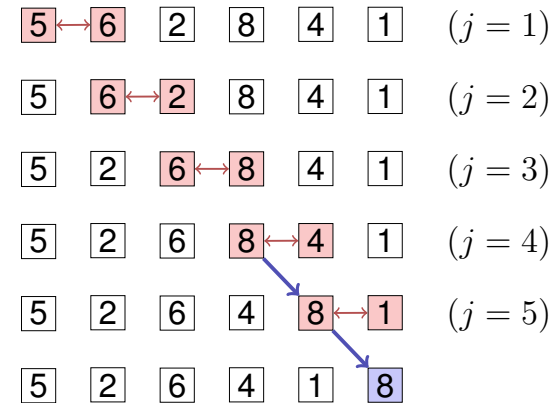
⇒ idea:

for $j \leftarrow 1$ to $n - 1$ do

```

    if  $A[j] > A[j + 1]$  then
        swap( $A[j], A[j + 1]$ );
    
```

Give it a try

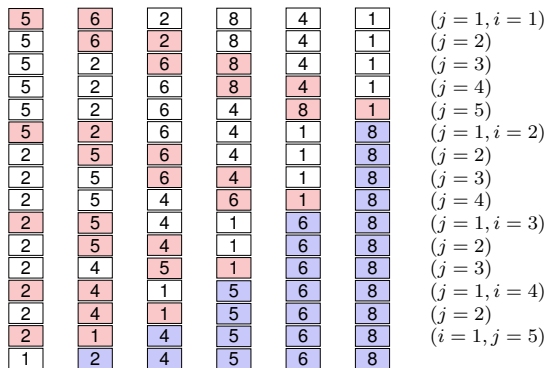


- Not sorted! 😞.
- But the greatest element moves to the right ⇒ new idea! 😊

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Try it out



- Apply the procedure iteratively.
- For $A[1, \dots, n]$, then $A[1, \dots, n - 1]$, then $A[1, \dots, n - 2]$, etc.

Algorithm: Bubblesort

Input : Array $A = (A[1], \dots, A[n])$, $n \geq 0$.

Output : Sorted Array A

```

for  $i \leftarrow 1$  to  $n - 1$  do
    for  $j \leftarrow 1$  to  $n - i$  do
        if  $A[j] > A[j + 1]$  then
            swap( $A[j], A[j + 1]$ );
    
```

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Analysis

Number key comparisons $\sum_{i=1}^{n-1} (n - i) = \frac{n(n-1)}{2} = \Theta(n^2)$.

Number swaps in the worst case: $\Theta(n^2)$

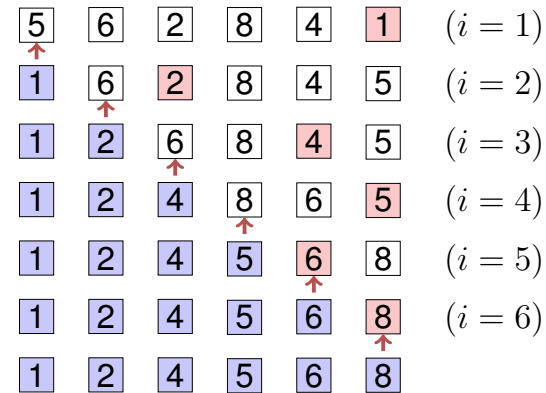
❓ What is the worst case?

⚠️ If A is sorted in decreasing order.

❓ Algorithm can be adapted such that it terminates when the array is sorted.
Key comparisons and swaps of the modified algorithm in the best case?

⚠️ Key comparisons = $n - 1$. Swaps = 0.

Selection Sort



- Iterative procedure as for Bubblesort.
- Selection of the smallest (or largest) element by immediate search.

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Algorithm: Selection Sort

Input : Array $A = (A[1], \dots, A[n])$, $n \geq 0$.

Output : Sorted Array A

```

for  $i \leftarrow 1$  to  $n - 1$  do
   $p \leftarrow i$ 
  for  $j \leftarrow i + 1$  to  $n$  do
    if  $A[j] < A[p]$  then
       $p \leftarrow j$ 
  swap( $A[i]$ ,  $A[p]$ )
  
```

Analysis

Number comparisons in worst case: $\Theta(n^2)$.

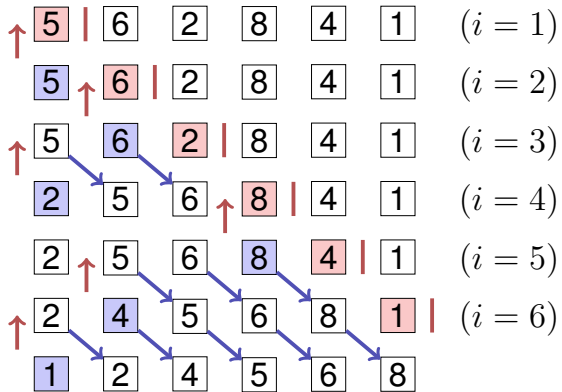
Number swaps in the worst case: $n - 1 = \Theta(n)$

Best case number comparisons: $\Theta(n^2)$.

