

## 17. Rekursion 2

Bau eines Taschenrechners, Ströme, Formale Grammatiken, Extended Backus Naur Form (EBNF), Parsen von Ausdrücken

### Naiver Versuch (ohne Klammern)

```
double lval;
std::cin >> lval;

char op;
while (std::cin >> op && op != '=') {
    double rval;
    std::cin >> rval;

    if (op == '+')
        lval += rval;
    else if (op == '*')
        lval *= rval;
    else ...
}
std::cout << "Ergebnis " << lval << "\n";
```

Eingabe 2 + 3 \* 3 =  
Ergebnis 15

## Motivation: Taschenrechner

Ziel: Bau eines Kommandozeilenrechners

### Beispiel

```
Eingabe: 3 + 5
Ausgabe: 8
Eingabe: 3 / 5
Ausgabe: 0.6
Eingabe: 3 + 5 * 20
Ausgabe: 103
Eingabe: (3 + 5) * 20
Ausgabe: 160
Eingabe: -(3 + 5) + 20
Ausgabe: 12
```

- Binäre Operatoren +, -, \*, / und Zahlen
- Fließkommaarithmetik
- Präzedenzen und Assoziativitäten wie in C++
- Klammerung
- Unärer Operator -

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### Analyse des Problems

#### Beispiel

Eingabe:

$$13 + 4 * (15 - 7 * 3) =$$

Muss gespeichert bleiben, damit jetzt ausgewertet werden kann!

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# Analyse des Problems

$$13 + 4 * (15 - 7 * 3)$$

Das "Verstehen" eines Ausdrucks erfordert Vorausschau auf kommende Symbole!

Wir werden die Symbole elegant mittels Rekursion zwischenspeichern.

Wir brauchen ein neues formales (von C++ unabhängiges) Handwerkszeug.

# Formale Grammatiken

- Alphabet: endliche Menge von Symbolen
- Sätze: endlichen Folgen von Symbolen

Eine formale Grammatik definiert, welche Sätze gültig sind.

Zur Beschreibung der Grammatik verwenden wir:

*Extended Backus Naur Form (EBNF)*

Short Communications  
Programming Languages

## What Can We Do about the Unnecessary Diversity of Notation for Syntactic Definitions?

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**Key Words and Phrases:** syntactic description  
language, extended BNF  
**CR Categories:** 4.20

The population of programming languages is steadily growing, and there is no end of this growth in sight. Many language definitions appear in journals, many are found in technical reports, and perhaps an even greater number remains confined to proprietary circles. After frequent exposure to these definitions, one cannot fail to notice the lack of "common denominators." The only widely accepted fact is that the language structure is defined by a syntax. But even notation for syntactic description eludes any commonly agreed standard form, although the underlying ancestor is invariably the Backus-Naur Form of the Algol 60 report. As variations are often only slight, they become annoying for their very lack of an apparent motivation.

Out of sympathy with the troubled reader who is weary of adapting to a new variant of BNF each time another language definition appears, and without any claim for originality, I venture to submit a simple notation that has proven valuable and satisfactory in use. It has the following properties to recommend it:

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1. The notation distinguishes clearly between meta-terminal, and nonterminal symbols.
2. It does not exclude characters used as metasympols from use as symbols of the language (as e.g. "[" in BNF).
3. It contains an explicit iteration construct, and thereby avoids the heavy use of recursion for expressing simple repetition.
4. It avoids the use of an explicit symbol for the empty string (such as empty) or ε.
5. It is based on the ASCII character set.

This meta language can therefore conveniently be used to define its own syntax, which may serve here as an example of its use. The word *identifier* is used to denote *nonterminal symbol*, and *literal* stands for *terminal symbol*. For brevity, *identifier* and *character* are not defined in further detail.

```

syntax = [production].
production = identifier "=" expression ":",
expression = term ["(" term),
term = factor {factor},
factor = identifier | literal | "(" expression ")" |
        "[" expression "]" | "[" expression "]" |
literal = "..." character {character} "..."

```

Repetition is denoted by curly brackets, i.e. [a] stands for ε | a | aa | aaa | ... . Optionality is expressed by square brackets, i.e. [a] stands for ε | a. Parentheses merely serve for grouping, e.g. (a|b)c stands for a|bc. Terminal symbols, i.e. literals, are enclosed in quote marks (and, if a quote mark appears as a literal itself, it is written twice), which is consistent with common practice in programming languages.

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# Ausdrücke

$$-(3 - (4 - 5)) * (3 + 4 * 5) / 6$$

Was benötigen wir in einer Grammatik?

- Zahl, ( Ausdruck )
- -Zahl, - ( Ausdruck )
- Faktor \* Faktor, Faktor
- Faktor / Faktor, ...
- Term + Term, Term
- Term - Term, ...