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Insertion Sort



- Iterative procedure:
 $i = 1 \dots n$
- Determine insertion position für element i .
- Insert element i array block movement potentially required

Insertion Sort

❓ What is the disadvantage of this algorithm compared to sorting by selection?

❗ Many element movements in the worst case.

❓ What is the advantage of this algorithm compared to selection sort?

❗ The search domain (insertion interval) is already sorted. Consequently: binary search possible.

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Algorithm: Insertion Sort

Input : Array $A = (A[1], \dots, A[n])$, $n \geq 0$.

Output : Sorted Array A

for $i \leftarrow 2$ **to** n **do**

$x \leftarrow A[i]$

$p \leftarrow \text{BinarySearch}(A[1 \dots i - 1], x)$; // Smallest $p \in [1, i]$ with $A[p] \geq x$

for $j \leftarrow i - 1$ **downto** p **do**

$A[j + 1] \leftarrow A[j]$

$A[p] \leftarrow x$

Analysis

Number comparisons in the worst case:

$$\sum_{k=1}^{n-1} a \cdot \log k = a \log((n-1)!) \in \mathcal{O}(n \log n).$$

Number comparisons in the best case $\Theta(n \log n)$.⁴

Number comparisons in the worst case $\sum_{k=2}^n (k-1) \in \Theta(n^2)$

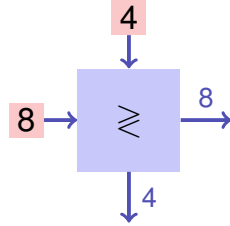
⁴With slight modification of the function BinarySearch for the minimum / maximum: $\Theta(n)$

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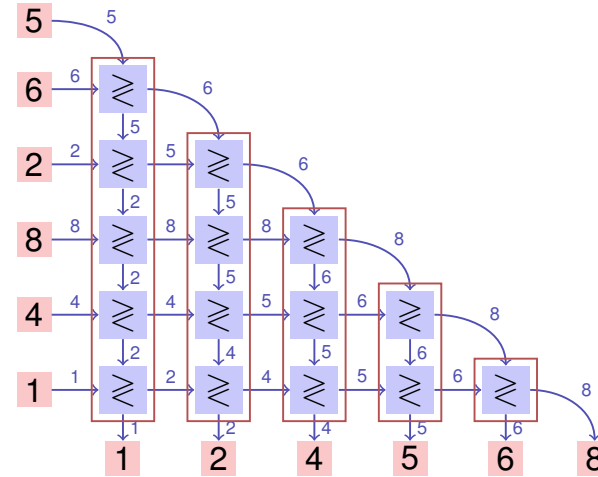
Different point of view

Sortierknoten:



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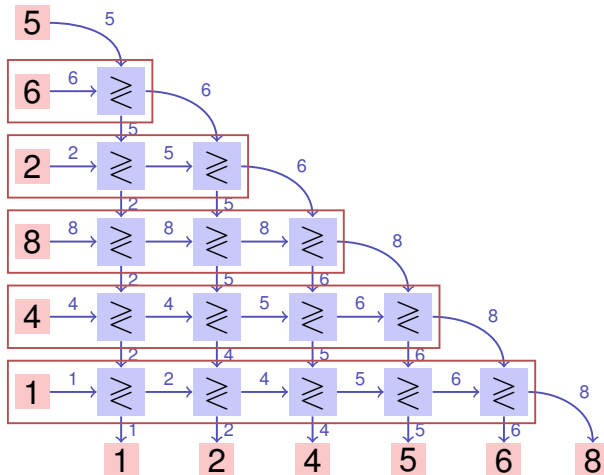
Different point of view



- Like selection sort [und like Bubblesort]

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Different point of view



- Like insertion sort

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Conclusion

In a certain sense, Selection Sort, Bubble Sort and Insertion Sort provide the same kind of sort strategy. Will be made more precise.⁵

⁵In the part about parallel sorting networks. For the sequential code of course the observations as described above still hold.

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Shellsort

Insertion sort on subsequences of the form $(A_{k,i})$ ($i \in \mathbb{N}$) with decreasing distances k . Last considered distance must be $k = 1$.

Good sequences: for example sequences with distances $k \in \{2^i 3^j \mid 0 \leq i, j\}$.

Shellsort

9	8	7	6	5	4	3	2	1	0	
1	8	7	6	5	4	3	2	9	0	insertion sort, $k = 4$
1	0	7	6	5	4	3	2	9	8	
1	0	3	6	5	4	7	2	9	8	
1	0	3	2	5	4	7	6	9	8	
1	0	3	2	5	4	7	6	9	8	insertion sort, $k = 2$
1	0	3	2	5	4	7	6	9	8	
0	1	2	3	4	5	6	7	8	9	insertion sort, $k = 1$