Faktor

Term

Ausdruck

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## Die EBNF für Ausdrücke

Ein Faktor ist

- eine Zahl,
- ein geklammerter Ausdruck oder
- ein negierter Faktor.

```
factor = unsigned_number  
      | "(" expression ")"  
      | "-" factor.
```

*Nicht-terminales Symbol* (pointing to "expression")

*Terminales Symbol* (pointing to "(" and ")")

*Alternative* (pointing to the vertical bar "|")

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## Die EBNF für Ausdrücke

Ein Term ist

- Faktor,
- Faktor \* Faktor, Faktor / Faktor,
- Faktor \* Faktor \* Faktor, Faktor / Faktor \* Faktor, ...
- ...

```
term = factor { "*" factor | "/" factor }.
```

*Optionale Repetition* (pointing to the curly braces "{}")

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## Die EBNF für Ausdrücke

```
factor = unsigned_number  
      | "(" expression ")"  
      | "-" factor.
```

```
term = factor { "*" factor | "/" factor }.
```

```
expression = term { "+" term | "-" term }.
```

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## Parseen

- **Parseen:** Feststellen, ob ein Satz nach der EBNF gültig ist.
- **Parser:** Programm zum Parseen
- **Praktisch:** Aus der EBNF kann (fast) automatisch ein Parser generiert werden:
  - Regeln werden zu Funktionen
  - Alternativen und Optionen werden zu `if`-Anweisungen
  - Nichtterminale Symbole auf der rechten Seite werden zu Funktionsaufrufen
  - Optionale Repetitionen werden zu `while`-Anweisungen

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## Funktionen

## (Parser mit Auswertung)

Ausdruck wird aus einem Eingabestrom gelesen.

```
// POST: extracts a factor from is
//       and returns its value
double factor (std::istream& is);

// POST: extracts a term from is
//       and returns its value
double term (std::istream& is);

// POST: extracts an expression from is
//       and returns its value
double expression (std::istream& is);
```

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## Vorausschau von einem Zeichen...

... um jeweils die richtige Alternative zu finden.

```
// POST: leading whitespace characters are extracted
//       from is, and the first non-whitespace character
//       is returned (0 if there is no such character)
char lookahead (std::istream& is)
{
    if (is.eof())           // eof: end of file (checks if stream is finished)
        return 0;
    is >> std::ws;         // skip all whitespaces
    if (is.eof())           // end of stream
        return 0;
    return is.peek();       // next character in is
}
```

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## Rosinenpickerei

... um jeweils nur das gewünschte Zeichen zu extrahieren.

```
// POST: if ch matches the next lookahead then consume it
//       and return true; return false otherwise
bool consume (std::istream& is, char ch)
{
    if (lookahead(is) == ch){
        is >> ch;
        return true;
    }
    return false;
}
```

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## Faktoren auswerten

```
double factor (std::istream& is)
{
    double v;
    if (consume(is, '(')) {
        v = expression (is);
        consume(is, ')');
    } else if (consume(is, '-')) {
        v = -factor (is);
    } else {
        is >> v;
    }
    return v;
}
```

```
factor = "(" expression ")"
        | "-" factor
        | unsigned_number.
```

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## Terme auswerten

```
double term (std::istream& is)
{
    double value = factor (is);
    while(true){
        if (consume(is, '*'))
            value *= factor (is);
        else if (consume(is, '/'))
            value /= factor(is)
        else
            return value;
    }
}
```

term = factor { "\*" factor | "/" factor }.

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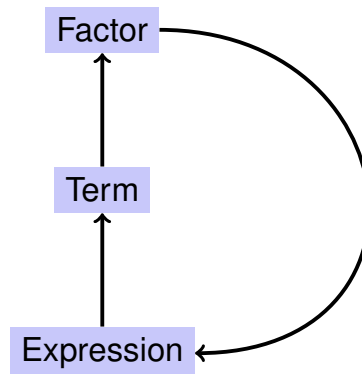
## Ausdrücke auswerten

```
double expression (std::istream& is)
{
    double value = term(is);
    while(true){
        if (consume(is, '+'))
            value += term (is);
        else if (consume(is, '-'))
            value -= term(is)
        else
            return value;
    }
}
```

expression = term { "+" term | "-" term }.

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## Rekursion!



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## EBNF — Und es funktioniert!

EBNF (calculator.cpp, Auswertung von links nach rechts):

```
factor    = unsigned_number
           | "(" expression ")"
           | "-" factor.

term      = factor { "*" factor | "/" factor }.

expression = term { "+" term | "-" term }.
```

```
std::stringstream input ("1-2-3");
std::cout << expression (input) << "\n"; // -4
```

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